

On the Interfacial Potential Differences for the Extraction of Alkaline-Earth Metal Picrates by 18-Crown-6 Ether Derivatives into Nitrobenzene

Yoshihiro Kudo* and Tomoyo Takeuchi

Graduate School of Science, Chiba University, 1-33 Yayoi-cho Inage-ku, Chiba 263-8522, Japan

Abstract

Individual distribution constants ($K_{D,A}$) of picrate ion (Pic^-) into nitrobenzene (NB) were determined at 298 K and given values of ionic strength, together with the determination of an extraction constant (K_{ex}) for the extraction of alkaline-earth metal picrates, MPic_2 , by 18-crown-6 ether (18C6) and benzo-18C6 (B18C6). Here, $K_{D,A}$ and K_{ex} were defined as $[\text{A}^-]_{\text{NB}}/[\text{A}^-]$ and $[\text{MLA}_2]_{\text{NB}}/([\text{M}^{2+}][\text{L}]_{\text{NB}}[\text{A}^-]^2)$, respectively; A⁻ shows Pic^- , L does either 18C6 or B18C6 and the subscript “NB” refers to the NB phase. Interfacial potential differences ($\Delta\phi_{\text{eq}}$ in a V unit) at extraction equilibria were evaluated from differences between the experimental $\log K_{D,\text{Pic}}$ and its standardized values ($\log K_{D,\text{Pic}}^{\text{S}}$) which have been determined by electrochemical measurements at a water/NB interface. By a combination with the K_{ex} values, other extraction constants, $K_{\text{ex}\pm} = [\text{MLPic}^+]_{\text{NB}}/([\text{Pic}^-]_{\text{NB}}[\text{M}^{2+}][\text{L}]_{\text{NB}}[\text{Pic}^-]^2)$, were also determined. Electrochemically-standardized $\log K_{\text{ex}\pm}$ values, $\log K_{\text{ex}\pm}^{\text{S}}$ ones, were calculated from the relation of $\log K_{\text{ex}\pm}^{\text{S}} = (\Delta\phi_{\text{eq}}/0.05916) + \log K_{\text{ex}\pm}^{\text{S}}$ at 298 K. Using the $\log K_{\text{ex}\pm}^{\text{S}}$ values, their correlation with the $\log K_{\text{ex}\pm}$ ones was discussed. Additionally, ion-pair formation constants ($K_{1,\text{NB}}$ & $K_{2,\text{NB}}$) for the stepwise reactions of ML^{2+} with Pic^- in the NB phase were evaluated from K_{ex}^{S} , $K_{\text{ex}\pm}$ and another constant ($K_{\text{ex}2\pm}$) reported before at $\Delta\phi_{\text{eq}} = 0$. Here, $K_{2,\text{NB}}$ was evaluated from $K_{\text{ex}}/K_{\text{ex}\pm}$ and $K_{1,\text{NB}}$ is defined as $[\text{MLPic}^+]_{\text{NB}}/([\text{ML}^{2+}]_{\text{NB}}[\text{Pic}^-]_{\text{NB}})$, which was evaluated from the relation of $K_{1,\text{NB}} = K_{\text{ex}\pm}/K_{\text{ex}2\pm}$. Moreover, reproductions of the electrochemically-standardized $K_{\text{ex}\pm}^{\text{S}}$ and $K_{\text{ex}2\pm}$ values were tried, using the $\Delta\phi_{\text{eq}}$ values and relations between $K_{\text{ex}\pm}$ or $K_{\text{ex}2\pm}$ and component equilibrium constants constituting their extraction ones. Consequently, a functional expression of $K_{\text{ex}\pm}^{\text{S}}$ with $\Delta\phi_{\text{eq}}$ was extended into the MPic_2 -L extraction systems, in addition to the AgPic -L extraction ones reported previously.

Keywords: Interfacial potential differences; Individual distribution constants of ions; Extraction into nitrobenzene; Alkaline-earth metal picrates; 18-Crown-6 ether derivatives

Introduction

Recently one of the authors has reported an expression by an interfacial potential difference ($\Delta\phi_{\text{eq}}$) of an extraction constant on silver picrate extraction with crown ethers (L) into 1,2-dichloroethane (DCE) or dichloromethane (DCM) [1]. In this study, its extraction constant has been defined as $[\text{AgL}^+]_{\text{o}}[\text{Pic}^-]_{\text{o}}/([\text{Ag}^+][\text{L}]_{\text{o}}[\text{Pic}^-]_{\text{o}})$, in addition to the well-known definition of $K_{\text{ex}} = [\text{AgL}^+\text{Pic}^-]_{\text{o}}/([\text{Ag}^+][\text{L}]_{\text{o}}[\text{Pic}^-]_{\text{o}})$, where the subscript “o” and Pic^- denote an organic (o) phase, such as DCE and DCM, and picrate ion, respectively. An introduction of $\Delta\phi_{\text{eq}}$ in extraction experiments also gave an answer for a problem of the deviation between the electrochemically-determined $K_{D,A}$ values and extraction-experimentally-determined values [1,2]. Here, the symbol $K_{D,A}$ refers to an individual distribution constant ($= [\text{A}^-]_{\text{o}}/[\text{A}^-]$) of A^- into the o phase. Similar problems have been observed in the extraction of divalent metal salts, such as CdPic_2 , PbPic_2 and CaPic_2 , by L into various diluents [3-5].

In the present paper, we determined at 298 K the $K_{D,\text{Pic}}$ values for the extraction of alkaline-earth metal picrates (MPic_2 ; M = Ca, Sr, Ba) by 18-crown-6 ether (18C6) or benzo-18C6 (B18C6) into nitrobenzene (NB) which shows the higher polarity. Then, the $\Delta\phi_{\text{eq}}$ values were evaluated from differences between the $K_{D,\text{Pic}}$ values electrochemically-determined and those determined by the present extraction-experiments. Here, the electrochemically-determined constant was expressed as $K_{D,\text{Pic}}^{\text{S}}$, showing the equilibrium constant standardized at $\Delta\phi_{\text{eq}} = 0$ V [1,6,7]. Moreover, the functional expressions of $K_{\text{ex}\pm}^{\text{S}}$, $K_{\text{ex}2\pm}$ and K_{ex} by $\Delta\phi_{\text{eq}}$ were examined; the symbols, $K_{\text{ex}\pm}$, $K_{\text{ex}2\pm}$ and K_{ex} , refer to $[\text{MLA}^+]_{\text{o}}[\text{A}^-]_{\text{o}}/([\text{M}^{2+}][\text{L}]_{\text{o}}[\text{A}^-]^2)$, $[\text{ML}^{2+}]_{\text{o}}[\text{A}^-]_{\text{o}}^2/([\text{M}^{2+}][\text{L}]_{\text{o}}[\text{A}^-]^2)$ and $[\text{MLA}_2]_{\text{o}}/([\text{M}^{2+}][\text{L}]_{\text{o}}[\text{A}^-]^2)$, respectively [3,4,8]. On the basis of the above values determined, the $\text{M}^{\text{II}}\text{Pic}_2$ extraction system with L into NB was characterized.

Theory

Derivation of a potential difference at the water/o interface

Using properties of electrochemical potentials $\bar{\mu}_i$ [9,10], we had reported relations between $\Delta\phi_{\text{eq}}$ and the constants expressing overall extraction equilibria, such as $\text{M}^{2+} + \text{L}_o + \text{A}^- \rightleftharpoons \text{MLA}_o^+$ and $\text{M}^+ + \text{L}_o + \text{A}^- \rightleftharpoons \text{ML}_o^+ + \text{A}_o^-$ [1]. The same handling [1,11] was applied for the present extraction equilibria. For example, the authors will apply it to the process:



This process was expressed by $\bar{\mu}_i$ as

$$\begin{aligned} \bar{\mu}_M + \bar{\mu}_{L,o} + 2\bar{\mu}_A &= \bar{\mu}_{\text{MLA},o} + \bar{\mu}_{A,o} \quad (2) \\ \mu_M^0 + RT \ln a_M + 2F\phi_M + \mu_{L,o}^0 + RT \ln a_{L,o} + 2(\mu_A^0 + RT \ln a_A - F\phi_A) \\ &= \mu_{\text{MLA},o}^0 + RT \ln a_{\text{MLA},o} + F\phi_{\text{MLA},o} + \mu_{A,o}^0 + RT \ln a_{A,o} - F\phi_{A,o} \quad (2a) \end{aligned}$$

