

The Mechanism and Properties of Electron Transfer in the Protein Molecules

Pang Xiao-Feng*

Institute of Life Science and Technology, University of Electronic Science and Technology of China, Chengdu, China

Abstract

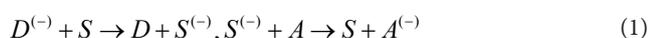
The mechanism and properties of electron transfer along protein molecules at finite temperature $T \neq 0$ in the life systems are studied using nonlinear theory of bio-energy transport and Green function method, in which the electrons are transferred from donors to acceptors in virtue of the supersound soliton excited the energy released in ATP hydrolysis. The electron transfer is, in essence, a process of oxidation-reduction reaction. In this study we first give the Hamiltonian and wave function of the system and find out the soliton solution of the dynamical equation in the protein molecules with finite temperature, and obtain the dynamical coefficient of the electron transfer. The results show that the speed of the electron transfer is related to the amplitude and velocity of the soliton, the electron's distribution in the donor and acceptor as well as the interaction among them. The stronger the coupling between them, then the larger the speed of electron transfer. We finally gain the changed rule of electric current arising from the electron transfer with varying time. These results are useful in molecular and chemical biology.

Keywords: Electron transfer; Soliton; Protein molecules; Non-linear theory; Donor; Acceptor; Dynamical coefficient

PACS Numbers: 76.80.+y; 33.40.-e; 71.38.+1; 03.40.kf

Introduction

Biological experiments show that there are a great number of electrons or charges transfer in the biological tissues and processes, such as the mitochondria, chloroplasts and chromatophores, the conduction of the nerve impulse, etc. [1,2]. As known, within the mitochondria a series of chemical transformations, called the citric acid (or Krebs) cycle, breaks down the carbon chain of glucose to carbon dioxide and produces nicotinamide adenine dinucleotide (NAD⁺) plus a proton (H⁺) and two electrons (2e⁻). These two electrons make three trips across a region off intrinsic membrane protein, carrying two protons inside the mitochondrion to outside on each pass. The dynamics of the two electrons (2e⁻) through the region of intrinsic membrane protein is of primary interest. This phenomenon shows that there is really an electron or proton transfer chains in the mitochondria, which are combined in a highly organized complex of protein molecules, the latter form the part of membrane of mitochondria. As a matter of fact, the process of the electron transfer occurs along the respiratory chain in its inner membranes of the mitochondria. The electron transfer can be carried out through different mechanisms and forms, such as the tunneling transfer of electrons and the electron transport over large distances in virtue of protein molecules [3-5]. However, there are always the donors and acceptors of the electrons and their carriers in the transfer process of large distances in virtue of protein molecules. In this model the electrons are transferred by the exciton or soliton in protein molecules, i.e., when the exciton is formed as soliton through deformation of chain, then electrons in donors are also attached on the soliton through the interaction between the donor and soliton and move further following the motion of the soliton along the molecular chains. Once the soliton meets and acts with the acceptors, the electrons are transferred to the acceptors from the soliton and attached on the surface of the acceptor. This process can be represented by



Therefore, the electron transfer is, in essence, a process of oxidation-reduction reaction. In this process the protein molecules play the bridge role of transferring the electrons in the life bodies.

Many scientists studied the electron transfer in different systems using different methods [6-9], for example, Davydov et al studied the electron and excitons in nonlinear molecular chains by a soliton theory [6], Sataric and Zakula; Sataric et al. [7,8] studied the electron transfer along the quasi-one-dimensional molecular structure by Davydov soliton model, Goldman [9] studied the long-range electron transfer in protein by a renormalized-perturbation-expansion approach. In this paper we will study the properties of the electron transfer in the protein molecules by Pang's soliton model [10-33], in which we think the electron transfer in protein molecules is carried out in virtue of the following mechanism. When the soliton is formed in the protein molecules with finite temperature under action of energy released in ATP hydrolysis, the deformation of the protein molecules occurs, then the electrons can be adhered on the soliton through an attracted interaction between them and moves towards the acceptor to accompany the motion of the soliton along the protein molecular chains. When they approach the acceptors, the electrons are transported to the acceptors due to the interaction between the electrons and acceptors. Thus the electrons are transferred to the acceptors from the donors in virtue of the soliton. Our studies are described as follows.

