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# Growth and Yield Models for Uneven-Aged Secondary Forest in IITA, Ibadan, Nigeria

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#### Abstract

The development of effective and accurate models to predict forest growth and products is essential for forest managers and planners. Decision-makers need information on the present yield of the forest for the purpose of monitoring growth. Despite the importance of growth and yield models in the determination of appropriate forest management strategies, no study has been undertaken in IITA's Forest Reserve. Volume equations for predicting tree volume were developed for tree species in IITA's Forest Reserve.

Complete enumeration of trees larger than 5 cm was carried out in fifteen permanent sample plots of size 20 m × 20 m. The data assessed were diameter at base, diameter at middle, diameter at top, diameter at breast height and total height for 1214 tree species. All trees encountered in each plot were identified with their botanical names.

The results revealed that there were 34 important tree species distributed among 23 families in the reserve. The most abundant tree species is Newbouldia laevis while the family with the highest number of species is Moraceae with six species. The number of observations per species ranged from 1 to 255 while the diameter at breast height ranged from 5.00 cm to 201.20 cm and highest percentage of the trees belong to the least diameter class (5-9 cm). The volume equations were fitted for individual species greater than or equal to five and all species combined. The assessment criteria coefficient of determination ( $R^2$ ), Standard error of estimate (SEE) with the validation results (using simple linear regression equation, percentage bias and probability plots of residuals) show that the model of logarithm transformed diameter at base and logarithm transformed total height was of good fit. Very high  $R^2$  values, small SEE and percentage biases were obtained. The model was discovered to be very adequate for tree volume estimation in the study area.

It is therefore recommended for further use in this ecosystem and in any other forest ecosystem with similar site condition.

**Keywords:** Ecosystem; Volume model; Forest inventory; Residual plots; Species

## Introduction

#### General background

Vanclay [1] defined stand growth models as abstractions of the natural dynamics of a forest stand, which may encompasses growth, mortality and other changes in stand composition and structure. Therefore Forest models can be used as very successful research and management tools. The models designed for research require many complicated and not readily available data, whereas the models designed for management use simpler and more readily accessible data [2]. Growth can be generally defined as the increase in dimensions of an organism or its fraction (forest-forest, stand-individual tree etc.) over time, whereas increment is regarded as the rate of change within a specific period of time [3].

The development of effective and accurate models to predict forest growth and products is essential for forest managers and planners. Growth and yield models, which rely on functions to measurement data from a sample of the forest population of interest, are the tools that have mainly been used to provide decision-support information that meets basic operational needs for evaluating various forest management scenarios [4]. Need for specific information for forest managers and planners are one of the reasons for the increase of the demand for forest models. Growth and yield modeling are very useful tools for managing forest properties either large or small. They are used for operational and strategic planning in nations that own and manage forest lands. Modeling is also good for decision making regarding buying, selling, and trading in forest resources.

Inventories taken at one instant in time provide information on current wood volumes and related statistics [5]. The allometric relationship between tree diameter and total tree height is commonly used to estimate tree volume and thus is a fundamental component of many growth and yield, functional, and forest planning models [6].

IITA Forest Reserve is gradually becoming an endangered ecosystem due to regular poaching activities and exploitation of timber. This ecosystem is an important ecological resource providing many functions and values such as wildlife habitat, water quality protection, biodiversity, timber production and contributes to carbon sequestration. Decision-makers need information on species and biotic type distribution patterns and the effective use of available technology and data at multiple scales of resolution is highly essential. Unfortunately, these information and data is rare [7].

Despite the importance of growth and yield models in the determination of appropriate forest management strategies, relatively few studies have been undertaken on tropical forests. This may be attributed to the existence of multi-species forests with different ages and a wide range of growth habits and stem sizes that pose special challenges to growth modelers. In Africa, only a few growth models have been developed for tree species. The main objective of this research is to develop growth and yield models to predict the growth and yield of a secondary forest in IITA.

## Methodology

#### The study area

This study was carried out in International Institute of Tropical Agriculture (IITA) forest reserve, it lies on Latitude 07°30'N and longitude 03°55'E at altitude 227 m above sea level in the city of Ibadan, Oyo State. The 350 hectares IITA Forest Reserve has been protected since 1965. The rainfall pattern is bimodal, the mean annual rainfall is about 1301.6 mm most of which falls between May and September. The average daily temperature ranges between 21°C and 23°C while the maximum is between 28°C and 34°C. Mean relative humidity is in the range of 64% to 83% (Figures 1-5).



Figure 1: Map of International Institute of Tropical Agriculture Nigeria.

#### Data collection

Diameter at breast height (dbh) and total height measurements had been carried out on 15 permanent sample plots (PSP) in the following years: 1975, 2005, 2008 and 2010. Two sets of data on the permanent sample plots (PSP) were used for this study. These are 2008 and 2013 data set. The 2013 data collection was the primary while the 2008 secondary, obtained from the International Institute of Tropical Agriculture (IITA). Complete enumeration of trees larger than 5 cm was carried out in the already demarcated 15 plots of size 20 m  $\times$  20 m. Within each plot, the following tree growth variables were measured: Total height, merchantable height, clear bole height, Diameter at breast height (Dbh), Diameter at the base, middle and top, Crown length and diameter.

#### Measurement of tree growth variables

**Crown diameter:** Crown measurements were based on the assumption that the vertical projection of a tree crown is circular [8]. Four radii were measured as in Ayhan [9] along four axes at right angle. Along the widest part of the tree crown the tape was held horizontally and extended until each person is vertically under the tip of the longest branch on their side. Measurement was recorded as maximum width. The tape was then turned by 90° and measurement repeated along the thinnest part of the tree crown and recorded as minimum width.

Average crown diameter (Cd) was calculated by summing up the four radii and dividing by 2, thus:

$$Cd = \frac{\sum r_i}{2} (1)$$

Where;

Cd=average crown diameter

r<sub>i</sub>=projected crown radii measured on four axes.

**Bole diameter**: Diameter at breast height (dbh) was measured for all tree individuals by means of a diameter tape. For trees with deformations at 1.3 m, the measurement was made at the sound point on the stem above the abnormality. For buttressed trees, a point of measurement was selected approximately 0.5 m above the convergence of the buttress [10]. Diameter at the top and middle was measured using a spiegel relaskop.

**Tree height:** Spiegel relaskop was used to measure total height, merchantable height, bole height and crown length.

#### Data analysis

The data collected from tree measurement was processed into suitable form for statistical analysis. Data processing included basal area estimation, stem volume, crown projection area estimation and tree slenderness estimation.

**Basal area estimation:** The diameter at breast height (dbh) was used to compute basal area using the given formula

$$BA = \pi H \left[ \frac{Db^2 + 4Dm^2 + Dt^2}{24} \right] (2)$$

Where BA=Basal area (m²), Diameter at breast height (m) and  $\pi{=}3.142$ 

**Volume estimation:** Volume of each tree was estimated using Newton's formula as described in Husch et al. [10]

$$V = \pi H \left[ \frac{Db^2 + 4Dm^2 + Dt^2}{24} \right] (3)$$

Where V=Stem volume (m<sup>3</sup>), H=height (m),  $D_b$ =Diameter at the base,  $D_m$ =Diameter at the middle,  $D_t$ =Diameter at the top and  $\pi$ =3.142

Crown ratio (CR) estimation: Crown ratio was estimated using the formula;

$$CR = \frac{CL}{THT} (4)$$

Where THT=Total height and CL=Crown length

**Crown projection area estimation:** The crown projection area for each tree was estimated using the formula:

$$CPA = \frac{(\pi CD^2)}{4} (5)$$

Where, CPA=Crown projection area  $(m^2)$  and CD=Crown diameter (m)

**Slenderness coefficient (SLC) estimation:** Tree slenderness coefficient was estimated using the formula:

$$SLC = \frac{THT}{dbh} (6)$$

Where, SLC=Tree slenderness coefficient, THT=Total height and dbh=Diameter at breast height

## Yield model generation

Volume model developed by Schumacher and Hall [11]; Clutter et al. [12]; Laar and Akca [13] was used for modelling process in this study. However, several forms of this model, using height with the introduction of other variable was considered. This is because height is the major determinant variable if stem volume of tree is considered [11]. In its original form, the model is expressed as:

 $V = b_0 D b_1 H b_2 (7)$ 

Where, V=tree volume (m<sup>3</sup>); D=diameter at breast height (cm); H=total tree height (m);  $b_0$ ,  $b_1$  and  $b_2$  are the regression parameters.