Rearranging this equation for the $K_{\text{ex}\pm}$ definition, then we obtained

$$\begin{aligned} RT \ln K_{\text{ex}\pm}^0 + \mu_{\text{MLA},o}^0 + \mu_{A,o}^0 - \mu_M^0 - \mu_{L,o}^0 - 2\mu_A^0 \\ = F\{(2\phi_M - \phi_{\text{MLA},o}) - (2\phi_A - \phi_{A,o})\}. \end{aligned}$$

*Corresponding author: Yoshihiro Kudo, Graduate School of Science, Chiba University, 1-33 Yayoi-cho Inage-ku, Chiba 263-8522, Japan, Tel: +81 43 290 2786; E-mail: iakudo@faculty.chiba-u.jp

Received July 15, 2014; Accepted August 12, 2014; Published August 20, 2014

Citation: Yoshihiro K, Takeuchi T (2014) On the Interfacial Potential Differences for the Extraction of Alkaline-Earth Metal Picrates by 18-Crown-6 Ether Derivatives into Nitrobenzene. J Thermodyn Catal 5: 133. doi: 10.4172/2157-7544.1000133

Copyright: © 2014 Yoshihiro K, et al. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

Therefore, the following equations were derived:

$$\Delta\phi_{\text{eq}} = \Delta\phi_{\text{ex}\pm}^0 + (2.3RT/F)\log K_{\text{ex}\pm}^0 \quad (3)$$

with $\Delta\phi_{\text{eq}} = (2\phi_M - \phi_{\text{MLA},o}) - (2\phi_A - \phi_{A,o})$, $\Delta\phi_{\text{ex}\pm}^0 = (\mu_{\text{MLA},o}^0 + \mu_{A,o}^0 - \mu_M^0 - \mu_{L,o}^0 - 2\mu_A^0)/F$ and $K_{\text{ex}\pm}^0 = a_{\text{MLA},o} a_{A,o} / \{a_M a_{L,o} (a_A)^2\}$. Here, $\phi_{j,\alpha}$ and $a_{j,\alpha}$ denote an inner potential for species j in the phase α ($= o$) and an activity of j in the α phase, respectively; the symbols without α mean those to the water (w) phase, although there is an exception to this rule. From Equation (3), the interfacial potential difference $\Delta\phi_{\text{eq}}$ at an equilibrium was defined [1,11]; in principle, $\Delta\phi_{\text{eq}}$ has been defined as $\phi(w \text{ phase}) - \phi(o \text{ phase})$. Then, rearranging Equation (3) in a molar concentration unit, we immediately obtain

$$\Delta\phi_{\text{eq}} = \Delta\phi_{\text{ex}\pm}^{0'} + (2.3RT/F)\log K_{\text{ex}\pm} \quad (3a)$$

with $\Delta\phi_{\text{ex}\pm}^{0'} = \Delta\phi_{\text{ex}\pm}^0 + (2.3RT/F)\log [y_{\text{MLA},o} y_{A,o} / \{y_M (y_A)^2\}]$ and $K_{\text{ex}\pm} = [\text{MLA}^+]_o [\text{A}^-]_o / ([\text{M}^{2+}]_o [\text{L}]_o [\text{A}^-]_o^2)$. Here, $y_{j,\alpha}$ refers to an activity coefficient of the ionic species j ($= \text{MLA}(\text{I}), \text{A}(-\text{I}), \text{M}(\text{II})$) in the α phase; the symbol y without α shows the coefficient for the w phase; $\Delta\phi_k^{0'}$ means a standard formal potential. Similarly, equilibrium constants of other processes were expressed as functions of potential differences. These results are listed in Table 1. The condition of $\Delta\phi_{\text{eq}} = 0 \text{ V}$ was applied for some processes from their properties: namely, $\Delta\phi_{\text{eq}}$ essentially becomes zero, when all species relevant to the inner potentials are present in a single phase [1,9].

Using thermodynamic cycles and the various equilibrium constants

Process	Symbol	Relation ^a
Overall		
$\text{M}^{2+} + \text{L}_o + 2\text{A}^- \rightleftharpoons \text{MLA}_{2,o}$	K_{ex}	$\log K_{\text{ex}} = -2f\Delta\phi_{\text{ex}}^{0'}$
$\text{M}^{2+} + \text{L}_o + 2\text{A}^- \rightleftharpoons \text{MLA}_o^+ + \text{A}_o^-$	$K_{\text{ex}\pm}$	$\log K_{\text{ex}\pm} = f(\Delta\phi_{\text{eq}} - \Delta\phi_{\text{ex}\pm}^{0'})$
$\text{M}^{2+} + \text{L}_o + 2\text{A}^- \rightleftharpoons \text{ML}^{2+}_o + 2\text{A}_o^-$	$K_{\text{ex}2\pm}$	$\log K_{\text{ex}2\pm} = 2f(\Delta\phi_{\text{eq}} - \Delta\phi_{\text{ex}2\pm}^{0'})$
Component		
$\text{M}^{2+} \rightleftharpoons \text{M}^{2+}_o$	$K_{\text{D},\text{M}}$	$\log K_{\text{D},\text{M}} = 2f(\Delta\phi_{\text{eq}} - \Delta\phi_{\text{M}}^{0'})$
$\text{ML}^{2+} \rightleftharpoons \text{ML}^{2+}_o$	$K_{\text{D},\text{ML}}$	$\log K_{\text{D},\text{ML}} = 2f(\Delta\phi_{\text{eq}} - \Delta\phi_{\text{ML}}^{0'})$
$\text{A}^- \rightleftharpoons \text{A}_o^-$	$K_{\text{D},\text{A}}$	$\log K_{\text{D},\text{A}} = -f(\Delta\phi_{\text{eq}} - \phi_{\text{A}}^{0'})$
$\text{M}^{2+}_o + \text{L}_o \rightleftharpoons \text{ML}^{2+}_o$	$K_{\text{ML,org}}$	$\log K_{\text{ML,org}} = -2f\Delta\phi_{\text{ML,w}}^{0'}$
$\text{M}^{2+} + \text{L} \rightleftharpoons \text{ML}^{2+}$	K_{ML}	$\log K_{\text{ML}} = -2f\Delta\phi_{\text{ML,w}}^{0' b}$
$\text{L} \rightleftharpoons \text{L}_o$	$K_{\text{D},\text{L}}$	$\log K_{\text{D},\text{L}} = -f\Delta\phi_{\text{L}}^{0'}$
$\text{ML}^{2+}_o + \text{A}_o^- \rightleftharpoons \text{MLA}_o^+$	$K_{1,\text{org}}$	$\log K_{1,\text{org}} = -f\Delta\phi_{1,\text{org}}^{0'}$
$\text{MLA}_o^+ + \text{A}_o^- \rightleftharpoons \text{MLA}_{2,o}$	$K_{2,\text{org}}$	$\log K_{2,\text{org}} = -f\Delta\phi_{2,\text{org}}^{0'}$
$\text{ML}^{2+}_o + 2\text{A}_o^- \rightleftharpoons \text{MLA}_{2,o}$	$\beta_{\text{ip,org}}^c$	$\log \beta_{\text{ip,org}} = -2f\Delta\phi_{\text{ip,org}}^{0'}$

^a $f = F/2.3RT$. Hence, $1/f = 0.05916 \text{ V}$ at 298 K. ^b $\Delta\phi_{\text{ML,w}}^{0'}$ shows a standard formal potential for the ML^{2+} formation in the w phase. ^c $\beta_{\text{ip,org}} = K_{1,\text{org}} K_{2,\text{org}}$. Accordingly, the relation of $2\Delta\phi_{\text{ip,org}}^{0'} = \Delta\phi_{1,\text{org}}^{0'} + \Delta\phi_{2,\text{org}}^{0'}$ holds

Table 1: Relations between the potential differences, $\Delta\phi_{\text{eq}}$, $\Delta\phi_k^{0'}$ or $\Delta\phi_j^{0'}$, and $\log K_k$ values in an extraction system.

