Characterization of Ion-Uptake for Single Osteoblast Cell under Electrical Stimuli

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Abstract

This paper presents the numerical and analytical characterization of ion uptake of osteoblast cell under the influence of different electrical stimuli. The effects of pico electrical field, electrode configuration, micro channel dimension and property of suspension media on ion uptake were investigated. The electrodes were assumed to be embedded in the walls of the microchip & osteoblast cell was suspended between these electrodes. In this context it is observed that the efficient ion uptake is conducted in very short duration low amplitude DC impulse. It is found that the ion uptake is sinusoidal distributed over the surface of osteo cell membrane and it is minimum at pole θ=90 & θ=270 and maximum value is obtained at pole θ=180 which is independent of specification of electrical pulse, geometry of electrode, dimension of micro channel & property of suspension media. But their value depends on the above parameters. So the region near by the θ=90 & θ=270 are assigned as high permeable area of the osteoblast cell. The effect of neighbour cells on ion-uptake is considered to make the result more authentic and realistic.

Keywords: Bi layer membrane; Ion uptake; Electrical stimuli; Osteoblast cell; Micro electrode

Introduction

All biological cells have bi-layer selectively-permeable membrane made by phospholipids that controls the exchange of ions and different materials such as sodium or potassium [1]. Inspire of this Lipid and proteins on the cell membrane surface often have short carbohydrate chains protruding out from the cell surface, known as glycolipids and glycoproteins. They form hydrogen bonds with the water molecules surrounding the cell and thus help to stabilize membrane structure. However, more importantly, they are used as receptor molecules, binding with hormones or neurotransmitters to trigger a series of chemical reactions within the cell itself. Among them sodium ion is more use full to generate nerve impulse and maintain the electrolyte balance and fluid balance [2]. The distribution of sodium ions are mediated in all animals by Na+/K+-ATPase, which is an active transporter pumping ions against the gradient, and sodium/potassium channels [3]. Transition metals such as iron, copper, manganese, and zinc are essential nutrients. High-affinity systems are active in metal-limited cells, whereas low-affinity systems play the predominant roles when the substrate is more abundant. Metal ion uptake systems of cells are tightly controlled, and both transcriptional and posttranscriptional regulatory mechanisms have been identified [4]. So ion uptake is an inherent property of biological cell. It is also applicable in rigid cell like osteolast [5]. But due to non-uniform distribution and concrete structure of osteoblast cell gives the challenges to researchers for its ion uptake.

A number of research works has been done considering the soft biological cell [6-8] but it is not applicable in osteoblast cell. We are focusing on that limitation and consider the original bi-layer structure of osteoblast cell. In this context a numbers of experimental study carried on at the outside of the micro or nano fluidic but all the reported studies on cell membrane surface pressure considered the cells in an infinitely large medium [9]. In micro fluidic devices, the cells are usually located in micro channels or micro chambers. The results of the current published studies may not reflect the boundary effects of micro fluidic-based electroporative devices & perfect optimization is to be needed [12]. As a result the original and realistic information about the developed ion uptake is limited for multi-layer or bi layer cell mainly in rigid cell like bone cell.

With references to the above limitations the bi-layer rigid bone cell like osteoblast is considered and ion uptake of bi-layer osteoblast cell is investigated, which is located in a micro channel in between two side wall electrodes. We also find out the effect of neighbour cells on it. The pulse shape was chosen as a square wave, which is widely used in the micro fluidic devices. This electric pulse shape can be easily generated by contracting the cross-sectional area of the micro channels or using a high-voltage Pulse generator [13]. Although we can also use the triangular or saw tooth electrical pulse but the results are not expected, where as in micro-fluidic channel the rectangular pulse is more convenient to apply.

In first part of the present study the analytical study of ion uptake for bi-layer osteoblast which is placed in between two electrodes at the micro fluidic channel is addressed. In the remaining part of this paper the effects of the specification of rectangular electric pulse (duration, intensity, interval), electrode geometry (width, gap, and shape, material), dimension of micro fluidic channel as well as the nature of suspension media on ion uptake of osteoblast cell at radio frequency (10GHz) have been studied. As the cells are in contact together tightly so we also consider the effect of neighbour cells on membrane electroporation to make the result more important and realistic. The mathematical modelling and governing equations of cell membrane ion uptake are introduced in numerical simulation section and Result and Discussion deals with graphical and numerical approach of our current study. All the information of our study gives the new aid to the osteo clinical diagnosis and bone cancer treatment.