Linear, logarithm transformed, quadratic and polynomial forms of regression yield models was adopted. Most equations were directly obtained from the available literature. Some models were modified specifically for the study.

## Simple linear regression model

 $v=b_0+b_1D$  (8)  $v=b_0+b_1DH$  (9)  $v=b_0+b_1CD$  (10)

## Multiple linear regression models

 $v=b_0+b_1D+b_2H$  (11)

 $v=b_0+b_1 D_m+b_2 H$  (12)

 $v = b_0 + b_1 D_t + b_2 H$  (13)

 $v = b_0 + b_1 D_b + b_2 H$  (14)

 $v=b_0+b_1 D+b_2CL$ (15) $v=b_0+b_1 BA+b_2H$ (16)Logarithm transformed models lnv=b0+b1lnD (17)lnv=b<sub>0</sub>+b<sub>1</sub>lnCD (18) $\ln v = b_0 + b_1 \ln D_2$ (19) $\ln v = b_0 + b_1 \ln DH$ (20) $lnv=b_0+b_1 lnD_2H$ (21) $\ln v = b_0 + b_1 \ln D_2 + b_2 \ln H$  (22)  $\ln v = b_0 + b_1 \ln D + b_2 \ln H$  (23)  $\ln v = b_0 + b_1 \ln D_b + b_2 \ln H$  (24)  $\ln v = b_0 + b_1 \ln D_m + b_2 \ln H$  (25)  $lnv=b_0+b_1 lnD_t+b_2 lnH$  (26)  $\ln v = b_0 + b_1 \ln BA + b_2 \ln H$  (27)  $\ln v = b_0 + b_1 \ln D + b_2 \ln CL$  (28)  $lnv=b_0+b_1 lnD_2+b_2 lnH_2$  (29) Quadratic model  $v = b_0 + b_1 D_2$ (30)

 $v=b_{0}+b_{1}D_{2}H$  (31)  $v=b_{0}+b_{1}D_{2}+b_{2}H$  (32)  $v=b_{0}+b_{1}D_{2}+b_{2}H_{2}$  (33)

## Polynomial models

$$\begin{split} &v\!=\!b_0\!+\!b_1D_2\!+\!b_2H\!+\!b_3D_2H~(34)\\ &v\!=\!b_0\!+\!b_1D\!+\!b_2H\!+\!b_3D_2\!+\!b_4H_2~(35)\\ &v\!=\!b_0\!+\!b_1D\!+\!b_2D_2\!+\!b_3DH\!+\!b_4D_2H~(36)\\ &v\!=\!b_0\!+\!b_1D_2\!+\!b_2H_2\!+\!b_3D_2H\!+\!b_4DH_2~(37) \end{split}$$

Where v=volume (m<sup>3</sup>), H=Total height (m), ln=natural log, D=Diameter at breast height (D<sub>bh</sub>) (m), C<sub>L</sub>=Crown length (m), C<sub>D</sub>=Crown diameter (m), D<sub>b</sub>=Diameter at the base (m), D<sub>m</sub>=Diameter at the middle (m), D<sub>t</sub>=Diameter at the top (m), b<sub>0</sub>=regression constant (intercept), b<sub>1</sub>, b<sub>2</sub>, b<sub>3</sub> and b<sub>4</sub>=regression coefficients

Volume equations for individual species: In developing volume equations for each of the 34 tree species in this study several model forms were considered and tried for the various species. It was clear that the best model for each species vary in form. The combined variable equation of Spurr [14] and the logarithmic of Schumacher and Hall [11] are classic volume models commonly used, often without question, when developing stem volume equations [15]. The generalized logarithmic model form, which in its original form was the Schumacher-Hall volume model [11], has been used in several studies. The model indicates that tree volume increases proportional to certain powers of D and H. In some previous works [16-18] the D was fixed to the power of 2 while H was fixed to the power of 1 to give the expression;

 $V=b_0+b1D^2H+E_i$  (38)

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Clutter et al. [12] referred to as the 'combined variable' volume function. Model Equation 6 above and the following models were fitted to the data;

$$\begin{split} & SV = b_0 + b_1 D^2 H \quad (39) \\ & SV = b_0 + b_1 D H \quad (40) \\ & SV = b_0 + b_1 D^2 + b_2 H \ (41) \\ & SV = b_0 + b_1 D^2 + b_2 H^2 \ (42) \end{split}$$

Where; SV=stem volume, D=Diameter at breast height and H=total height

#### Assessment of the models

The volume models were assessed with the view of recommending those with good fit for further uses. The following statistical criteria were used:

**Significance of regression (F-ratio):** This is to test the overall significance of the regression equations. The critical value of F (i.e., F-tabulated) at p<0.05 level of significance was compared with the F-ratio (F-calculated). Where the variance ratio (F-calculated) is greater than the critical values (F-tabulated) such equation is therefore significant and can be accepted for prediction.

**Coefficient of determination (R<sup>2</sup>):** This is the measure of the proportion of variation in the dependent variable that is explained by the behavior of the independent variable [19]. For the model to be accepted, the  $R^2$  value must be high (>50%).

**Regression Mean Square Error (RMSE):** This is also referred to as the standard deviation or residual of the error variance of the estimate. It measures the spread of data and is a good indicator of precision. The value must be small.

$$RMSE = \sqrt{\frac{\sum \left(Y_i - Y\right)^2}{n - p}} (43)$$

Note: Y<sub>i</sub>=observed value of the dependent variable

Y=predicted value of the dependent variable

n=number of observations

p=number of parameters

#### Validation of the models

It is highly essential to validate the models selected after assessment before their suitability can be introduced to forest resource management. Validation was done by comparing the models' output with values observed on the field. This, according to VanHorn [20] is to build an acceptable level of confidence that any inference about the simulated process is correct or valid about the actual process. The validation process also examines the usefulness or validity of the models [21]. The first set (calibrating set) and the second the validation set. The calibrating set is used to construct the models while the validation set is used to test them [22].

All field data were divided into two sets. The first set (calibrating set), comprised growth variables from 971 trees (80%). These were used for generating the models (total volume models) when all species were pooled. The second set (validating set) comprised tree data from 243 trees (20%). These were used for validating the models [23]. For selected species, especially those with few trees, all data were used for

calibrating and validating. This was to ensure adequate data to represent different tree growth form and size within a species. Model outputs were individually compared with observed values using the Student t-test for paired means [24] and the simple linear regression equation [25]. In adopting the simple linear regression equation, the observed volume was the dependent variable while the model output was the independent variable.

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For models with good fit, there should be no significant difference between the means of the observed and predicted volumes. For the simple linear regression equation, the intercept must approach 0 and the slope approach 1, and the model must be significant (p<0.05 or very high f-ratio value). There must be high correlation between the observed and predicted values, and the coefficient of determination values must also be very high (near 100%) and the standard error of estimates must be small [25-27]. To verify that the residuals are normally distributed and not over or under estimated, residual plots were obtained for all allometric equations by plotting residual values against the independent variate i.e., the predicted volume [28]. While there is many assumptions in the models, the essential multiple leastsquare regression assumptions are that the residuals should have normal distribution with zero mean and constant variance of the residuals.