Overall process & its cycle ^a	Relation ^b
$\text{M}^{2+} + \text{L}_o + 2\text{A}^- \rightleftharpoons \text{MLA}_{2,o}$ $K_{\text{ex}} = K_{\text{D},\text{M}}(K_{\text{D},\text{A}})^2 K_{\text{ML,org}} \beta_{\text{ip,org}}$	$\Delta\phi_{\text{ex}}^{0'} = \Delta\phi_{\text{M}}^{0'} - \Delta\phi_{\text{A}}^{0'} + \Delta\phi_{\text{ML,org}}^{0'} + \Delta\phi_{\text{ip,org}}^{0'}$
$\text{M}^{2+} + \text{L}_o + 2\text{A}^- \rightleftharpoons \text{MLA}_o^+ + \text{A}_o^-$	(a) $\Delta\phi_{\text{ex}\pm}^{0'} = 2\Delta\phi_{\text{M}}^{0'} - 2\Delta\phi_{\text{A}}^{0'} + 2\Delta\phi_{\text{ML,org}}^{0'} + \Delta\phi_{1,\text{org}}^{0'} + \Delta\phi_{\text{eq}}$ (b) $\Delta\phi_{\text{ex}2\pm}^{0'} = 2\Delta\phi_{\text{ML,w}}^{0'} + 2\Delta\phi_{\text{ML}}^{0'} + \Delta\phi_{1,\text{org}}^{0'} - 2\Delta\phi_{\text{A}}^{0'} - \Delta\phi_{\text{L}}^{0'} + \Delta\phi_{\text{eq}}$
(a) $K_{\text{ex}\pm} = K_{\text{D},\text{M}}(K_{\text{D},\text{A}})^2 K_{\text{ML,org}} K_{1,\text{org}}$ (b) $K_{\text{ex}2\pm} = K_{\text{ML}} K_{\text{D},\text{ML}} K_{1,\text{org}} (K_{\text{D},\text{A}})^2 / K_{\text{D},\text{L}}$	
$\text{M}^{2+} + \text{L}_o + 2\text{A}^- \rightleftharpoons \text{ML}^{2+}_o + 2\text{A}_o^-$ $K_{\text{ex}2\pm} = K_{\text{D},\text{M}}(K_{\text{D},\text{A}})^2 K_{\text{ML,org}}$	$\Delta\phi_{\text{ex}2\pm}^{0'} = \Delta\phi_{\text{M}}^{0'} - \Delta\phi_{\text{A}}^{0'} + \Delta\phi_{\text{ML,org}}^{0'} + \Delta\phi_{\text{eq}}$

^aA thermodynamic cycle of an extraction constant expressed by the component equilibrium constants. ^b $\Delta\phi_{\text{ip,org}}^{0'} = (\Delta\phi_{1,\text{org}}^{0'} + \Delta\phi_{2,\text{org}}^{0'})/2$

Table 2: Some examples on relations between the $\Delta\phi_k^{0'}$ values and the potential differences based on component equilibrium constants.

in Table 1, we can express the overall extraction processes [1]. Thereby, it becomes possible that we express the overall extraction constants as functions of some formal potentials with $\Delta\phi_{\text{eq}}$. As an example, $K_{\text{ex}2\pm}$ (see Introduction for its definition) is expressed as $K_{\text{D},\text{M}}(K_{\text{D},\text{A}})^2 K_{\text{ML,org}}$. Taking logarithms of both sides in this equation and rearranging it based on the corresponding relations in Table 1, we easily obtain

$$\Delta\phi_{\text{ex}2\pm}^{0'} = \Delta\phi_{\text{M}}^{0'} - \Delta\phi_{\text{A}}^{0'} + \Delta\phi_{\text{ML,org}}^{0'} + \Delta\phi_{\text{eq}} \quad (4)$$

from $\Delta\phi_{\text{eq}} - \Delta\phi_{\text{ex}2\pm}^{0'} = (\Delta\phi_{\text{eq}} - \Delta\phi_{\text{M}}^{0'}) - (\Delta\phi_{\text{eq}} - \Delta\phi_{\text{A}}^{0'}) - \Delta\phi_{\text{ML,org}}^{0'}$. The same was true of K_{ex} and $K_{\text{ex}\pm}$, where the condition of $\Delta\phi_{\text{eq}} = 0 \text{ V}$ was satisfied for K_{ex} , since all species relevant to the inner potentials were present in the single phase [1,9]. Table 2 summarizes these results. According to the previous paper [1], when the $\log K_{\text{D},\text{A}}$ values are determined experimentally and the $\Delta\phi_{\text{A}}^{0'}$ ones are available, we immediately can calculate the $\Delta\phi_{\text{eq}}$ values from the relation in Table 1.

For an analytical handling of extraction processes

The extraction-constant parameter, $K_{\text{ex}}^{\text{mix}}$, has been employed for the determination of $K_{\text{D},\text{A}}$ and K_{ex} [3-5]:

$$\log K_{\text{ex}}^{\text{mix}} = \log \{([\text{MLA}_2]_o + [\text{MLA}^+]_o) / ([\text{M}^{2+}]_o [\text{L}]_o [\text{A}^-]_o^2)\}$$

$$= \log \{K_{\text{ex}} + K_{\text{D},\text{A}} / ([\text{M}^{2+}]_o [\text{L}]_o [\text{A}^-]_o)\} \quad (5)$$

under the condition of $[\text{A}^-]_o \approx [\text{MLA}^+]_o (>> 2[\text{M}^{2+}]_o + 2[\text{ML}^{2+}]_o)$. A regression analysis to the plot of $\log K_{\text{ex}}^{\text{mix}}$ versus $-\log ([\text{M}^{2+}]_o [\text{L}]_o [\text{A}^-]_o^2)$ yielded the $K_{\text{D},\text{A}}$ and K_{ex} values [3-5]. Equation (5) can be also rearranged as

$$\log K_{\text{ex}}^{\text{mix}} = \log \{K_{\text{ex}} + (K_{\text{ex}\pm} / [\text{M}^{2+}]_o [\text{L}]_o)^{1/2} [\text{A}^-]_o^{-1}\}. \quad (5a)$$

Then, this equation makes it possible that one obtains the $K_{\text{ex}\pm}$ value from the plot of $\log K_{\text{ex}}^{\text{mix}}$ versus $-\log \{([\text{M}^{2+}]_o [\text{L}]_o)^{1/2} [\text{A}^-]_o\}$. In this study, the regression analyses with Equation (5a) were performed at a fixed condition of the K_{ex} value which was determined in terms of the analysis of Equation (5) and accordingly the thus-obtained $K_{\text{ex}\pm}$ value was checked by calculating it from each experimental point (Table 3).

Evaluation of stepwise ion-pair formation constants for MLA_2 in the o phase

Stepwise ion-pair formation constants for MLA_2 in the water-saturated o phase for given $I_{\text{org,av}}$ values were evaluated from the following relations.

$$K_{1,\text{org}} = [\text{MLA}^+]_o / [\text{ML}^{2+}]_o [\text{A}^-]_o = K_{\text{ex}\pm} / K_{\text{ex}2\pm} \quad (6)$$

$$K_{2,\text{org}} = [\text{MLA}_2]_o / [\text{MLA}^+]_o [\text{A}^-]_o = K_{\text{ex}} / K_{\text{ex}\pm} \quad (7)$$

Here, the symbol, $I_{\text{org,av}}$, was defined as $(\sum I_{\text{org}}) / N$ with a number (N) of run and ionic strength (I_{org}) for the o phase. Table 3 lists the five equilibrium constants determined with the above procedures. The $K_{\text{ex}2\pm}^{\text{S}}$ values which were available from references [8] were actually used as $K_{\text{ex}2\pm}$ in the $K_{1,\text{NB}}$ -calculation with Equation (6). Strictly speaking, there

L	M	log $K_{D,A}$	log K_{ex} () ^a	log K_{ext}	log $K_{n,NB}$ () ^b	
					n=1	2
18C6	Ca	-1.43 ± 0.03	9.82 ± 0.02 (5.3×10 ⁻³)	5.44 ± 0.07 5.4 ₃ ± 0.1 ₈ ^c	5.9 [4.7] ^d	4.38 ± 0.08 (8.9×10 ⁻⁴)
	Sr	-0.98 ± 0.07	11.44 ± 0.03 (3.1×10 ⁻³)	6.9 ₂ ± 0.1 ₂ ^c 6.9 ₁ ± 0.1 ₃ ^c	5.3 [4.6] ^d	4.5 ₂ ± 0.1 ₂ ^c (4.8×10 ⁻⁴)
	Ba	-0.69 ± 0.04	10.75 ± 0.08 (4.5×10 ⁻³)	7.3 ₅ ± 0.1 ₁ ^c 7.4 ₁ ± 0.3 ₃ ^c	4.9 [3.4] ^d	3.4 ₁ ± 0.1 ₁ ^c (5.9×10 ⁻⁴)
B18C6	Ca	-1.92 ± 0.04	7.35 ± 0.08 (3.6×10 ⁻³)	2.7 ₁ ± 0.1 ₀ ^c 2.8 ₀ ± 0.2 ₉ ^c	5.0 [5.5] ^d	4.6 ₂ ± 0.1 ₁ ^c (6.9×10 ⁻⁴)
	Sr	-1.34 ± 0.04	9.41 ± 0.02 (4.0×10 ⁻³)	4.34 ± 0.08 4.3 ₃ ± 0.1 ₃ ^c	4.7 [4.6] ^d	5.07 ± 0.08 (2.3×10 ⁻⁴)
	Ba	-1.17 ± 0.02	9.51 ± 0.02 (4.7×10 ⁻³)	5.0 ₁ ± 0.1 ₁ ^c 5.0 ₀ ± 0.4 ₂ ^c	4.1 [4.2] ^d	4.5 ₀ ± 0.1 ₁ ^c (2.1×10 ⁻⁴)

^aAverage values of I in the w phase. ^bAverage values of I_{NB} in the NB phase. ^cLogarithms of average values calculated from each values of K_{ext} and their propagation errors simultaneously-calculated. ^dNumber, h , of water molecules coextracted with ML^{2+} into the NB phase. See ref. [17]

Table 3: Fundamental equilibrium constants for the extraction of alkaline-earth metal picrates by L into nitrobenzene at 298 K.

is a difference between actual contents calculated from Equations (6) and (7). See Appendix for this details.