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Theoretical Analysis of Ion Uptake

Effect of rectangular pulse specification on ion uptake

The following Schematic diagram of double -shelled spherical cell in suspension, which is used for theoretical explanation of membrane potential of a biological cell [14,15], which is related with ion uptake of the cell (Figure 1).

According to the transfer functions defined by C. Yao the inner and outer membranes to a given rectangular pulse electric field $E(t)$ can be obtained

$$V_m(t) = L^2 \left[ H_m(s) \cdot E(S) \right]$$

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Where,

$$H_m(s) = \frac{v_m(s) \cos \theta}{E(s)} - \frac{1.5 R_e \cos \theta}{t_{cell} S + 1}$$

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After simplification of equation (1) & (2) we get the outer membrane potential $V_{m}(t)$ are as follows

$$V_m(t) = 1.5 R_e E(t) \left[ -e^{-\frac{v}{d}} - l(t-\tau) + e^{-\frac{v}{d}} \cdot l(t-\tau) \right] \cos \theta$$

(3)

It is known from the bio chemistry that the ion uptake can be calculated by following mathematical calculation,

$$I_{uptake} = Kf \left[ 1 + \left( 1 + \frac{Kp}{v_m} \right) \cdot e^{-\frac{Kp}{v_m}} \right]$$

$$(17)$$

Where, $Kf = \frac{DSc}{ve}$, and $Kp = \frac{v}{d}$,

$$v = \left[ \left( \frac{AR. v_m(t) \cdot \text{area}(s) \cdot e^{V_m}}{8Kb.T.d^2} \right) \right]$$

$$(4)$$

$D =$ Diffusion co efficient, $Vc =$ Area of the pore, $d =$ thickness, $Sc =$ N. r. x²,

$ARVp =$ Area of pore, $\Delta R Vp =$ Area of pore

$T =$ Temp in kelvin.

$Kb =$Boltz man constant

$\varepsilon W =$permittivity of water,

$\varepsilon C =$permittivity of cytoplasm. &

$Te =$pulse duration.

$r \bar{=} =$radius of initial pores,

$r m (t) =$membrane potential

By replacing $r m (t)$ from equation 3 into the equation 4, the dependency of pulse specification on ion uptake is addressed.

Effect of micro-electrode specification on ion uptake

As we know that $E(t) = v / d$

where $v =$applied voltage & $d =$ distances in between two electrode. We replace $E(t) =$ v/d in equation (3) & (4) and get outer membrane potential $V_{m}(t)$ is

$$V_m(t) = 1.5 R_e \left[ \frac{v}{d} \right] \left[ -e^{-\frac{v}{d}} - l(t-\tau) + e^{-\frac{v}{d}} \cdot l(t-\tau) \right] \cos \theta$$

(5)

If the value of $V_m(t) is replaced in equation (4) than the relation among the ion uptake occurred with intra-electrode gape is established.

In this context it is known from the theory of electrochemistry the value of produced voltage at metal electrode $v$ is expressed as

$$v = - \frac{K \cdot T}{z \cdot e} \log (C_{net})$$

(6)

Where $K =$ Boltz man constant, $T =$ absolute temperature, $z =$ valancy of electrode material & $e =$charge of an electrode, $C_{net} =$ ionic concentration of electrode material. If the value of $V$ is replaced in equation (5) and (4) than the relation among the ion uptake occurred with electrode material and shape of electrode is established.

From the knowledge of dielectric spectroscopy of cell membrane it is found out that

$$\frac{1}{2T^0} + \frac{1}{R_i \cdot 2 \cdot G_f} \cdot \left( \frac{1}{4} \right)$$

(7)

Where $R_i =$ resistances of cytoplasm, $\phi =$ volume fraction,

$$G_f = \left( \frac{\text{width of electrode } \cdot \text{length of electrode}}{\text{inter electrode gap}} \right)$$

Replaces $\frac{1}{2T^0} + \frac{1}{R_i \cdot 2 \cdot G_f} \cdot \left( \frac{1}{4} \right)$ in equation (3), it is obtained that

$$\text{recell} = R_i \cdot 2 \cdot G_f \cdot \left( \frac{1}{4} \right) \cdot \frac{\text{area} \cdot d}{\text{dm} \cdot d}$$

(8)

By replacing, recell = $R_i \cdot 2 \cdot G_f \cdot \left( \frac{1}{4} \right) \cdot \frac{\text{area} \cdot d}{\text{dm} \cdot d}$ and

$$v = \left( \frac{K \cdot T}{z \cdot e} \right) \log (C_{net})$$

(3) & (4), then the dependency of electrode width, length, material and geometry on ion uptake of the osteo blast cell is expressed.