The student t-test: This was used to test for any significant difference between the actual values or field values and the predicted values (model output) of the various models generated according to Goulding [29,30]

$$t = \frac{\bar{X}_1 - \bar{X}_2}{S_{X1_X2} \cdot \sqrt{\frac{2}{n}}} \,(44)$$

and,

$$S_{X_1X_2} = \sqrt{\frac{1}{2}} (S_{X_1}^2 + S_{X_2}^2)$$
(45)

Where:

$$\bar{X}$$
=Means for predicted and observed data respectively $S_{X_1X_2}$ 

=Pooled standard deviation

This is also expected to should show no significant difference in any of the species-size class at 5% level of significance.

**Percentage bias estimation:** The absolute percentage difference (% bias) was determined by dividing the difference between volumes obtained with Newton's formula (observed volume) and models output by the same observed volume and multiplied by 100.

% bias= $(V_0/V_p) \times 10046$ 

Where:

V<sub>0</sub>=The observe volume

Vp=The predicted volume (models output)

The value must be relatively small for the model to be acceptable for management purpose.

## **Results and Discussion**

## Data summary

The entire data set used for this study consists of 34 species in IITA forest reserve as indicated in Table 1. In terms of their taxonomy, these species belong to 23 different families as indicated in Table 2.

S No	Code	Species	Family	Freq.	% Abundance
1	AL	Albizia lebbeck	Fabaceae	1	0.082
2	AZ	Albizia zygia	Fabaceae -Mimosoideae	11	0.906
3	AC	Alchornea cordifolia	Euphorbiaceae	2	0.165
4	ALX	Alchornea laxiflora	Euphorbiaceae	6	0.494
5	AA	Antiaris africana	Moraceae	59	4.86
6	BN	Barteria nigritiana	Passifloraceae	1	0.082
7	BS	Blighia sapida	Sapindaceae	185	15.239
8	вв	Bombax buonopozense	Bombacaceae	2	0.165
9	CA	Celtis africana	Cannabaceae	31	2.554
10	CZ	Celtis zenkeri	Ulmaceae	3	0.247
11	CA	Chrysophyllum albidum	Sapotaceae	87	7.166
12	CN	Cola nitida	Sterculiaceae	4	0.329
13	DG	Dialium guineense	Fabaceae - Caesalpinioideae	17	1.4
14	DC	Diospyros crassiflora	Ebenaceae	1	0.082
15	FE	Ficus exasperata	Moraceae	104	8.567
16	FM	Ficus mucuso	Moraceae	2	0.165
17	FU	Funtumia elastica	Apocynaceae	191	15.733
18	GA	Gmelina arborea	Verbenaceae	1	0.082
19	HF	Holarrhena floribunda	Apocynaceae	7	0.577
20	LC	Lecaniodiscus cupanioides	Sapindaceae	57	4.695
21	LS	Lonchocarpus sericeus	Fabaceae -Papilionoideae	1	0.082
22	ME	Milicia excelsa	Moraceae	1	0.082
23	MT	Millettia thonningii	Fabaceae - Papilionoideae	4	0.329
24	МІ	Mitragyna inermis	Rubiaceae	3	0.247
25	ММ	Morus mesozygia	Moraceae	20	1.647
26	NI	Napoleonaea imperialis	Lecythidaceae	3	0.247
27	ND	Nauclea diderrichii	Rubiaceae	64	5.272
28	NL	Newbouldia laevis	Bignoniaceae	255	21.005
29	PA	Pycnanthus angolensis	Myristicaceae	13	1.071
30	SM	Spondias mombin	Anacardiacae	29	2.389
31	SG	Syzgium guineense	Myrtaceae	1	0.082

32	ТМ	Trichila monadelpha	Meliaceae	29	2.389
33	ТА	Trilepisium madagascariense	Moraceae	16	1.318
34	TS	Triplochiton scleroxylon	Sterculiaceae	3	0.247
		Total		1214	100

Table 1: Data distribution according to species.

A summary of the pooled data for the all species showing number of observations, mean and standard error for each variable is presented in Table 3.

S No.	Family	No. of Species	No. of Observations	%
1	Anacardiacae	1	29	2.39
2	Apocynaceae	2	198	16.31
3	Bignoniaceae	1	255	21.00
4	Bombacaceae	1	2	0.16
5	Cannabaceae	1	31	2.55
6	Ebenaceae	1	1	0.08
7	Euphorbiaceae	2	8	0.66
8	Fabaceae	1	1	0.08
9	Fabaceae - Caesalpinioideae	1	17	1.40
10	Fabaceae -Mimosoideae	1	11	0.91
11	Fabaceae-Papilionoideae	2	5	0.41
12	Lecythidaceae	1	3	0.25
13	Meliaceae	1	29	2.39
14	Moraceae	6	202	16.64
15	Myristicaceae	1	13	1.07
16	Myrtaceae	1	1	0.08
17	Passifloraceae	1	1	0.08
18	Rubiaceae	2	67	5.52
19	Sapindaceae	2	242	19.93
20	Sapotaceae	1	87	7.17
21	Sterculiaceae	2	7	0.58
22	Ulmaceae	1	3	0.25
23	Verbenaceae	1	1	0.08
	Total	34	1214	100

Table 2: Data distribution according to family.

The number of observations per species was generally low, with only eleven species having frequencies above 20. *Newbouldia laevis* (255)

has the highest frequency, next to which are *Funtumia elastica* (191), *Blighia sapida* (185), *Ficus exasperata* (104), *Chrysophyllum albidum* (87), *Nauclea diderrichii* (64), *Antiaris africana* (59), *Lecaniodiscus cupanioides* (57), *Celtis africana* (31), *Spondias mombin* (29), and *Trichila monadelpha* (29).

The family with the highest number of species is Moraceae (6 species). This is followed by Apocynaceae, Euphorbiaceae, Fabaceae-Papilionoideae, Rubiaceae, Sapindaceae and Sterculiaceae with two species each. The family, Fabaceae, is a large family with three sub-families namely Caesalpiniodeae, Mimosoideae and Papilionoideae. The number of species in these sub-families is 1, 1 and 2, respectively.

#### **Growth variables**

The result of the descriptive statistics of data collected on growth variables for the species are given in Table 3. The table shows the mean, standard error, standard deviation, co-efficient of variation, minimum, maximum, kurtosis and skewness values of each growth variable.

Variables	Mean	S.E	S.D	c.v	Min.	Max.	Kurtosi s	Skewnes s
тнт	6.7	0.1	3.65	0.54	1.6	31.2	4.22	1.53
CD	3.18	0.06	1.93	0.61	0.25	19.01	8.55	1.93
DBH	25.25	0.62	21.56	0.85	5	201.2	13.63	2.8
DB	39.23	1.03	35.99	0.92	8	491	42.3	4.91
DM	13.6	0.36	12.62	0.93	2.8	124.1	16.9	3.11
DT	6.23	0.17	5.91	0.95	1.6	62	18.81	3.23
CL	1.91	0.03	1.13	0.59	0.2	7	1.52	1.17
ВА	0.09	0.01	0.21	2.46	0	3.18	94.68	8.51
CR	0.28	0	0.04	0.16	0.06	0.62	5.74	-0.61
SLC	33.21	0.39	13.68	0.41	5.74	131.37	3.87	1.23
СРА	10.89	0.49	17.11	1.57	0.05	283.86	98.71	7.76
VOL	0.77	0.14	4.97	6.45	0.003	117.26	350.15	17.48

**Table 3:** Descriptive statistics for the tree species (2013). THT=Total height (m), CD=Crown diameter (m), DBH=Diameter at breast height (m), DB=Diameter at base (m), DM=Diameter at middle (m), DT=Diameter at top (m), CL=Crown length (m), BA=Basal area (m<sup>2</sup>), CR=Crown ratio, SLC=Tree slenderness coefficient, CPA=Crown projection area (m<sup>2</sup>) and VOL=Volume (m<sup>3</sup>)

#### Diameter and height distribution

Tables 4 and 5 shows the mean, minimum, maximum, standard error and standard deviation values of diameter at breast height in the PSP from 2008 to the year 2013. There has been a decline in the total number of stems in the PSP over the years, which is probably as a result of illegal exploitation hence recruitment of young trees.