Methods and Results

The Hamiltonian and wave function of the system and its soliton solution of dynamical equation

Based on the above mechanism of the electron transfer in protein molecules proposed by us we can give the Hamiltonian of the great system, which is composed of protein molecules, donor, acceptor and electron, in Pang's model [9-33], which is as follows:

*Corresponding author: Pang Xiao-Feng, Institute of Life Science and Technology, University of Electronic Science and Technology of China, Chengdu 610054, China, Tel: +862883202316; Fax: +862883208238; E-mail: pangxf2006@aliyun.com

Received June 27, 2017; Accepted August 02, 2017; Published August 07, 2017

Citation: Xiao-Feng P (2017) The Mechanism and Properties of Electron Transfer in the Protein Molecules. J Proteomics Bioinform 10: 193-197. doi: 10.4172/jpb.1000440

Copyright: © 2017 Xiao-Feng P. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

$$H = H_0^{ex-ph} + H(A, D) + H_{int} \quad (2)$$

Where

$$H_0^{ex-ph} = H_{ex} + H_{ph} + H_{int} = \sum_n \{ \epsilon_0 B_n^+ B_n - J(B_n^+ B_{n+1} + B_{n+1}^+ B_n) \} + \left[\frac{P_n}{2M} + \frac{1}{2} \lambda_1 (u_n - u_{n-1})^2 - \frac{1}{3} \lambda_2 (u_n - u_{n-1})^3 \right] + \sum_n [\chi_1 (u_n - u_{n-1}) B_n^+ B_n + \chi_2 (u_n - u_{n-1}) (B_{n+1}^+ B_n B_n^+ B_{n+1})] \quad (3)$$

It describes the motions of the exciton and phonon and their interaction in Pang's model. The Hamiltonian of the donor and acceptor is denoted as:

$$H(A, D) = \sum_i \epsilon_A A_i^+ A_i + \sum_m \epsilon_D D_m^+ D_m + \sum_{i\delta} \hbar \omega_{i\delta} a_{i\delta}^+ a_{i\delta} + \sum_{lm} \hbar \omega_{lm} d_{lm}^+ d_{lm} \quad (4)$$

Where D_m^+ (D_m) and A_m^+ (A_m) are the creative and annihilation operator of the electron in the donor with the energy ϵ_A and the electron in the acceptor with the energy ϵ_D , respectively. $a_{i\delta}^+$ ($a_{i\delta}$) and d_{lm}^+ (d_{lm}) the creative and annihilation operator of the Boson in the donor with the energy $\hbar \omega_{i\delta}$ and the electron in the acceptor with the energy of $\hbar \omega_{lm}$ arising from the excitation of vibration, respectively.

$$H_{int} = \sum_{n\delta i} [V_{in}^{(\delta)} B_n^+ A_i a_{i\delta} + V_{in}^{(\delta)*} A_i^+ B_n a_{i\delta}^+] + \sum_{nmil} [W_{mn}^{(l)} B_n^+ D_m d_{lm} + W_{mn}^{(l)*} D_m^+ B_n d_{lm}^+] + \sum_{n\delta im} [Y_{im} a_{i\delta}^+ B_n^+ A_i^+ D_m + Y_{im}^* D_m^+ A_i^+ B_n a_{i\delta}] + \sum_{n\delta il} [\hbar \bar{\omega}_{mn} a_{i\delta}^+ A_i^+ D_m d_{lm} + \hbar \bar{\omega}^* d_{lm}^+ D_m^+ A_i a_{i\delta}] \quad (5)$$

Where $V_{in}^{(\delta)}$ is the matrix element of interaction between the exciton and vibrational excitation (l) of the acceptor at site i , l is the matrix element of interaction between the exciton and vibrational excitation (l) of the donor at site m , they have a maximum when,

$$V_{in}^{(\delta)} = V_0^{(\delta)} \delta_{in} \quad \text{and} \quad W_{mn}^{(l)} = W_0^{(l)} \delta_{mn} \quad (6)$$

Y_{im} is the matrix element of interaction between the exciton and electron in the electron migration from the donor to acceptor.