Effect of micro-channel specification on ion uptake

It is reported that if radius of cell is $R_i$ and channel height $H$ than relative resistances of cell placed in the micro channel is consider as $R = R_i / 2H$ If we replaces $R = R_i / 2H$ in equation (3) and (4) then the effect of channel height on ion uptake is established.

The basic concept of micro fluidic devices the channel resistances $R$ $ch$ is numerically defined as $R_{ch} = \frac{Kz}{\sigma m \cdot d}$ and $Kz = \frac{2k (k^2)}{k (1-k^2)}$

Where $k = 2$ for biological cell, $\sigma m =$ Conductivity of medium and $d = dn = d$

Thickness of Membrane.

After simplification it is turned as

**Figure 1: Schematic of double -shelled spherical.**
\[ d = \frac{2 \cdot k_z}{Rch \cdot \sigma m} \]  
\[ Wc = \left[ V0 \cdot \left( \frac{Rch + 2 \cdot Raqu}{2 \cdot Raqu} \right) \right] \left( \frac{k_z}{2 \cdot k} \right) \]

On the other hand, width of the channel is defined as

\[ Wc = \left[ V0 \cdot \left( \frac{Rch + 2 \cdot Raqu}{2 \cdot Raqu} \right) \right] \left( \frac{k_z}{2 \cdot k} \right) \]

Where, \( V0 \) = Initial velocity of fluid, \( Raqu \) = resistances of aqua medium. By replacing value of equation (9) and (10) in equation (3) and (4) then the effect of channel resistances on ion uptake is exposed.

**Effect of micro-fluidics specification on ion uptake**

In primary concept of fluids dynamic it reveals that flow rate \( \frac{Q}{\Delta P / Rch} \), As channel resistances has a great influences on membrane potential so flow rate has also a large influences on membrane ion uptake.

**Numerical Analysis of Ion Uptake**

**Simulation tools**

In this study, above Equations are solved numerically to find the electric potential developed in outer and inner membrane to investigate the creation of nano-pores on the cell membrane. The Mat lab 7.2 & Comsol-4.3a, commercial package was used in the numerical simulations.

**Used simulation parameter**

Table 1 Values for constants and parameters used in the simulations [15] (Table 1).

**Electrical field analysis**

Figure 2a and 2b depicts the potential distribution with the micro devices having the non uniform distribution of potential and intra cellular organelle also effect by this field. At pole \( \theta = 90^\circ \) and \( \theta = 270^\circ \) maximum potential are exposed which is similar as our numerical result. And complete electrical potential distribution within the 3D hybrid micro chip. Where cell is affected through the whole channel. Figure 3 shows the Graphical view of polarization and electric field with respect to height of the bi metallic electrode within the 3D hybrid micro chip which helps us to find out the maximum polarization area of Nono pores. It explore that the centre part (300-600) \( \mu \text{m} \) of the chip holds the maximum uniform potential where the nano pores are generated at the intra organelle. Maximum velocity excreted at the centre of the chip, it affects the ion uptake of intra cellular unit of the rigid cell. All the information exposed in COMSOL simulation is as similar as numerical and experimental values of intra organelle nano poration of multi-layer dense osteoblast cell (Figures 2 and 3).

**Numerical simulation results and discussion**

In this study, above equations are solved numerically to find the surface pressure developed in outer and inner membrane to investigate the creation of nonporous on the cell membrane. The MATLAB7.2 & COMSOL 4.2a commercial package was used in the numerical simulations.

The quantitative information used in the simulations is provided in

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Cell parameters</th>
<th>Osteoblast</th>
</tr>
</thead>
<tbody>
<tr>
<td>conductivity (S/m)</td>
<td>Extracellular medium (σe)</td>
<td>( 10 \times 10^{-12} )</td>
</tr>
<tr>
<td></td>
<td>Cell membrane (σm)</td>
<td>( 1.2 \times 10^{-7} )</td>
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<tr>
<td></td>
<td>Cell cytoplasm (σc)</td>
<td>( 0.039 \text{s} )</td>
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<tr>
<td></td>
<td>Nuclear membrane (σn)</td>
<td>( 0.08 \text{s} )</td>
</tr>
<tr>
<td></td>
<td>Nuclear cytoplasm (σn)</td>
<td>( 0.08 \text{s} )</td>
</tr>
<tr>
<td>relative permittivity</td>
<td>Extracellular medium (ε)</td>
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<tr>
<td></td>
<td>Cell membrane (εm)</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>Cell cytoplasm (εc)</td>
<td>93</td>
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<tr>
<td></td>
<td>Nuclear membrane (εn)</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>Nuclear cytoplasm (εn)</td>
<td>93</td>
</tr>
<tr>
<td>Geometry parameter (μm)</td>
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<td>Cell membrane thickness (d)</td>
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<td></td>
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<td>( D )</td>
<td>( 5 \times 10^{15} )</td>
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</tr>
<tr>
<td></td>
<td>( \sigma )</td>
<td>( 1 \times 10^{-8} )</td>
</tr>
</tbody>
</table>