Year	Min. Dbh	Max. Dbh	S.E	S.D	Stem density
2008	10.00	456.00	1.31	39.12	893
2013	5.00	201.20	0.62	21.56	1214

Table 4: Diameter summary statistics from 2008 to 2013.

Status	5-9	10-14	15-19	20-24	25-29	30-34	35-39	40-44	45-49	>50	Stem density
live trees (2008)	-	86	115	106	101	105	63	60	36	221	893
live trees (2013)	285	231	128	99	89	95	69	48	45	125	1214

Table 5: Life table for the pooled species (2008-2013).

**Diameter size class distribution in the PSP year 2013:** The distribution of the trees in the Year 2008 and 2013 of the study area into height classes is presented in the Tables 6 and 7 about 94.1% of the measured trees in the Year 2008 fall into the height class (0.1-10 m). This constitutes the largest percentage of the trees in the Year 2008. This was followed by the second height class (10.1-20 m), which had about 3.8%. In the Year 2013 only 0.4% of the trees are in the height class of 20.1-30 m.

Height (m)	2008		2013		
	Frequency	Percentage	Frequency	Percentage	
0.1-10	840	94.06	1003	82.62	
10.1-20	34	3.81	205	16.89	
20.1- 30	16	1.79	5	0.41	
>30	3	0.34	1	0.08	
Total	893	100	1214	100	

**Table 6:** Distribution of the trees into height classes.

#### Distribution of growth variables

Slenderness coefficient (SLC) greatly determines the ability of the tree to withstand wind throw. The slenderness coefficient values obtained from the analysis were classified into three categories as suggested by Navratil et al. [31]:

SLC values>99=High slenderness coefficient

70 to 99=Moderate slenderness coefficient

SLC<70=Low slenderness coefficient

SLC-class	Frequency	%
< 70	1200	98.85
70-99	11	0.91
>99	3	0.25
Total	1214	100

 Table 7: Slenderness class distribution.

Slenderness values usually fall within the range 50-150; slenderness values below 70 are generally an indicator of adequate individual tree stability, 1200 trees have slenderness values of less than 70 which indicate adequate tree stability and 3 trees have high slenderness coefficient. The height of trees in relation to their breast height diameter, their slenderness ratio, seems to be one of the single most important factors determining stem deflection and strength of the tree to resist wind [32]. Trees with a higher slenderness ratio are at risk of firstly being bent sideways by wind then being pulled down by the weight of their crown. Petty and Swain [33] found that slenderness ratio (taper) is probably the most important factor affecting susceptibility to wind breakage with trees of low taper (high slenderness ratio) being much more susceptible to damage. Slenderness values of less than 70 generally produced stability while values of approximately 100 produce instability.

In different studies on the resistance of trees and stands to the action of wind stability of trees is defined by the slenderness factor [34-36]. It is considered as an adequate measure for the determination of stability of trees and their resistance to the action of wind [35,36]. At the same time it needs to be stressed that less regular stands are more stable and thus more resistant to the action of wind than forest monocultures [37].

CR-class	Frequency	%
0.0-0.3	1206	99.34
0.4-0.5	7	0.58
>0.5	1	0.08
Total	1214	100

Table 8: Crown ratio class distribution.

Crown ratio (CR) is a common indicator of tree vigor [38,39] and is a very useful parameter in forest health assessment used to predict growth and yield of trees and forests. Crown ratio, also as an indirect measure of a tree's photosynthetic capacity and a measure of stand density, is used as a predictor variable in many existing forest growth and yield models [40,41]. It is also a good indicator of competition and survival potential [42]. It is used as an indicator of wood quality [43], wind firmness [44] and stand density [12].

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Table 8 shows that a high proportion of the trees in IITA Forest Reserve have low vigour, this depicts that those with low vigour have small crown length and just one of the trees have high vigour.

Crown Diameter class	Freq.	%
0.10-3	649	53.46
3.10-6	482	39.70
6.10-9	69	5.68
9.10-12	9	0.74
12.10-15	3	0.25
>15	2	0.16
Total	1214	100

The size of a tree crown has marked effect on, and is strongly correlated with the growth of the tree and its various parts. It is an indicator of tree vigor. Table 9 shows higher proportions of the trees are in the 0.10-3 size class. The base of live crown varies greatly between and within species, and is usually influenced by growing space, competition, site quality, extent of self-pruning by individual trees, and other factors.

Estimates of crown width can also be used to calculate stand canopy closure, which is important for assessing wildlife habitat suitability, fire risk, and understory light conditions for regeneration [45]. Consequently, quantification of crown width attributes is an important component of many forest growth and yield models.

## Correlation coefficient of the various growth parameters

There is generally more positive linear relationship between the variables. The highest correlation coefficient value was obtained between diameter at middle and diameter at top (0.99) (Table 10).

	тнт	CD	Dbh	Db	Dm	Dt	CL	ВА	CR	SLC	СРА	Vol
тнт	1											
CD	0.63	1										
Dbh	0.83	0.72	1									
Db	0.77	0.71	0.92	1								
Dm	0.76	0.67	0.93	0.86	1							
Dt	0.74	0.65	0.91	0.85	0.99	1						
CL	0.97	0.61	0.77	0.71	0.71	0.69	1					
ВА	0.67	0.6	0.88	0.89	0.84	0.83	0.58	1				
CR	0.31	0.24	0.19	0.15	0.16	0.15	0.5	0.05	1			
SLC	-0.23	-0.44	-0.57	-0.49	-0.51	-0.5	-0.22	-0.35	-0.01	1		
СРА	0.54	0.89	0.68	0.72	0.65	0.65	0.51	0.7	0.14	-0.33	1	
Vol	0.48	0.41	0.6	0.75	0.59	0.59	0.38	0.85	-0.02	-0.15	0.56	1

**Table 10:** Correlation matrix for tree growth variables in the study area. THT=Total height (m), CD=Crown diameter (m),  $D_{bh}$ =Diameter at breast height (m),  $D_{b}$ =Diameter at base (m),  $D_{m}$ =Diameter at middle (m), Dt=Diameter at top (m), CL=Crown length (m), BA=Basal area (m<sup>2</sup>), CR=Crown ratio, SLC=Tree slenderness coefficient, CPA=Crown projection area (m<sup>2</sup>) and Vol=Volume (m<sup>3</sup>)

The value (0.97) obtained between crown length and total height is also very high and positive. There is a high correlation between some of the variable for example;  $D_{bh}$  and  $D_b$  (0.92),  $D_m$  (0.93),  $D_t$  (0.91) and BA (0.88). There is a negative relationship between tree slenderness coefficient and all the other growth variables.

## The volume equations

**Volume equations for all species combined:** The volume equations for all species combined is presented in Table 11a-11e. The results of the simple linear regression volume equations, using dbh, height or crown diameter only as predictor variable, is presented in Table 11a. The model  $v=b_0+b_1DH$  had the highest coefficient of determination ( $R^2$ ) of 0.70; the value of  $b_0$  is negative in all the models. However,  $b_1$  has a positive value for each of the models. The standard errors are reasonably high.