As it is known, there are still the coherent features of collective excitations of the exciton and phonon arising from the energy released in ATP hydrolysis in the protein molecules, although the donors and acceptors exist in this system, which are very small. Thus the wave function of the system containing small donors, acceptors and electrons can still be represented by:

$$|\Phi(t)\rangle \gg |\varphi(t)\rangle |\alpha(t)\rangle \gg \frac{1}{\lambda} \left[1 + \sum_n \varphi_n(t) B_n^+ + \frac{1}{2!} (\sum_n \varphi_n(t) B_n^+)^2 \right] |0\rangle_{ex} \times \exp \left\{ (1/N) \sum_{nq} [\alpha_{nq}(t) a_q - \alpha_{nq}^*(t) a_q^+] \right\} \prod_q (v_q')^{-1/2} (a_q^+)^{v_q'} |0\rangle_{ph} \quad (7)$$

Where $|v\rangle \gg \prod_q (v_q'!)^{-1/2} (a_q^+)^{v_q'} |0\rangle_{ph}$

Is the phononic complete set which represents the elementary excitation state of single phonon due to the finite temperature $T \neq 0$. In this meanwhile, we here used the following relations:

$$R_n = \sum_q (\hbar / 2MN\omega_q)^{1/2} (a_q + a_{-q}^+) e^{im\omega_q}, P_n = i \sum_q (M\hbar\omega_q / 2M)^{1/2} (a_{-q}^+ - a_q) e^{im\omega_q}, i = \sqrt{-1} \quad (8)$$

where $\omega_q = 2(W/M)^{1/2} \sin(r_0 q/2)$ is the frequency of a phonon with wave vector q , N is the number of amino acid in the molecular chain, r_0 is the distance between two amino acids, a_q (a_q^+) is the annihilation

(creation) operators of phonon.

$$\text{From equations (2)-(6) and } i\hbar \frac{\partial \varphi_n(t)}{\partial t} = \frac{\partial \bar{H}}{\partial \varphi_n^*(t)} \quad \text{and} \quad \frac{\partial \alpha_q(t)}{\partial t} = \frac{\partial \bar{H}}{\partial \alpha_q^*(t)}$$

(here $\bar{H} = \langle \Phi(t) | H | \Phi(t) \rangle$). In continuity approximation and in one dimensional case [6-12] we can obtain:

$$i\hbar \frac{\partial \varphi_n(t)}{\partial t} = (\epsilon_0 - 2JB(T))\varphi(x, t) - Jr_0^2 B(T) \frac{\partial \varphi(x, t)}{\partial x} - \frac{2(\chi_1 + \chi_2)}{\partial x} \frac{\partial Q(x, t)}{\partial x} \varphi(x, t) \quad (9)$$

$$\left. \frac{\partial^2 Q(x, t)}{\partial x^2} - v_0^2 \frac{\partial^2 Q(x, t)}{\partial t^2} - \frac{v_0^2 r_0^2}{12} \frac{\partial^4 Q(x, t)}{\partial x^4} = \frac{r_0(\chi_1 + \chi_2)}{M} \frac{\partial}{\partial x} |\varphi(x, t)|^2 + \frac{\lambda_1 r_0^3}{3M} \frac{\partial}{\partial x} \left| \frac{\partial Q(x, t)}{\partial x} \right| \right\} \quad (10)$$

Where $Q(x, t) = -\frac{\partial}{\partial x} \langle \Phi(t) | u(x, t) | \Phi(t) \rangle$,

$$B(T) = \prod_q \exp \{ -2cth(\hbar \omega_q / k_B T) |\alpha_{nq}|^2 \sin(r_0 q / 2) \}$$