Materials and Methods

Chemicals

Purities of commercial $Ca(NO_3)_2 \cdot 4H_2O$ {Kanto Chemical Co. (Kanto), guaranteed reagent (GR)}, $Sr(NO_3)_2$ (Kanto, GR) and $Ba(NO_3)_2$ {Wako Pure Chemical Industries (Wako), GR} were checked by a chelatometric titration with disodium salt of EDTA. Also, a purity of commercially-available picric acid, HPic, with amount of 10-15%(w/w) water (Wako, GR) was checked by an acid-base titration [1,5]. Commercial crown ethers, 18C6 (99%, Acros) and B18C6 (98%, Aldrich), were dried at room temperature for >20 h under a reduced pressure. Their purities were checked by measurements of the melting points: 39₇-40₁ or 37₂-39₉ °C for 18C6; 42₃-42₈ for B18C6. Additionally, their water contents were determined by a Karl-Fischer titration: 0.462₈%(w/w) for 18C6 and 0.410₇ for B18C6. Nitrobenzene (Kanto, GR) was washed three-times with water and then kept at a water-saturated condition. Other chemicals were of GR grades and used without further purifications. A tap water was distilled once with a still of the stainless steel and then purified by passing through the Autopure system (type WT101 UV, Yamato/Millipore). Thus purified water was employed for the present work.

Extraction procedures

Alkaline-earth metal nitrates $M(NO_3)_2$, HPic and L were mixed with 0.002 mol dm⁻³ HNO₃ in a stoppered glass-tube of about 30cm³ and then the same volume of NB was added in its solution. Their total concentrations were $[Ca(NO_3)_2]_t = 0.0012$ mol dm⁻³, $[HPic]_t = 0.0024$ and $[18C6]_t = (0.70-7.0) \times 10^{-4}$; $[Sr(NO_3)_2]_t = 6.8 \times 10^{-4}$, $[HPic]_t = 0.0014$ and $[18C6]_t = (0.86-6.4) \times 10^{-4}$; $[Ba(NO_3)_2]_t = 8.8 \times 10^{-4}$, $[HPic]_t = 0.0018$ and $[18C6]_t = (0.071-2.6) \times 10^{-3}$ and $[Ca(NO_3)_2]_t = 8.0 \times 10^{-4}$, $[HPic]_t = 1.6 \times 10^{-3}$ and $[B18C6]_t = (0.080-2.4) \times 10^{-3}$; $[Sr(NO_3)_2]_t = 4.1 \times 10^{-4}$, $[HPic]_t = 8.2 \times 10^{-4}$ and $[B18C6]_t = (0.082-2.5) \times 10^{-3}$; $[Ba(NO_3)_2]_t = 3.5 \times 10^{-4}$, $[HPic]_t = 7.1 \times 10^{-4}$ and $[B18C6]_t = (0.032-2.0) \times 10^{-3}$. The thus-prepared glass tube was shaken for 1 minute by hand and was agitated at 298 ± 0.2 K for 2 h in a water bath (Iwaki, type WTE-24) equipped with a driver unit (Iwaki, SHK driver) and a thermoregulator (Iwaki, type CTR-100). After this operation, its mixture was centrifuged with a Kokusan centrifuge (type 7163-4.8.20) for 7 minutes.

A portion of the separated NB phase was transferred into another

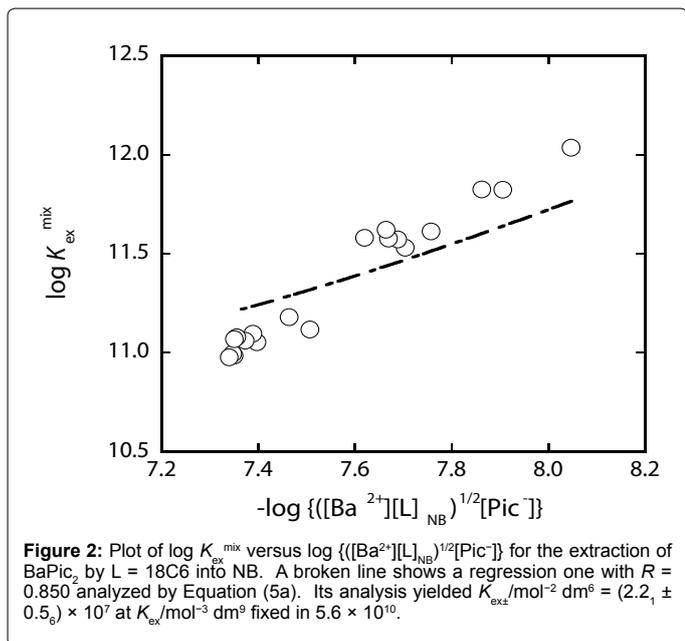
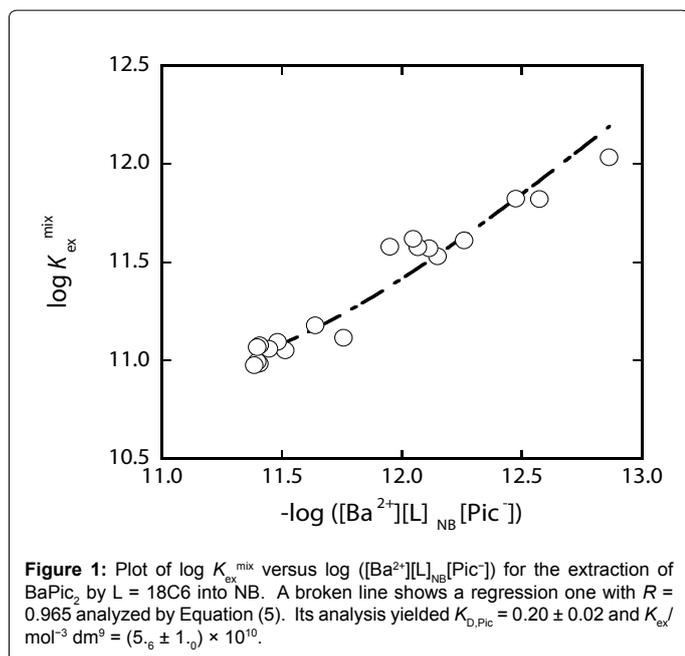
stoppered glass-tube and then 0.1 mol dm⁻³ HNO₃ was added in this tube. By shaking the tube, all M(II) species in the NB phase were back-extracted into the HNO₃ solution. If necessary, the operation for this back extraction was repeated. An amount of all the M(II) species in the aqueous HNO₃ solution was determined by a Hitachi polarized Zeeman atomic absorption spectrophotometer (type Z-6100) with a hollow cathode lamp of Ca (type 10-020, Mito-rika Co. under the license of Hitachi, Ltd.; measured wavelength: 422.7 nm) or Sr (type 10-038, Mito-rika Co.; 460.7 nm). A calibration-curve method was employed for the determination of the M(II) concentration by AAS. For the Ba(II) determination, a >0.1 mol dm⁻³ NaOH solution was added in the back-extracted solution with Pic⁻ and then its Ba(II) solution was measured at 355 nm based on the Pic⁻ absorption and 298 K by a spectrophotometer (Hitachi, type U-2001). The Ba(II) concentration was determined with a calibration curve which had been prepared at 355 nm. On the other hand, the pH value in the separated w phase was measured at 298 K with the same electrode and pH/ion meter [1,4,5].