The developed multiple linear regression volume functions (Table 11b), with the exception of the model  $v=b_0+b_1BA+b_2H$ , the value of  $b_0$  is negative in all the models. However,  $b_1$  has a positive value for each of the models. The best multiple linear regression model is  $v=b_0+b_1BA$ + $b_2H$ , coefficient of determination (R<sup>2</sup>) of 0.73.

The results of log-transformed models (Table 11c), with model  $lnv=b_0+b_1 lnD_b+b_2lnH$  ranked 1st. The criteria adopted for ranking the models was through comparison of coefficient of determination (R<sup>2</sup>) and standard error of the estimate (SEE) which is one of the standard ways of ranking and validating models as pointed out by Huang et al. [46].

The higher the  $R^2$  values the better and the lower the SEE the better. Previous studies such as Akindele [47] have shown that equations with  $R^2$  values of 0.86 and 0.96 or higher are considered very good and make good predictors. Low SEE values indicate high level of precision.

 Table 9: Crown diameter class.

The standard error of estimate is a good measure of overall predictive value of regression equations [47]. It is a common measure of goodness of fit in regression models, with low values indicating better fit. In the log-transformed models, the SEE values ranged from 0.2740 to 1.4409.

Relationship between growth variables















Model form	<b>b</b> <sub>0</sub>	<b>b</b> <sub>1</sub>	R <sup>2</sup>	SEE
v=b <sub>0</sub> +b <sub>1</sub> D	-2.717	13.804	0.36	3.9772
v=b <sub>0</sub> +b <sub>1</sub> DH	-1.5872	1.006	0.7	2.7138
v=b <sub>0</sub> +b <sub>1</sub> CD	-2.617	1.064	0.17	4.5226

**Table 11a:** Simple linear regression volume equations. H=Total height (m), CD=Crown diameter (m), D=Diameter at breast height (m), v=volume (m<sup>3</sup>), b<sub>0</sub>=regression constant (intercept), b<sub>1</sub>=regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate

Model form	<b>b</b> <sub>0</sub>	b <sub>1</sub>	b <sub>2</sub>	R2	SEE
v=b <sub>0</sub> +b <sub>1</sub> D+b <sub>2</sub> H	-2.5429	14.572	-0.0548	0.36	3.9772
$v=b_0+b_1D_m+b_2H$	-2.7722	20.8561	0.1053	0.35	4.0076
$v=b_0+b_1D_t+b_2H$	-2.8371	42.8348	0.1402	0.35	4.0101
$v=b_0+b_1D_b+b_2H$	-2.169	12.7459	-0.3077	0.58	3.206
v=b <sub>0</sub> +b <sub>1</sub> D+b <sub>2</sub> CL	-1.9405	17.3746	-0.8764	0.38	3.9286
v=b <sub>0</sub> +b <sub>1</sub> BA+b <sub>2</sub> H	0.1909	21.9217	-0.1969	0.73	2.5996

**Table 11b:** Multiple linear regression volume equations. H=Total height (m),  $D_b$ =Diameter at base (m),  $D_m$ =Diameter at middle (m),  $D_t$ =Diameter at top (m), D=Diameter at breast height (m), v=Volume (m<sup>3</sup>), CL=Crown length (m), BA=Basal area (m<sup>2</sup>),  $b_0$ =regression constant (intercept),  $b_1$  and  $b_2$ =regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate

Model form	<b>b</b> <sub>0</sub>	<b>b</b> <sub>1</sub>	<b>b</b> <sub>2</sub>	R <sup>2</sup>	SEE
Inv=b <sub>0</sub> +b <sub>1</sub> InD	1.7569	2.4034		0.92	0.5183
Inv=b <sub>0</sub> +b <sub>1</sub> InCD	-4.2279	2.0508		0.48	1.3141
Inv=b <sub>0</sub> +b <sub>1</sub> InD <sub>2</sub>	1.7552	1.2014		0.92	0.2687
Inv=b <sub>0</sub> +b <sub>1</sub> In DH	-2.388	1.4859		0.94	0.4479
Inv=b <sub>0</sub> +b <sub>1</sub> InD <sub>2</sub> H	-0.7851	0.931		0.94	0.4285

	7 2541	1 4071	2 7607	0.02	0 7722
	-7.2041	1.4271	2.7007	0.02	0.7722
$Inv=b_0+b_1InD+b_2InH$	-1.0679	1.7975	1.0307	0.95	0.4278
$Inv=b_0+b_1InD_b+b_2InH$	-2.1228	1.8797	1.2094	0.98	0.274
$Inv=b_0+b_1InD_m+b_2InH$	-1.5735	1.4174	1.4898	0.94	0.4625
$lnv=b_0+b_1 lnD_t+b_2lnH$	-1.184	1.273	1.6542	0.92	0.5042
Inv=b <sub>0</sub> +b <sub>1</sub> InBA+b <sub>2</sub> InH	-0.854	0.8982	1.0313	0.94	0.4278
Inv=b <sub>0</sub> +b <sub>1</sub> InD+b <sub>2</sub> InCL	0.7258	1.9689	0.6599	0.94	0.454
Inv=b <sub>0</sub> +b <sub>1</sub> InD <sub>2</sub> +b <sub>2</sub> InH <sub>2</sub>	-7.2541	1.4271	1.3803	0.82	0.7722

**Table 11c:** Logarithm transformed regression volume equations. In=natural log, H=Total height (m),  $D_b$ =Diameter at base (m),  $D_m$ =Diameter at middle (m),  $D_t$ =Diameter at top (m), D=Diameter at breast height (m), v=volume (m<sup>3</sup>), CL=Crown length (m), BA=Basal area (m<sup>2</sup>), b0=regression constant (intercept), b<sub>1</sub> and b<sub>2</sub>=regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate.

Table 11d shows the quadratic regression volume equations. The volume function;  $v=b_0 + b_1D_2H$  has an R<sup>2</sup> value of 0.93, this is probably due to use of the reciprocal of  $D_2H$  as a weighting factor which appeared to be appropriate for reducing heteroscedasticity. Similar

remarks have been made by other researcher including Akindele [47], Cunia [48], Clutter et al. [12] and Philip [49]. Bi and Hamilton [15] explained that this variable represents the volume of a cylinder of diameter D and height H. Stem volume is directly related to the cylindrical volume by the coefficient of this variable that varies with stem form, that is, the solid shape of the stem.

Model form	b <sub>0</sub>	<b>b</b> <sub>1</sub>	b <sub>2</sub>	R <sup>2</sup>	SEE
$v=b_0 + b_1 D_2$	-0.9339	15.457		0.72	2.6533
$v=b_0 + b_1 D_2 H$	-0.2945	0.7607		0.93	1.3243
$v=b_0 + b_1 D_2 + b_2 H$	0.191	17.2195	-0.1969	0.73	2.5996
$\mathbf{v}=\mathbf{b}_0+\mathbf{b}_1\mathbf{D}_2+\mathbf{b}_2\mathbf{H}_2$	-1.1539	14.0425	0.0065	0.72	2.6391

Table 11d: Quadratic regression volume equations. H=Total height (m), D=Diameter at breast height (m), v=volume (m<sup>3</sup>), b<sub>0</sub>=regression constant (intercept), b<sub>1</sub> and b<sub>2</sub>=regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate

The  $R^2$  values ranged between 0.87 and 0.98 for the polynomial regression volume equations generated (Table 11e) for IITA Forest Reserve. All the polynomial regression models developed in this study were discovered to be very adequate for yield estimation in secondary rainforest ecosystem and they are recommended for further use.