Using an approximate method we can obtain the solutions of equations (8 and 9) as follows:

$$Q(x, t) \approx \frac{3M(v'^2 - v_0^2)}{2\lambda_1} \sec h^2 [v'(x - vt)], (v > v_0, v' = \frac{1}{r_0} (\frac{v^2}{2v_0^2} - \frac{1}{2})) \quad (11)$$

$$\varphi(x, t) = A'(T) \sec h [v'(x - x_0 - vt) \exp \{ i[\bar{k}x - \omega_{sol}(t)] \}], \bar{k} = m^* v / \hbar, \quad (12)$$

Where $A'(T) = (4W_0 m^*(T) / \hbar^2 v^2)^{1/2}$, $m^*(T) = 2\hbar^2 / JB(T)r_0^2$. We can find out the solutions of Eqs. (8 and 9) in the case of in initial condition of $Q^{(0)}(\varphi) = A\varphi$ using the iterative method [6-12], which can be represented by:

$$Q(x, t) = \frac{6v'}{\rho} \sec h^2 [v'(x - x_0 - vt)], (v > v_0), (\rho = \frac{4(\chi_1 + \chi_2)}{Jr_0 B(T)}) \quad (13)$$

$$\varphi(x, t) = (3v' / 4)^{1/2} \sec h [k'(x - x_0 - vt) \exp \{ i[\bar{k}'(x - x_0) - \omega_{sol}(t)] \}], \quad (14)$$

Where $(\bar{k}' = \hbar v' / 2Jr_0^2, k' = 2(6^{-1/2} A\rho^{2/3})$. Clearly, the above soliton solutions in equations (12) and (14) are the supersound solitons and stable, which thus can serve as the carrier of the electron transfer in living systems.

The dynamical coefficient of electron transfer and its properties

We now calculate ratio of the electron transfer from the donor to acceptor by virtue of the above supersound solitons. In the system of electron transfer the number operators of the soliton, donor and acceptor are denoted by:

$$N(B_n) = \sum_n B_n^+ B_n, N(A_i) = \sum_i A_i^+ A_i, N(D_m) = \sum_m D_m^+ D_m$$

respectively. Obviously, whole particle number $N = N(B_n) + N(A_i) + N(D_m)$, which is related to Hamiltonian of the system in Eq. (2), is conservative, i.e.,

$$i\hbar \dot{N} = [N, H] = 0$$

These number operators satisfy the following Haisenberg equations.

$$i\hbar \dot{N}_{k'} = [N_{k'}, H], (k' = B_n, A_i, D_m) \quad (15)$$

Using Eq. (2) we can obtain:

$$i\hbar \dot{N}(B) = \sum_{\delta ni} [V_{in}^\delta B_n^+ A_i a_{i\delta} - V_{in}^{\delta*} a_{i\delta}^+ A_i^+ B_n] + \sum_{imm} [W_{mn}^{l*} B_n^+ D_m d_{lm} - W_{mn}^l d_{lm}^+ D_m^+ B_n]$$

$$i\hbar \dot{N}(A) = \sum_{\delta ni} [V_{in}^{\delta*} a_{i\delta}^+ A_i^+ B_n - V_{in}^\delta B_n^+ A_i a_{i\delta}]$$

$$i\hbar \dot{N}(D) = \sum_{imm} [W_{mn}^{I*} d_{im}^+ D_m^+ B_n - W_{mn}^I B_n^+ D_m d_{im}^-] \quad (16)$$

In this system of electron transfer the number currents formed are in equilibrium state and satisfy the following relationship.

$$\dot{N}(B) = -[\dot{N}(A) + \dot{N}(D)] \quad (17)$$

Based on this feature we can use the statistic theory of quasi-equilibrium state established by Zubarev [34] to study the electron transfer. Corresponding statistic operator of the quasi-equilibrium state can be represented by:

$$\hat{\rho} = \frac{1}{2} \exp\{-\bar{\beta}[H - \sum_{a=1}^3 \mu_a N_a + \sum_{a=1}^3 \int_{-\infty}^0 e^{\varepsilon t} \dot{N}_a dt]\} = \frac{1}{2} \exp(-\hat{M} + \delta M) \quad (18)$$