Determination of K_{ex}^{mix}

We used here the same extraction model as that [5] for sub-analysis described previously. Its component equilibria are 1) $M^{2+} + A^- \rightleftharpoons MA^+$ [12], 2) $A^- \rightleftharpoons A^-$, 3) $M^{2+} \rightleftharpoons M^{2+}$, 4) $MLA^+ + A^- \rightleftharpoons MLA_{2,0}$, 5) $ML^{2+} \rightleftharpoons ML^{2+}$, 6) $L \rightleftharpoons L$, 7) $M^{2+} + L \rightleftharpoons ML^{2+}$, 8) $M^{2+} + L \rightleftharpoons ML^{2+}$, 9) $H^+ + A^- \rightleftharpoons HA$ [4], 10) $HA \rightleftharpoons HA$ [4], 11) $HA \rightleftharpoons H^+ + A^-$ [13], 12) $H^+ \rightleftharpoons H^+$ [6], 13) $X^- \rightleftharpoons X^-$ [11] and 14) $H^+ + X^- \rightleftharpoons HX$ [11], where the symbol HX shows a strong acid, such as HNO₃ and HCl, in water. In particular, the two reactions, 7) and 8), indirectly yielded the process 5). Also, the parentheses with the asterisks show that their equilibrium constants at 298 K have been already determined by several methods (see below for some values).

The equilibrium constants for the reactions 1) and 9) were estimated taking account of the ionic strength, I , for the w phases in a successive approximation [3,5]. Here, the formation constants (K_{MA}) for $MA^+ = MPic^+$ ($M = Sr, Ba$) in the w phase were determined by the same method as that [4] reported before: as the log K_{MPic} values at 298 K and $I \rightarrow 0$ mol dm⁻³, 2.1₈ for $M = Sr$ and 2.0₈ for Ba were obtained. While the K_{CaPic} value was estimated with the value available from reference [12].

The procedure for the calculation of K_{ex}^{mix} values by the successive approximation was essentially the same as that [3] described previously (see the theoretical section). Plots of $\log(D_{expl}/[Pic^-]^2)$ versus $\log[L]_{NB}$ gave a straight line with a slope of 0.56 and an intercept of 7.9 for the CaPic₂-18C6 system, 0.91 and 11.1 ($\approx \log K_{ex}$) for SrPic₂-18C6, 0.62 and 9.4 for BaPic₂-18C6, 0.38 and 5.9 for CaPic₂-B18C6, 0.65 and 8.5 for SrPic₂-B18C6 and 0.44 and 7.9 for BaPic₂-B18C6. Here, the distribution ratio D_{expl} is defined as $[AAS\text{-analyzed } M(II)]_{NB} / \{ [M(NO_3)_2]_t - [AAS\text{-analyzed } M(II)]_{NB} \}$ and the intercept corresponds to the log K_{ex} value only when the slope is about unity [3-5]. Except for the SrPic₂-18C6 system, the compositions of M(II):L:Pic(-) were assumed to be 1:1:2 in the determination of $K_{D,Pic}$, K_{ex} and K_{ext} [3-5]. The slope's values less than unity indicate dissociations of $MLPic_2$ in the NB phases [4]. Figures 1 and 2 show the plots for the BaPic₂-18C6 extraction system based on Equations (5) and (5a), respectively, yielding the $K_{D,Pic}$, K_{ex} and K_{ext} values (Table 3). The less correlation coefficient (R) of the plot in Figure 2 may reflect the defect in the sub-analytical extraction model



[4,5], that is, the absence of the ion-pair formation for $MLPic_2$ in the w phase. Also, the other extraction systems yielded similar plots, from which we got similarly these three kinds of values (Tables 3).

In the determination of $K_{D,Pic}$, K_{ex} and $K_{\text{ex}\pm}$ for the $BaPic_2$ -L extraction system, it was assumed that a total amount, $[Ba(II)]_{\text{NB,t}}$ of $Ba(II)$ in the NB phase nearly equals the half of that, $[Pic^-]_{\text{NB,t}}$ of Pic^- in the NB one. This assumption was derived as follows. A charge balance equation for the NB phase was essentially

$$2[Ba^{2+}]_{\text{NB}} + 2[BaL^{2+}]_{\text{NB}} + [BaLPic^+]_{\text{NB}} + [H^+]_{\text{NB}} = [Pic^-]_{\text{NB}} + [X^-]_{\text{NB}} \quad (8)$$

where the distribution of $BaPic^+$ into the NB phase was neglected, because its data were not available. When $[H^+]_{\text{NB}} \approx [X^-]_{\text{NB}}$ holds, Equation (8) becomes $2[Ba^{2+}]_{\text{NB}} + 2[BaL^{2+}]_{\text{NB}} + [BaLPic^+]_{\text{NB}} \approx [Pic^-]_{\text{NB}}$.

Rearranging this equation and adding $2[BaLPic_2]_{\text{NB}}$ in its both sides, we can immediately obtain

$$[Pic^-]_{\text{NB}} + 2[BaLPic_2]_{\text{NB}} = [Pic^-]_{\text{NB,t}} \\ \approx 2[Ba^{2+}]_{\text{NB}} + 2[BaL^{2+}]_{\text{NB}} + [BaLPic^+]_{\text{NB}} + 2[BaLPic_2]_{\text{NB}} \quad (8a)$$

Hence, when the condition of $2[BaLPic_2]_{\text{NB}} > [BaLPic^+]_{\text{NB}}$ ($> 2[BaL^{2+}]_{\text{NB}} + 2[Ba^{2+}]_{\text{NB}}$) holds, the half of the left hand side of Equation (8a) approximately becomes $[Ba^{2+}]_{\text{NB}} + [BaL^{2+}]_{\text{NB}} + [BaLPic^+]_{\text{NB}} + [BaLPic_2]_{\text{NB}}$, namely $[Ba(II)]_{\text{NB,t}}$. We were able to determine spectrophotometrically the $([Pic^-]_{\text{NB}} + 2[BaLPic_2]_{\text{NB}})$ value at least by the back extraction experiments.

Results and Discussion

Tendencies of $K_{D,Pic}$, K_{ex} , $K_{\text{ex}\pm}$ and $K_{1,NB}$ at $n = 1, 2$

As can be seen from Table 3, the $\log K_{D,Pic}$ values are different from each other in spite of the same definition. These are in the orders of $Ca < Sr < Ba$ for a given L. Also, the orders are $B18C6 < 18C6$ for a given M(II). Thus, these $K_{D,Pic}$ orders are influenced by sizes [14,15] of M^{2+} and L, not cavity sizes of L; molar volumes of L were reported to be $214 \text{ cm}^3 \text{ mol}^{-1}$ for $L = 18C6$ and 252 for $B18C6$ [15].

The values of both $\log K_{\text{ex}}$ and $\log K_{\text{ex}\pm}$ were in the orders of $Ca < Sr < Ba$ (Table 3). These tendencies are similar to those for $\log K_{D,M}^s$ and $\log K_{ML,NB}$ (see below for these values). Such facts suggest the presence of these equilibrium constants in the thermodynamic cycles (Table 2). Also, two procedures for evaluating the $\log K_{\text{ex}\pm}$ values in Table 3 well agreed within calculation errors. These facts support that the regression analyses based on Equation (5a) are essentially valid under the conditions of constant K_{ex} values.

Orders of the $\log K_{1,NB}$ values were $Ca > Sr > Ba$ for the both L, when we neglected differences in I_{NB} among the extraction systems (see Table 3 for I_{NB}). On the other hand, the $\log K_{2,NB}$ values were $Ca < Sr > Ba$. These differences suggest that sizes of $M(II)$ are more-effectively reflected to stability of the 1st-step ion-pair formation than to that of the 2nd-step formation. In other words, these results seem to be due to differences in a size and/or charges, such as the formal and net charges, between ML^{2+} and $MLPic^+$ as reaction species in NB saturated with water. Also, such effects may be reduced in the more-bulky $SrPic_2$ - and $BaPic_2$ - $B18C6$ systems.

As another explanation for the $K_{2,NB}$ orders, it can be considered that the I_{NB} values of the $Ca(II)$ system are largest of all the systems. The I_{NB} orders were of $M = Ca > Sr < Ba$ for $L = 18C6$ and $Ca > Sr \geq Ba$ for $B18C6$ (Table 3). The highest I_{NB} values for the $Ca(II)$ systems may cause the lowest $K_{2,NB}$ values. While their values were less effective for the $K_{1,NB}$ values, because $K_{1,NB}$ is constituted by the concentrations of all the ionic species.