Model form	<b>b</b> <sub>0</sub>	<b>b</b> <sub>1</sub>	<b>b</b> <sub>2</sub>	b <sub>3</sub>	<b>b</b> <sub>4</sub>	R <sup>2</sup>	SEE
$v=b_0+b_1D_2+b_2H+b_3D_2H$	0.256	-11	0.0055	1.2073		0.97	0.8955
$v=b_0+b_1D+b_2H+b_3D_2+b_4H_2$	3.8942	-10.833	-0.9213	16.2284	0.0686	0.87	1.7793
$v=b_0+b_1D+b_2D_2+b_3DH+b_4D_2H$	-0.722	10.488	-18.978	-0.5674	1.618	0.98	0.7734
$v=b_0+b_1D_2+b_2H_2+b_3D_2H+b_4DH_2$	0.3876	-9.2319	0.0064	0.9694	0.015	0.97	0.8874

**Table 11e:** Polynomial regression volume equations. H=Total height (m), D=Diameter at breast height (m), v=volume (m<sup>3</sup>),  $b_0$ =regression constant (intercept),  $b_1$ ,  $b_2$ ,  $b_3$  and  $b_4$ =regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate

**Fit statistics:** The intercept  $(b_0)$ , slope  $(b_1)$ , coefficient of determination  $(R^2)$ , standard error of estimates (SEE), observed volume, predicted volume and % biases are presented in Table 12a for

simple linear models SEE for total volume ranged from 3.8515 to 8.5888. The % biases also ranged from 12.51 to 48.81%. These values were relatively high.

Model form	<b>b</b> 0	<b>b</b> <sub>1</sub>	R <sup>2</sup>	SEE	Observed vol.	Predicted vol.	Bias (%)
v=b <sub>0</sub> +b <sub>1</sub> D	-0.7414	2.1198	0.56	6.8561		1.11 ± 0.23	31.09
v=b <sub>0</sub> +b <sub>1</sub> DH	-2.6380	1.4256	0.86	3.8515	1.62 ± 0.66	1.41 ± 0.43	12.51
v=b <sub>0</sub> +b <sub>1</sub> CD	-0.9416	2.8318	0.31	8.5888		0.91 ± 0.13	48.81

**Table 12a:** Validation results and % bias of the simple linear models with simple linear regression model. H=Total height (m), CD=Crown diameter (m), D=Diameter at breast height (m), v=Volume ( $m^3$ ),  $b_0$ =regression constant (intercept),  $b_1$ =regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate

Validation results was carried out on the multiple linear models which had a  $R^2$  greater than 0.50. There was a high  $R^2$  and high standard error of the regression equations as shown in Table 12b. The percentage biases range from 22.87% to 33.45%.

Model form $\mathbf{b}_0$ $\mathbf{b}_1$ $\mathbf{R}^2$ SEEObservPredictBias(%)
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v=b <sub>0</sub> +b <sub>1</sub> Db -0.235 1.718	4.343 1.62 ±	1.08 ±
+b <sub>2</sub> H 6 6 0.8	8 0.66	0.35 33.45

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v=b <sub>0</sub> +b <sub>1</sub> BA +b <sub>2</sub> H	-0.041 2	1.328 7	0.84	4.203 6		1.24 0.46	±	22.87
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**Table 12b:** Validation results and % bias of the multiple linear models with simple linear regression model. H=Total height (m), Db=Diameter at base (m), BA=Basal area (m2), b0=regression constant (intercept), b1=regression coefficients, R2=Coefficient of Determination and SEE=Standard Error of Estimate

The R<sup>2</sup> for the log transformed equations ranged from 0.35 to 0.96 for models for predicting total volume and SEE ranged from 0.3597 to 1.4004 (Table 12c). lnv=b<sub>0</sub>+b<sub>1</sub> lnD<sub>m</sub>+b<sub>2</sub>lnH had the lowest positive % biases of 2.72%. lnv=b<sub>0</sub>+b<sub>1</sub> lnD<sub>2</sub>, lnv=b<sub>0</sub>+b<sub>1</sub> lnD<sub>2</sub>+b<sub>2</sub>lnH and lnv=b<sub>0</sub>+b<sub>1</sub> lnD<sub>2</sub>+b<sub>2</sub>lnH<sub>2</sub> had a high negative % biases.

Model form	<b>b</b> 0	<b>b</b> <sub>1</sub>	R <sup>2</sup>	SEE	Observed vol.	Predicted vol.	Bias (%)
Inv=b <sub>0</sub> +b <sub>1</sub> InD	0.051 8	0.98 32	0.9 0	0.55 94		-1.96 ± 0.11	-4.41
Inv=b <sub>0</sub> +b <sub>1</sub> InCD	-0.01 37	0.90 16	0.3 5	1.40 04		-2.06 ± 0.07	-9.95
Inv=b <sub>0</sub> +b <sub>1</sub> InD <sub>2</sub>	3.320 5	0.57 94	0.9 0	0.55 94		-8.99 ± 0.18	-378. 99
Inv=b <sub>0</sub> +b <sub>1</sub> In DH	-0.00 06	0.99 66	0.9 2	0.50 17		-1.88 ± 0.11	-0.23
Inv=b <sub>0</sub> +b <sub>1</sub> InD <sub>2</sub> H	0.021 7	0.99 46	0.9 2	0.47 82		-1.91 ± 0.11	-1.62
$\frac{\text{Inv=b}_0\text{+}\text{b}_1}{\text{InD}_2\text{+}\text{b}_2\text{InH}}$	1.258 0	0.73 73	0.8 9	0.58 36		-4.26 ± 0.14	-126. 88
$lnv=b_0+b_1$ $lnD$ $+b_2lnH$	0.017 8	0.99 52	0.9 2	0.47 81	-1.88 ± 0.11	-1.90 ± 0.11	-1.34

Inv=b <sub>0</sub> +b <sub>1</sub> +b <sub>2</sub> InH	InD <sub>b</sub>	0.003 4	0.98 67	0.9 6	0.35 97	-1.91 0.11	±	-1.54
Inv=b <sub>0</sub> +b <sub>1</sub> +b <sub>2</sub> InH	InD <sub>m</sub>	-0.03 83	1.00 66	0.9 3	0.43 58	-1.83 0.11	±	2.72
Inv=b <sub>0</sub> +b <sub>1</sub> <sub>+</sub> b <sub>2</sub> InH	InDt	-0.03 82	1.00 96	0.9 3	0.47 23	-1.83 0.11	±	2.99
Inv=b <sub>0</sub> +b <sub>1</sub> +b <sub>2</sub> InH	InBA	0.018 5	0.99 55	0.9 2	0.47 81	-1.90 0.11	±	-1.35
Inv=b <sub>0</sub> +b <sub>1</sub> +b <sub>2</sub> InCL	InD	0.046 9	1.00 04	0.9 2	0.50 44	-1.92 0.11	±	-2.35
Inv=b <sub>0</sub> +b <sub>1</sub> InD <sub>2</sub> +b <sub>2</sub> InH	2	1.258 2	0.73 73	0.8 9	0.58 36	-4.25 0.14	±	-126. 89

**Table 12c:** Validation results and % bias of the Logarithm transformed regression models with simple linear regression model. In=natural log, H=Total height (m),  $D_b$ =Diameter at base (m),  $D_m$ =Diameter at middle (m),  $D_t$ =Diameter at top (m), D=Diameter at breast height (m), v=Volume (m<sup>3</sup>), CL=Crown length (m), BA=Basal area (m<sup>2</sup>),  $b_0$ =regression constant (intercept),  $b_1$ =regression coefficients, R<sup>2</sup>=Coefficient of Determination and SEE=Standard Error of Estimate

There was a high  $R^2$  and high standard error of the regression equations as shown in Table 12d except model  $v=b_0+b_1D_2H$  which had a SEE of 2.0346. The percentage biases range from 2.36% to 22.86%.