Where

$$\hat{M} = \bar{\beta}(H - \sum_{a=1}^3 \mu_a N_a), \delta \hat{M} = \bar{\beta}[\mathfrak{R}_{AB} \int_{-\infty}^0 dt e^{\varepsilon t} \dot{N}(A_i) + \mathfrak{R}_{DB} \int_{-\infty}^0 dt e^{\varepsilon t} \dot{N}(D_m)], \bar{\beta} = 1 / K_B T$$

Z is statistic sum of the system, μ_a is the chemical potential of ath component. ε is a small parameter, \mathfrak{R}_{AB} and \mathfrak{R}_{DB} denote the chemical affinity in the chemical reaction in Eq.(1), their relationship with chemical potential are as follows:

$$\mathfrak{R}_{AB} = -(\mu_A - \mu_B), \mathfrak{R}_{DB} = -(\mu_D - \mu_B) \quad (19)$$

Since $\delta \hat{M}$ is small and the request of normalization, i.e., $SP(\hat{\rho}) = 1$, then Eq. (10) can express as:

$$\hat{\rho} = [1 - \int_0^1 d\tau e^{\hat{M}\tau} \delta \hat{M} e^{-\hat{M}\tau} - \int_0^1 d\tau \langle e^{-\hat{M}\tau} \delta M e^{\hat{M}\tau} \rangle_q] \rho_q \quad (20)$$

where $\hat{\rho}_q$ is a localized equilibrium density matrix, which can be denoted by:

$$\hat{\rho}_q = e^{-\hat{M}} / Sp(e^{-\hat{M}}) \quad (21)$$

Then the number current of acceptor can be expressed by

$$\langle \dot{N}(A) \rangle = sp(\dot{N}(A) \hat{\rho}_q), \text{ thus we yield.}$$

$$\langle \dot{N}(A) \rangle = \langle \dot{N}(A) \rangle_q + \int_0^1 d\tau \langle \dot{N}(A) e^{\hat{M}\tau} \delta \hat{M} e^{-\hat{M}\tau} \rangle_q - \langle \dot{N}(A) e^{-\hat{M}\tau} \delta M e^{\hat{M}\tau} \rangle_q \quad (22)$$

There is the relation of $\langle \dot{N}(A) \rangle = 0$ in the localized equilibrium state without dissipation, then the number current of acceptor can be expressed by:

$$\langle \dot{N}(A) \rangle = \bar{\beta} \mathfrak{R}_{AB} Q(\dot{N}(A), \dot{N}(A)) + \bar{\beta} \mathfrak{R}_{DB} Q(\dot{N}(A), \dot{N}(D)) \quad (23)$$

Where the dynamic coefficients in this process are of the forms:

$$Q(\dot{N}(A), \dot{N}(A)) = \int_{-\infty}^0 dt e^{\varepsilon t} \int_0^1 d\tau \langle \dot{N}(A) e^{-\hat{M}\tau} \dot{N}(A) e^{\hat{M}\tau} \rangle_q \quad (24)$$

$$Q(\dot{N}(A), \dot{N}(D)) = \int_{-\infty}^0 dt e^{\varepsilon t} \int_0^1 d\tau \langle \dot{N}(A) e^{-\hat{M}\tau} \dot{N}(D) e^{\hat{M}\tau} \rangle_q \quad (25)$$

These coefficients characterize the sizes of change of particles and features of particle current formed, respectively. They represent the number of particles of transformation in unit time in the process of electron transfer. If the quadric terms in Eq.(2) are only considered, the operator \hat{M} can represent as

$$\hat{M} \approx M_{eff} = \bar{\beta}(H - \sum_a \mu_a N_a)_{eff} = \bar{\beta}[\sum_n (\varepsilon_n - \mu_a) B_n^+ B_n + \sum_i (\varepsilon_A - \mu_A) A_i^+ A_i + \sum_m (\varepsilon_D - \mu_D) D_m^+ D_m + \sum_{\delta i} \hbar \omega_{\delta i} a_{\delta i}^+ a_{\delta i} + \sum_{lm} \hbar \omega_{lm} d_{lm}^+ d_{lm}] \quad (26)$$