If the 1st-step ion-pair formation is assumed to be



with $p = h - m$, then $K_{1,NB}$ can be expressed as $K_{1,NB} / ([H_2O]_{\text{NB}})^p$ with $K_{1,NB}' = [MLPic^+]_{\text{NB}} ([H_2O]_{\text{NB}})^p / [ML^{2+}]_{\text{NB}} [Pic^-]_{\text{NB}}$ (as an expression without a hydrated H_2O). Here, the hydration of Pic^- in the NB phase was neglected [16]. From Table 3, the larger the h values [17] are, the larger the $K_{1,NB}$ values become. These facts suggest that the m values are about a constant and thereby the p values are proportional to the h ones. Taking logarithms of the both sides of the equation, $K_{1,NB} = K_{1,NB}' / ([H_2O]_{\text{NB}})^p$, we can immediately obtain the equation, $\log K_{1,NB} = \log K_{1,NB}' - p \times \log [H_2O]_{\text{NB}}$. Under the conditions of $[H_2O]_{\text{NB}} (= 0.178 \text{ mol}$

dm^{-3} at 298 K [17,18]) < 1 and $p > 0$, the equation becomes $\log K_{1,\text{NB}} = \log K_{1,\text{NB}}' + 0.750p$. Therefore, the $\log K_{1,\text{NB}}$ values basically increase with an increase in p and consequently can increase with that in h (Table 3). The above results suggest the existence of the reaction (9) with H_2O molecules in NB phase, as reported before on the process of $\text{M}^+ + \text{L}_{\text{NB}} + \text{A}^- \rightleftharpoons \text{ML}_{\text{NB}}^+ + \text{A}^-_{\text{NB}}$ [8].

Calculation of the $\Delta\phi_{\text{eq}}$ values from the experimental $\log K_{\text{D,Pic}}$ values

Using the relation of $\log K_{\text{D,A}} = -(\Delta\phi_{\text{eq}} - \Delta\phi_{\text{A}}^0)/0.05916$ at 298 K (Table 1), we calculated the $\Delta\phi_{\text{eq}}$ values from the $\log K_{\text{D,Pic}}$ and $\Delta\phi_{\text{Pic}}^{\text{or}}$ ones, where the $\Delta\phi_{\text{Pic}}^{\text{or}}$ value of 3.0×10^{-3} V [6] at the w/NB interface was employed. Thus obtained values are summarized in Table 4. The $\Delta\phi_{\text{eq}}$ range for the 18C6 system was a little smaller than that for B18C6 one. From a comparison with the $\log K_{\text{ex}\pm}$ values in Table 3, the smaller the $\Delta\phi_{\text{eq}}$ values are, the larger the $\log K_{\text{ex}\pm}$ ones become. This trend is similar to that reported previously for the extraction of AgPic by B18C6 and benzo-15-crown-5 ether B15C5 into DCE or DCM [1].

Determination of the $\log K_{\text{ex}\pm}^{\text{s}}$ and $\log K_{\text{ex}2\pm}^{\text{s}}$ values

The $\Delta\phi_{\text{ex}\pm}^{\text{or}}$ values were evaluated from the $\Delta\phi_{\text{eq}}$ and $\log K_{\text{ex}\pm}$ values (Tables 3&4) using $\log K_{\text{ex}\pm} = (\Delta\phi_{\text{eq}} - \Delta\phi_{\text{ex}\pm}^{\text{or}})/0.05916$ listed in Table 1. After these evaluations, the $\log K_{\text{ex}\pm}^{\text{s}}$ values were calculated from the same equation at the condition of $\Delta\phi_{\text{eq}} = 0$ V. The same values were evaluated from $\Delta\phi_{\text{ex}\pm}^{\text{or}} = 2\phi_{\text{M}}^{\text{or}} - 2\Delta\phi_{\text{A}}^{\text{or}} + 2\Delta\phi_{\text{ML,org}}^{\text{or}} + \Delta\phi_{1,\text{org}}^{\text{or}} + \Delta\phi_{\text{eq}}$ in Table 2 and then $\log K_{\text{ex}\pm}^{\text{s}} = -\Delta\phi_{\text{ex}\pm}^{\text{or}}/0.05916$. Here, we calculated the $\Delta\phi_{\text{M}}^{\text{or}}$ values from $\log K_{\text{D,M}}^{\text{s}} = -11.799$ for M = Ca, -11.562 for Sr and -10.818 for Ba [19] and similarly the $\Delta\phi_{\text{ML,NB}}^{\text{or}}$ values from $\log K_{\text{ML,NB}} = 11.2$ for $\text{ML}^{2+} = \text{Ca}(\text{18C6})^{2+}$, 13.1 for $\text{Sr}(\text{18C6})^{2+}$, 13.4 for $\text{Ba}(\text{18C6})^{2+}$, $\log K_{\text{ML,NB}} = 9.43$ for $\text{Ca}(\text{B18C6})^{2+}$, 11.1 for $\text{Sr}(\text{B18C6})^{2+}$ and 11.6 for $\text{Ba}(\text{B18C6})^{2+}$ [20]. Also, the $\Delta\phi_{1,\text{NB}}^{\text{or}}$ values were calculated from the relation of $\log K_{1,\text{NB}} = -\Delta\phi_{1,\text{NB}}^{\text{or}}/0.05916$ (Table 1) and the $\log K_{1,\text{NB}}^{\text{s}}$ values in Table 3. Similar evaluations were performed for the $\log K_{\text{ex}2\pm}^{\text{s}}$ values using the relation among the potentials listed in Table 2.

As can be seen from Table 4, the $\log K_{\text{ex}\pm}^{\text{s}}$ values calculated from the relation in Table 1 are equal or close to those calculated from that in Table 2. Especially, a little larger deviations for the BaPic₂-L systems may be due to the approximation of $[\text{Ba}(\text{II})]_{\text{NB},\text{t}} \approx [\text{Pic}^-]_{\text{NB},\text{t}}$ (see Materials and Methods). On the other hand, the $\log K_{\text{ex}2\pm}^{\text{s}}$ values calculated from the relation in Table 2 are very small, compared to those [8] reported before, although the order in magnitude of the calculated values is the same as that of the reported ones [8]. A correlation between these two orders was expressed by the following equation: $\log K_{\text{ex}2\pm}^{\text{s}}(\text{calcd}) = (1.54 \pm 0.05)\log K_{\text{ex}2\pm}^{\text{s}}(\text{found}) - (2.62 \pm 0.07)$ at $R = 0.998$. Also, differences between the $\log K_{\text{ex}2\pm}^{\text{s}}(\text{calcd})$ and $\log K_{\text{ex}2\pm}^{\text{s}}(\text{found})$ values

L	M	$\Delta\phi_{\text{eq}}/\text{V}^{\text{a}}$	$\log K_{\text{ex}\pm}^{\text{s}}$		$\log K_{\text{ex}2\pm}^{\text{s}}$	
			Found ^b	Calcd ^c	Found ^d	Calcd ^e
18C6	Ca	0.088	3.96	3.9 ₆	-0.5	-3.4 ₆
	Sr	0.061	5.89	5.9 ₃	1.6	-0.4 ₂
	Ba	0.044	6.61	6.8 ₉	2.4	1.2 ₁
B18C6	Ca	0.12	0.75	0.7 ₈	-2.3	-6.20
	Sr	0.082	2.95	2.9 ₉	-0.4	-3.1 ₄
	Ba	0.072	3.79	4.0 ₇	0.6	-1.5 ₆

^aEssentially based on $\Delta\phi/\text{V}$ versus $\text{Ph}_2\text{As}^+\text{BPh}_4^-$ electrode. ^bCalculated from the relation of $\log K_{\text{ex}\pm} = f(\phi_{\text{eq}} - \Delta\phi_{\text{ex}\pm}^{\text{or}})$ in Table 1. ^cCalculated from the relation of $\Delta\phi_{\text{ex}\pm}^{\text{or}} = 2(\Delta\phi_{\text{M}}^{\text{or}} - \Delta\phi_{\text{A}}^{\text{or}} + \Delta\phi_{\text{ML,org}}^{\text{or}}) + \Delta\phi_{1,\text{org}}^{\text{or}} + \Delta\phi_{\text{eq}}$ in Table 2. ^dCalculated from the thermodynamic cycle, $\log K_{\text{ex}2\pm}^{\text{s}} = \log K_{\text{D,M}}^{\text{s}} + 2\log K_{\text{D,Pic}}^{\text{s}} + \log K_{\text{ML,NB}}^{\text{s}}$. See ref. [8]. ^eCalculated from the relation of $\Delta\phi_{\text{ex}2\pm}^{\text{or}} = \Delta\phi_{\text{M}}^{\text{or}} - \Delta\phi_{\text{A}}^{\text{or}} + \Delta\phi_{\text{ML,org}}^{\text{or}} + \Delta\phi_{\text{eq}}$ in Table 2
Table 4: $\Delta\phi_{\text{eq}}$ and the $\log K_{\text{ex}\pm}$ and $\log K_{\text{ex}2\pm}$ values at 298 K standardized by their potentials.