The R<sup>2</sup> for the polynomial models ranged from 0.93 to 0.99 and SEE ranged from 0.9012 to 2.6472 (Table 12e).  $v=b_0+b_1D+b_2H+b_3D_2+b_4H_2$  had the only positive % biases of 14.25%.  $v=b_0+b_1D_2+b_2H_2+b_3D_2H$ + $b_4DH_2$  had a high negative % biases of -58.54%.

Model form	<b>b</b> 0	<b>b</b> 1	R <sup>2</sup>	SEE	Observed vol.	Predicted vol.	Bias (%)
v=b <sub>0</sub> +b <sub>1</sub> D <sub>2</sub>	-0.2049	1.3664	0.83	4.2204		1.33 ± 0.44	17.58
v=b <sub>0</sub> +b <sub>1</sub> D <sub>2</sub> H	-0.0969	1.0850	0.96	2.0346	1.62 ± 0.66	1.58 ± 0.60	2.36
v=b <sub>0</sub> +b <sub>1</sub> D <sub>2</sub> +b <sub>2</sub> H	-0.0413	1.3287	0.84	4.2036		1.25 ± 0.46	22.86
v=b <sub>0</sub> +b <sub>1</sub> D <sub>2</sub> +b <sub>2</sub> H <sub>2</sub>	-0.2735	1.3711	0.84	4.1188		1.38 ± 0.44	14.79

**Table 12d:** Validation results and % bias of the quadratic models with simple linear regression model. H=Total height (m), D=Diameter at breast height (m), v=Volume (m3), b0=regression constant (intercept), b1=regression coefficients, R2=Coefficient of Determination and SEE=Standard Error of Estimate.

Model form	<b>b</b> <sub>0</sub>	<b>b</b> <sub>1</sub>	R <sup>2</sup>	SEE	Observe d vol.	Predicte d vol.	Bias (%)
$v=b_0+b_1D_2+b_2H$ + $b_3D_2H$	-0.06 36	1.01 39	0. 99	1.18 70		1.66 ± 0.65	-2.49
$v=b_0+b_1D+b_2H$ + $b_3D_2+b_4H_2$	0.03 32	1.13 88	0. 93	2.64 72	1.62 ± 0.66	1.39 ± 0.56	14.25
$v=b_0+b_1D$ + $b_2D_2+b_3DH+b_4D_2H$	-0.07 74	0.99 87	0. 99	0.90 12		1.70 ± 0.66	-4.98

$v=b_0+b_1D_2+b_2H_2+b_3$ $D_2H+b_4DH_2$	-0.68 37	0.89 72	0. 98	1.40 23		2.56 0.73	±	-58.5 4
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**Table 12e:** Validation results and % bias of the polynomial models withsimple linear regression model. H=Total height (m), D=Diameter atbreast height (m), v=Volume (m<sup>3</sup>), b<sub>0</sub>=regression constant (intercept),b<sub>1</sub>=regression coefficients, R<sup>2</sup>=Coefficient of Determination andSEE=Standard Error of Estimate.

The logarithm transformed regression models  $lnv=b_0+b_1lnD+b_2lnH$  and  $lnv=b_0+b_1lnDb+b_2lnH$  were discovered to have good fit and as a result, they are very adequate for tree volume estimation. This is because of the high coefficient of variation  $(R^2)$  values and small

standard error of estimate. The percentage biases when the output of each model was compared with the observed volume for models  $lnv=b_0+b_1 lnD+b_2 lnH$  is -1.34 and  $lnv=b_0+b_1 lnDb+b_2 lnH$  is -1.54.

The results of the assessment and validation reveal that models  $lnv=b_0+b_1 lnD+b_2lnH$  and  $lnv=b_0+b_1 lnD_b+b_2lnH$  are the best for IITA forest reserves. The fitness and validity of all these models were further confirmed by obtaining the residual plots (i.e. residual values against predicted volume).

## Conclusion

A growth and yield model was developed for the growth of a tropical uneven aged secondary forest in IITA forest reserve, Ibadan. This study assessed tree species diversity and also tested the efficacy of linear regression equations for tree volume estimation in IITA forest ecosystem. One thousand two hundred and fourteen trees comprising 34 species distributed among 23 families were involved in model generation.

Stand volume is probably the most important output variable for forest managers, and integrates the effects of height, diameter and density. Volume estimation is critical to forest resource management. Estimation of this parameter is usually confounded by factors such as lack of equipment for measurement of tree height and upper diameter, difficulties in measurement of tree height in tropical forests, the complex architectural structure of tropical forests and the high cost of inventory work. To avoid this problem, models for total volume estimation were developed in this study.

Total volume estimates obtained using logarithm transformed models with height measurements and diameter at base as well as logarithm transformed models with height measurements and diameter at breast height were reasonable.

The prediction of volume in IITA forest reserve required the transformation of dependent and independent variables. Based on validation analyses, logarithm transformed diameter at base and logarithm transformed total height provides a reasonable alternative to other available equations when predicting total volume for IITA forest reserve in Ibadan.

Logarithmic transformation gives better results compared with other untransformed values. This is so because of high variability within and among species in terms of their size and height.

For forest managers, sustainably managing a particular forest tract means determining, in a tangible way, how to use it today to ensure similar benefits, health and productivity in the future. Forest managers must assess and integrate a wide array of sometimes conflicting factors-commercial and non-commercial values, environmental considerations, community needs, and even global impact-to produce sound forest plans.

Forest growth models have become an indispensable tool for forest management. Clearly, models are useful, but they could be more useful. To realize their full utility, models need to become more accurate, and need to become an integral part of the forest management system. Model predictions should be monitored to reveal any discrepancies between predicted and realized outturn. This feedback loop provides the basis for a system of continual improvement both in growth modeling and in forest management.

Growth and yield modeling is an essential prerequisite for evaluating the consequences of a particular management action on the

future development of forest ecosystem and has been central theme of Forest Management.

Forests are inherently complex. Models can be useful tools to understand the interactions and dynamic processes occurring in the forest, examine different forest management strategies and their impacts, study the development and evolution of trees and other competing vegetation, graphically visualize the responses of forests to human intervention, or observe ecological and economic interactions of the different components of a forest ecosystem. Forest growth and yield models are used routinely in forest management, and increasingly in other applications (e.g., investigation of impacts of climate change), and many users take their reliability for granted.

Models developed for IITA Forest Reserve can serve as decision support tools that ensure better, sound and sustainable management of the forests. Increasingly, models are becoming more integrated taking advantage of the strengths of each model making them more flexible, robust and user-friendly.

The fitted volume models yielded the statistical outcomes needed for further use. They are sound for volume estimation in this study area and at similar sites. If used outside the study area, some precautions must be taken. The models are recommended for further use. The appropriate use of the developed model may be short-term inventory updating. For long-term projection, the model should be used with caution. Nevertheless, the present model provides a useful tool for forest researchers and managers to predict future stand states.

The cost of forest measurements during forest inventories will be considerably reduced when using volume tables since reliable volume estimates based on two easy measurable variables (height and diameter at base) can be obtained.

Since this forest have no developed growth and yield models, this model has great potential for managers of this forest and should be considered as a useful tool in planning its use and management.