Table 1: Values for constants and parameters used in the simulations.

Figure 2: Potential distribution with the micro devices for the osteo ion uptake of a cell of radius a (12 μm).
Table 1. A cell of radius $a$ (12 µm) is considered in the microchannel of height (500µm). The necessary electric field (1v) was applied by the two electrodes of width (50 m) located on the walls of the micro channel. The electric pulse span was on the order of microseconds to pico second operated at radio frequency (10 GHz hertz). The results of the numerical simulations are as follows.

**Evaluation of pulse:** Figure 4(a) shows that the amount of ion uptake of osteoblast cell is sinusoidally varied with respect to azimuthal angle of the electric field. It is observed that if pulse interval is increased than the amount of molecules (ion uptake) taken by the cell is reduced and maximum ion uptake is occurred at pole $\theta = 180^\circ$ whereas minimum value at the pole $\theta = 90^\circ$ and $\theta = 270^\circ$. But Figure 4(b) shows that ion uptake is independent with pulse amplitude variation (Figure 4).

**Evaluation of micro-electrode:** In Figure 5(a) shows that ion uptake depends on the shape of the micro electrode and if the shape is saw-tooth than maximum ion uptake is occurred but polar location is fixed and it is $\theta = 180^\circ$.

From the Figure 5(b), it has also been observed that the value of ion uptake is inversely proportional with inter electrode distances and it is maximum when electrode gap is 10 µm.

**Evaluation of micro-channel:** Figure 6(a) shows that micro channel height does not effect the ion uptake and it is uniform throughout the whole micro channel but channel resistances affects the molecule incursion which is depicted in Figure 6(b). It also observed that the ion uptake inversely proportional with channel resistances and maximum value is obtained when channel resistances is 10 MΩ (Figure 6).

**Evaluation of micro-fluidics:** Figure 7 illustrates the effects of conductivity and flow rate of suspension media on ion uptake. Figure 7(a) shows that ion uptake of osteoblast cell is inversely proportional to conductivity of the micro fluids but flow rate does not effect on it. Finally it is concluded that the flow rate and conductivity of suspension medium have great influences on ion uptake. For efficient ion uptake the flow rate and conductivity should be as low as possible (Figure 7).
Figure 5: Variation of (a) electrode shape (b) electrode gap with azimuthal angle of electric field of the osteo ion uptake.

Figure 6: Variation of (a) channel height (b) channel resistance with azimuthal angle of electric field of the osteo ion uptake.

Figure 7: Variation of (a) conductivity (b) flow rate with azimuthal angle of electric field of the osteo ion uptake.
Conclusion

After all discussion it is concluded that ion uptake is not same throughout the whole surface of the osteoblast cell and it is sinusoidally occurred. The maximum ion uptake is occurred at pole $\theta = 180^\circ$ and minimum at pole $\theta = 90^\circ$ ad $\theta = 270^\circ$ which is independent of pulse, micro electrode, micro channel and micro fluid specifications. Low amplitude (1V) and very short interval DC pulse is required for effective ion uptake. In addition, the saw tooth micro electrode having the electrode gap of 10 µm for effective ion uptake. It also observed that micro channel height does not effect the ion uptake and the ion uptake inversely proportional with channel resistances and maximum value is obtained when channel resistances is 10 MΩ. These analytical results are independent with nature of pulse, geometry of electrode and micro-channel. In present study it is explored that the width of electrode in micro channel has no effect on cell ion uptake because they are placed in the sidewall of micro channel.

In brief it is conclude that osteo ion uptake can be externally controlled by short impulse electrical stimuli. In future the researcher could be think about the design and fabrication of 3D bi-layer micro bio chip for more effective in osteo ion uptake which would be widely used in drug delivery system.

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References