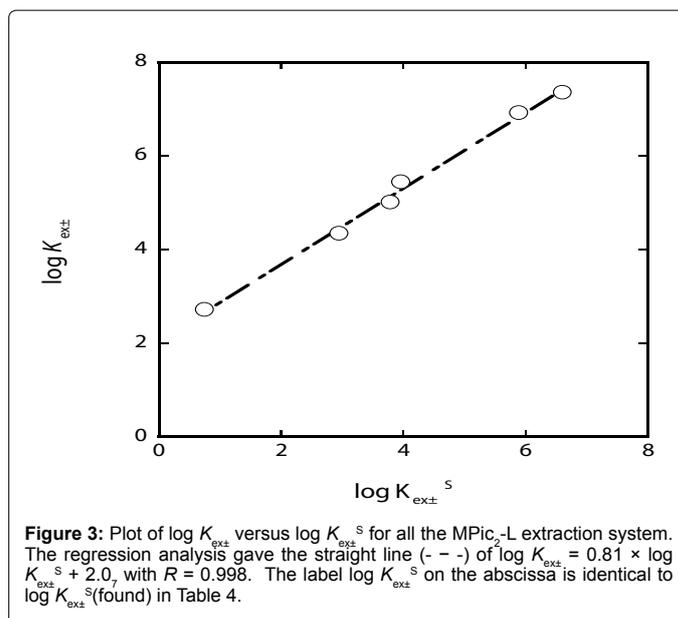


Figure 3: Plot of $\log K_{\text{ex}\pm}$ versus $\log K_{\text{ex}\pm}^{\text{s}}$ for all the MPic₂-L extraction system. The regression analysis gave the straight line (---) of $\log K_{\text{ex}\pm} = 0.81 \times \log K_{\text{ex}\pm}^{\text{s}} + 2.07$, with $R = 0.998$. The label $\log K_{\text{ex}\pm}^{\text{s}}$ on the abscissa is identical to $\log K_{\text{ex}\pm}^{\text{s}}(\text{found})$ in Table 4.

were in the range of 1.2 to 3.9 (Table 4). (i) These differences can be due to experimental errors of data, because estimated fractions, $[\text{ML}^{2+}]_{\text{NB}}/[\text{AAS-analyzed M(II)}]_{\text{NB}}$, were in the ranges of 0.001₂-0.043% for M = Ca, 0.02₄-0.33 for Sr and 0.0₅-3.1 for Ba. That is, these values indicate that the amounts of ML^{2+} in the NB phases are negligible, compared to those of all species with M(II) in the phases and accordingly the $K_{\text{ex}\pm}$ evaluations may cause the larger errors. (ii) Or the difference can come from the fact that the original extraction model does not take account of the overall process, $\text{M}^{2+} + \text{L}_{\text{NB}} + 2\text{Pic}^- \rightleftharpoons \text{ML}_{\text{NB}}^{2+} + 2\text{Pic}^-_{\text{NB}}$. While the overall process, $\text{M}^{2+} + \text{L}_{\text{NB}} + 2\text{Pic}^- \rightleftharpoons \text{MLPic}_{\text{NB}}^+ + \text{Pic}^-_{\text{NB}}$, has been included in the model [3-5] [see Equation (5a)]. However, it is unclear whether the two above facts, (i) and (ii), cause the negative errors of $\log K_{\text{ex}\pm}^{\text{s}}$ or not.

Figure 3 shows a plot of $\log K_{\text{ex}\pm}$ versus $\log K_{\text{ex}\pm}^{\text{s}}(\text{found})$ for all the MPic₂-L systems. Here, the former logarithmic values are listed in Table 3, while the latter values in Table 4. The plot gave a good correlation between both the values: $\log K_{\text{ex}\pm} = (0.81 \pm 0.03)\log K_{\text{ex}\pm}^{\text{s}}(\text{found}) + (2.0, \pm 0.1)$, at $R = 0.998$. This fact indicates that the experimental $\log K_{\text{ex}\pm}$ values clearly reflect the $\log K_{\text{ex}\pm}^{\text{s}}$ ones at $\Delta\phi_{\text{eq}} = 0$. The result is the same as that [1] reported before for the AgPic extraction by B15C5 and B18C6 into DCE or DCM. On the other hand, in this study, we were not able to obtain the $\log K_{\text{ex}2\pm}$ values which are comparable to the above $\log K_{\text{ex}\pm}$ ones.

Accordance of $\Delta\phi_{\text{eq}}$ with the distribution of ML^{2+} into NB

The individual distribution constants ($K_{\text{D,ML}}$) of ML^{2+} into the NB phase can be evaluated from the other thermodynamic cycle, $K_{\text{ex}\pm} = K_{\text{ML}}K_{\text{D,ML}}K_{1,\text{org}}(K_{\text{D,A}})^2/K_{\text{D,L}}$ (Table 2). Here, K_{ML} and $K_{\text{D,L}}$ (Table 1) are defined as $[\text{ML}^{2+}]/[\text{M}^{2+}][\text{L}]$ and $[\text{L}]_0/[\text{L}]$ [15], respectively, and these values at 298 K were available from references; $\log K_{\text{M18C6}} = 0.48$ for M = Ca, 2.72 for Sr and 3.87 for Ba [4]; $\log K_{\text{MB18C6}} = 0.48$ for M = Ca, 2.41 for Sr and 2.90 for Ba [21,22]; $\log K_{\text{D,L}} = -1.00$ [18] for L = 18C6 and 1.57 [20] for B18C6. Using the logarithmic form of the above equation, we obtained $\log K_{\text{D,M18C6}} = 0.8₈$ for M = Ca, $-0.1₇$ for Sr and $-0.9₉$ for Ba and $\log K_{\text{D,MB18C6}} = 2.6₃$ for M = Ca, $1.4₃$ for Sr and $1.6₁$ for Ba. There was a tendency that these values increase with an increase in the $\log K_{\text{D,ML}}^{\text{s}}$ ones: $\log K_{\text{D,ML}} = (1.6₁ \pm 0.5₀)\log K_{\text{D,ML}}^{\text{s}} + (3.6₇ \pm 0.9₂)$ at $R = 0.848$. Here, the $\log K_{\text{D,ML}}$ values [20] determined in terms of ion-transfer

polarography were employed as $\log K_{D,ML}^s$. Also, the $\Delta\phi_{eq}$ values can be easily evaluated from a modified form, $\log K_{D,ML}^s = 2(\Delta\phi_{eq}/0.05916) + \log K_{D,ML}^s$, of the relation in Table 1: $\Delta\phi_{eq} = 0.088$ V for the $CaPic_2$ -18C6 system, 0.06₀ for $SrPic_2$ -18C6, 0.04₇ for $BaPic_2$ -18C6, 0.1₂ for $CaPic_2$ -B18C6, 0.08₁ for $SrPic_2$ -B18C6 and 0.07₁ for $BaPic_2$ -B18C6 at 298 K. These $\Delta\phi_{eq}$ values were in good agreement with those listed in Table 4. This fact indicates that the expression of $K_{ex\pm}$ and $K_{D,Pic}$ by $\Delta\phi_{eq}$ in the $MPic_2$ extraction systems with L into NB does not conflict with the data [20] obtained from the electrochemical measurements. Additionally, the $\Delta\phi_{ex\pm}^0$ values calculated from the relation in Table 1 were well reproduced by the $\Delta\phi$ -relation (b) in Table 2.