## References

- Vanclay JK (1994) Modelling Forest Growth and Yield: Applications to Mixed Tropical Forests. CABI Publishing, CAB International, Wallingford, UK, pp: 312.
- Johnsen K, Samuelson L, Teskey R, McNulty S, Fox T (2001) Process models as tools in forestry and management. Forest Science 47: 2-8.
- Weiskittel AR, Hann DW, Kershaw Jr JA, Vanclay JK (2011) Forest growth and yield modeling. John Wiley and Sons, Ltd., Markono Print Media Ltd, Singapore, pp: 415.
- Mohren GM, Burkhart HE, Jansen JJ (1994) Contrasts between biologically-based process models and management oriented growth and yield models. Forest Ecological Managemen 69: 1-5.
- 5. Changhui P (1999) Growth and yield models for uneven-aged stands: past, present and future. Forest Ecology and Management 132: 259-279.
- Yuancai L, Parresol BR (2001) Remarks on height-diameter modeling. Res. Note SRS-10. USDA Forest Service, Southern Research Station, Asheville, NC, pp: 5.
- Miller RI (1994) Mapping for Monograph: Baselines for Resource. In Miller RI (edn). Mapping the Diversity of Nature Chapman and Hall, NY, pp: 21-25.
- 8. Krajicek JE, Brinkman KA, Gingrich SF (1961) Crown competition: a measure of density. Forest Science 7: 35-42.
- 9. Ayhan HO (1973) Crown diameter/dbh relationships in Scots pine. Arbor 5: 15-25.
- Husch B, Beers TW, Kershaw Jr JA (2003) Forest Mensuration. 4th ed. John Wiley and Sons, Inc., New Jersey, USA, pp: 443.

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- 11. Schumacher FX, Hall FS (1933) Logarithmic expression of timber-tree volume. Journal of Agricultural Research 47: 719-734.
- Clutter JL, Fortson JC, Pienaar LV, Brister GH, Bailey RL (1983) Timber Management: A Quantitative Approach. JohnWiley and Sons, New York, pp: 333.
- Laar A, Akça A (2007) Forest Mensuration. Dordrecht, The Netherlands. Springer, pp: 383.
- 14. Spurr H (1952) Forest Inventory. The Ronald Press Company, New York, pp: 476.
- Bi H, Hamilton F (1998) Stem volume equations for native tree species in southern New South Wales and Victoria. Australian Forestry 61: 275-286.
- 16. Edminster CB, Beeson RT, Metcalf GB (1980) Volume tables and pointsampling factors for ponderosa pine in the front range of Colorado. Rocky Mountain Forest and Range Experiment Station, Research Paper RM-218. US Forest Service, US Department of Agriculture, pp: 14.
- 17. Abayomi JA (1983) Volume tables for Nauclea diderrichii in Omo forest reserve, Nigeria. Nigerian Journal of Forestry 13: 46-52.
- Omule SAY, Fletcher VE, Polsson KR (1987) Total and merchantable volume equations for small coastal Douglas-fir. B.C. Min. For. Lands-FRDA Rep.
- Thomas JJ (1977) An introduction to statistical analysis for economists. Weidenfeldand Nicholson Ltd, London, pp: 286.
- VanHorn R (1969) Validation in the Design of Computer Simulation Experiments. H. Naylor (ed) Duke Uni Press, Durham, NC, pp: 232-235.
- 21. Marshall PL, Northway (1993) Suggested minimum procedure for validation of growth and yield model. In: Vanclay JK, et al. (eds). Growth and yield estimation from successive forest inventories. IUFRO World Congress proceedings, Copenhagen, pp: 281.
- Maltamo M, Kangas A (2008) Methods based on k-nearest neighbor regression in estimation of basal area diameter distribution. Canadian Journal of Forest Research 28: 1107-1115.
- 23. Cooper RA, Weekes AJ (1983) Data, Models and Statistical. Published by Barnes and Noble Books.
- 24. Neter J, Kutner M, Nachtsheim C, Wasserman W (1996) Applied Linear Statistical Models. McGraw-Hill Companies, Inc., NY.
- Amaro A, Reed D, Tome M, Themido I (1998) Modelling dominant height growth: Eucalyptus plantations in Portugal. Forest Science 44: 37-46.
- Onyekwelu JC, Akindele SO (1995) Stand volume equation for Gmelina arborea plantations in Oluwa Forest Reserve, Nigeria. Nigerian Journal of Forestry 24-25: 92-95.
- Adekunle VAJ, Akindele SO, Fuwape JA (2004) Structure and yield models for tropical lowland rainforest ecosystem of South West Nigeria. Food Agric Environ 2: 395-399.
- 28. Adekunle VAJ (2006) Conservation of tree species diversity in tropical rainforest ecosystem of Southwest Nigeria. J Trop For Sci 18: 91-101.
- 29. Ajit S (2010) Estimation and validation methods in tree volume and biomass modelling: statistical concept. National Research Centre for agroforestry, Jhansi, India, p: 18.
- Goulding CJ (1979) Validation of Growth Models Used In Forest Management. New Zealand Journal of Forestry 24: 108-124.

- Navratil S, Brace LG, Sauder EA, Lux S (1994) Silvicultural and harvesting options to favour immature white spruce and Aspen regeneration in Boreal Mixed woods Can. For. Serv. North. For Cent. Inf. Rep. No. NOR-X-337.
- Peltola H, Kellomaki D (1993) A mechanistic model for calculating withdraw and stem breakage of Scots pines at stand edge. Silva Fennica 27: 99-111.
- Petty JA, Swain C (1985) Factors influencing stress breakage of conifers in high winds. Forestry 58: 75-84.
- 34. Erteld W, Hengst E (1966) Forest income doctrine. Radebeul neumann publisher.
- 35. Jaworski A (2004) Growth increment and ecological foundations for regeneration and tending of stands. State Publishing House for Agriculture and Forestry Warsaw.
- Peltola HM (2006) Mechanical stability of trees under static loads. American Journal of Botany 93: 1501-1511.
- Gardiner B, Marshall B, Achim A, Belcher R, Wood C (2005) The stability of different silvicultural systems: a wind-tunnel investigation. Forestry 78.
- 38. Smith DM (1988) The practice of silviculture. New York: John Wiley.
- 39. Hasenauer H, Monserud RA (1996) A crown ratio model for Austrian forests. Forest Ecology and Management 84: 49-60.
- 40. Leites LP, Robinson AP, Crookston NL (2009) Accuracy and equivalence testing of crown ratio models and assessment of their impact on diameter growth and basal area increment predictions of two variants of the Forest Vegetation Simulator. Canadian Journal of Forest Research 39: 655-665.
- Monserud RA, Sterba H (1996) A basal area increment model for individual trees growing in even- and uneven-aged forest stands in Austria. Forest Ecology and Management 80: 57-80.
- 42. Oliver CO, Larson BC (1996) Forest Stand Dynamics. John Wiley and Sons, Toronto.
- 43. Kershaw JA, Maguire DA, Hann DW (1990) Longevity and duration of radial growth in Douglas-fir branches. Canadian Journal of Forest Research 20: 1690-1695.
- Navratil S (1997) Wind damage in thinned stands. In: Proceedings of a commercial workshop. Whitecourt, AB, October 17-18, 1997. Forest Engineering Research Institute of Canada (FERIC), pp: 29-36.
- 45. Crookston NL, Stage AR (1999) Percent canopy cover and stand structure statistics from the Forest Vegetation Simulator. US For. Ser. Gen. Tech. Rep. RMRS-GTR-24, p: 11.
- 46. Huang S, Yang Y, Wang Y (2003) A critical look at procedures for validating growth and yield models. In: Amaro A, Reed D and Soares P (eds.). Modeling Forest Systems. CAB international.
- Akindele SO, LeMay VM (2006) Development of tree volume equations for common timber species in tropical rain forest area of Nigeria. Forest Ecology and Management 226: 41-48.
- Cunia T (1964) Weighted least squares method and construction of volume tables. Forest Science 10: 180-191.
- Philip MS (1994) Measuring Trees and Forests. 2nd edn. CAB International, Wallingford, UK, p: 310.