Conclusion

Expressions of the extraction constants by $\Delta\phi_{eq}$ were extended into $K_{ex\pm}$, $K_{ex2\pm}$ and K_{ex} of the $M^{II}Pic_2$ extraction systems with L, in addition to $K_{ex\pm}$ and K_{ex} of the $AgPic$ -L systems [1]. These expressions were summarized in Tables 1 and 2. However, the matters for precision of the values in the analyses have been present for the determination of $K_{ex2\pm}^s$. Also, there may be self-inconsistency for the estimation of the $K_{n,NB}$ values. It was demonstrated that the $\log K_{ex\pm}$ values well reflect the $\log K_{ex\pm}^s$ ones. So, one can see markedly the relation between $K_{ex\pm}$ obtained from an extraction experiment and $K_{ex\pm}^s$ from an electrochemical one. This result fundamentally enables us to discuss the extraction-ability and -selectivity of L against M^{2+} from both the values. Moreover, it was shown that the expressions of $K_{ex\pm}$, $K_{D,ML}$ and $K_{D,Pic}$ by $\Delta\phi_{eq}$ do not conflict with data obtained from the electrochemical measurements.

Acknowledgement

The authors thank Mr. Shinichi Nakajima for his experimental assistance in the K_{MPic} determination.

Appendix

In practice, we have calculated the values of

$$\log K_{ex\pm} - \log K_{ex2\pm}^s = f(\Delta\phi_{eq} - \Delta\phi_{ex\pm}^0) - \log K_{ex2\pm}^s \quad (A1)$$

from Equation (6) and the relation in Table 1. Rearranging this equation, the following equation can be easily obtained

$$\log K_{ex\pm} - \log K_{ex2\pm}^s = \log K_{ex\pm}^s - \log K_{ex2\pm}^s + f\Delta\phi_{eq} \quad (A2)$$

Also, Equation (7) gave

$$\begin{aligned} \log K_{ex} - \log K_{ex\pm} &= \log K_{ex}^s - \log K_{ex\pm} = \log K_{ex}^s - f(\Delta\phi_{eq} - \Delta\phi_{ex\pm}^0) \\ &= \log K_{ex}^s - \log K_{ex\pm}^s - f\Delta\phi_{eq} \quad (A3) \end{aligned}$$

$\log K_{1,NB}$ and $\log K_{2,NB}$ in Table 3 are equal to Equations (A2) and (A3), respectively. As examples, the $\log K_{1,NB}$ and $\log K_{2,NB}$ values for the $SrPic_2$ -B18C6 system were calculated from these equations to be 4.7₃ and 5.0₇, respectively. These values were in good accord with those listed in Table 3.

Why do Equations (A2) and (A3), the functions expressing $\log K_{1,NB}$ and $\log K_{2,NB}$, contain $\Delta\phi_{eq}$? This question comes from the fact that $\log K_{n,NB}$ ($n = 1, 2$) in Table 1 were derived from the condition of $\Delta\phi_{eq} = 0$ V. Also, the above results are self-consistent to the fact that all the $\log K_{n,NB}$ values in Table 3 are conditional equilibrium-constants, such as $K_{n,NB}$ fixed in an I_{NB} value. Unfortunately, the authors cannot now explain these inconsistencies.

References

- Kudo Y, Ojihara M, Katsuta S, Takeda Y (2014) An electrochemical understanding of extraction of silver picrate by benzo-3m-crown-m ethers ($m = 5, 6$) into 1,2-dichloroethane and dichloromethane. *American Journal of Analytical Chemistry* 5: 433-444.
- Kudo Y, Harashima K, Katsuta S, Takeda Y (2011) Solvent extraction of sodium permanganate by mono-benzo-3m-crown-m ethers ($m = 5, 6$) into 1,2-dichloroethane and nitrobenzene: a method which analyzes the extraction system with the polar diluents. *International Journal of Chemistry* 3: 99-107.
- Kudo Y, Horiuchi N, Katsuta S, Takeda Y (2013) Extraction of cadmium bromide and picrate by 18-crown-6 ether into various less-polar diluents: analysis of overall extraction equilibria based on their component equilibria with formation of their ion pairs in water. *Journal of Molecular Liquids* 177: 257-266.
- Kudo Y, Takahashi Y, Katsuta S, Takeda Y (2013) Extraction of several divalent metal picrates by 18-crown-6 ether derivatives into benzene: a refinement of methods for analyzing extraction equilibria. *International Journal of Chemistry* 5: 90-102.
- Kudo Y, Takahashi Y, Numako C, Katsuta S (2014) Extraction of lead picrate by 18-crown-6 ether into various diluents: examples of sub-analysis of overall extraction equilibrium based on component equilibria. *Journal of Molecular Liquids* 194: 121-129.
- Kudo Y, Harashima K, Hiyoshi K, Takagi J, Katsuta S, et al. (2011) Extraction of some univalent salts into 1,2-dichloroethane and nitrobenzene: analysis of overall extraction equilibrium based on elucidating ion-pair formation and evaluation of standard potentials for ion transfers at the interfaces between their diluents and water. See comment in PubMed Commons below *Anal Sci* 27: 913-919.
- Markin VS, Volkov AG (1989) The Gibbs free energy of ion transfer between two immiscible liquids. *Electrochimica Acta* 34: 93-107.
- Kudo Y, Katsuta S, Takeda Y (2012) Evaluation of overall extraction constants for the crown ether-complex ions of alkali and alkaline-earth metal with counter picrate ions from water into nitrobenzene based on their component equilibrium constants. *Journal of Molecular Liquids* 173: 66-70.
- Bard AJ, Faulkner LR (2001) *Electrochemical Method: Fundamentals and Applications* (Edn 2), John Wiley & Sons, New York, pp. 60-62
- Guggenheim EA (1928) The conceptions of electrical potential difference between two phases and individual activities of ions. *Journal of Physical Chemistry* 33: 842-849.
- Takeda Y, Ezaki T, Kudo Y, Matsuda H (1995) Distribution study on electroneutral and protonated amino acids between water and nitrobenzene. Determination of the standard ion-transfer potentials of protonated amino acids. *Bulletin of the Chemical Society of Japan* 68: 787-790.
- Kudo Y, Takeuchi S, Kobayashi Y, Katsuta S, Takeda Y (2007) Potentiometric determination of ion-pair formation constants for cadmium, calcium salts, and cadmium-18-crown-6 ether derivative complexes with a sulfate ion in water. *Journal of Chemical and Engineering Data* 52: 1747-1752.
- Ohkouchi T, Kakutani T, Senda M (1991) Electrochemical study of the transfer of uncouplers across the organic/aqueous interface. *Biochemistry and Bioenergetics* 25: 71-80.
- Shannon RD (1976) Revised effective ionic radii and systematic studies of interatomic distances in halides and chalcogenides. *Acta Crystallographica A* 32: 751-767.
- Takeda Y (2002) Extraction of alkali metal picrates with 18-crown-6, benzo-18-crown-6, and dibenzo-18-crown-6 into various organic solvents. Elucidation of fundamental equilibria governing the extraction-ability and -selectivity. *Bunseki Kagaku (Analytical Chemistry)* 51: 515-525.
- Osakai T, Ebina K (1998) Non-Bornian theory of the Gibbs energy of ion transfer between two immiscible liquids. *Journal of Physical Chemistry B* 102: 5691-5698.
- Iwachido T, Minami M, Kimura M, Sadakane A, Kawasaki M, Tōei K (1980) The coextraction of water into nitrobenzene with alkali and alkaline-earth metal salts of 2,2',4,4',6,6'-hexanitrodiphenylamine in the presence of several crown ethers and cryptands. *Bulletin of the Chemical Society of Japan* 53: 703-708.
- Iwachido T, Minami M, Sadakane A, Tōei K (1977) The coextraction of water into nitrobenzene with alkaline-earth metal 2,2',4,4',6,6'-hexanitrodiphenylaminates in the presence of crown ethers. *Chemistry Letters* 1977: 1511-1514.
- Marecek V, Samec Z (1983) Determination of calcium, barium and strontium ions by differential pulse stripping voltammetry at a hanging electrolyte drop electrode. *Analytica Chimica Acta* 151: 265-269.
- Kudo Y, Miyakawa T, Takeda Y, Matsuda H (1996) Ion-transfer polarographic study of the distribution of alkali and alkaline-earth metal complexes with 3m-crown-m ether derivatives ($m = 6, 8$) between water and nitrobenzene phases. *Journal of Inclusion Phenomena and Molecular Recognition in Chemistry* 26: 331-341.
- Takeda Y, Kohno R, Kudo Y, Fukada N (1989) Stabilities in water and transfer activity coefficients from water to nonaqueous solvents of benzo-18-crown-6-metal ion complexes. *Bulletin of the Chemical Society of Japan* 62: 999-1003.
- Takeda Y, Nishida M (1989) Solvent extraction of various metal picrates with benzo-18-crown-6 into $CHCl_3$. *Bulletin of the Chemical Society of Japan* 62: 1468-1471.