Utilizing Eq. (26) and separating the functions related to τ and

completing these integrations in it then we denote Eq. (24) as:

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{1}{(i\hbar)^2} \sum_{\delta m \delta' n'} \frac{V_{in}^{(\delta)*} V_{in'}^{(\delta')}}{\beta E_{\delta}} (e^{-\beta E_{\delta}} - 1) \int_{-\infty}^t dt e^{\varepsilon t} \langle a_{\delta i}^+ A_i^+ B_n | B_n^+(t) A_i(t) a_{\delta' i'}(t) \rangle_q - \frac{1}{(i\hbar)^2} \sum_{\delta m \delta' n'} \frac{V_{in}^{(\delta)*} V_{in'}^{(\delta')}}{\beta E_{\delta}} (e^{-\beta E_{\delta}} - 1) \int_{-\infty}^t dt \langle B_n^+ A_i a_{\delta i} | a_{\delta' i'}^+(t) B_n^+(t) A_i(t) \rangle_q \quad (27)$$

Where we used the following relationships:

$$e^{\pm \hat{M}_{eff}} (B_n^+ A_i a_{\delta i}) e^{\mp \hat{M}_{eff}} = B_n^+ A_i a_{\delta i} e^{\pm \beta E_{\delta}}, e^{\pm \hat{M}_{eff}} (a_{\delta i}^+ A_i^+ B_n) e^{\mp \hat{M}_{eff}} = a_{\delta i}^+ A_i^+ B_n e^{\pm \beta E_{\delta}}$$

$$e^{-\beta E_{\delta}} \langle a_{\delta i}^+ A_i^+ B_n | B_n^+(t) A_i(t) a_{\delta' i'}(t) \rangle_q = \langle B_n^+(t) A_i(t) a_{\delta' i'}(t) a_{\delta i}^+ A_i^+ B_n \rangle_q$$

$$e^{\beta E_{\delta}} \langle B_n^+ A_i a_{\delta i} | a_{\delta' i'}^+(t) A_i(t) B_n^+(t) \rangle_q = \langle a_{\delta' i'}^+(t) A_i(t) B_n^+(t) B_n^+ A_i a_{\delta i} \rangle_q,$$

$$E_{\delta} = \Delta - \varepsilon_A - \hbar \omega_{\delta n} - \mu_B + \mu_A$$

These dynamical coefficients can become the following Onsager representations in virtue of Boson postponed Green function [6-7,34].

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{1}{(i\hbar)^2} \sum_{\delta m \delta' n'} \frac{V_{in}^{(\delta)*} V_{in'}^{(\delta')}}{\beta E_{\delta}} \int_{-\infty}^t dt e^{\varepsilon t} \langle a_{\delta i}^+ A_i^+ B_n | B_n^+(t) A_i(t) a_{\delta' i'}(t) \rangle^{ret} + C.C \quad (28)$$

where

$$\langle a_{\delta i}^+ A_i^+ B_n | B_n^+(t) A_i(t) a_{\delta' i'}(t) \rangle^{ret} = \frac{\mathcal{G}(-t)}{i\hbar} a_{\delta i}^+ A_i^+ B_n \langle B_n^+(t) A_i(t) a_{\delta' i'}(t) \rangle_q$$

where the step function $Q(\dot{N}(A), \dot{N}(A))$ 1 (if $t < 0$), or 0 (if $t > 0$).

Because the dynamical coefficient $Q(\dot{N}(A), \dot{N}(A))$ contains odd Fermi operators, thus its average is zero.

In order to find out the explicit representation of $Q(\dot{N}(A), \dot{N}(A))$ we must calculate the Green function of three particles as above mentioned. We here denote approximately it by Green function of signal particle. Since $H(A,D)$ is only related to squares of A_i and $a_{\delta i}$, then the following equations hold.

$$A_i(t) = e^{iHt/\hbar} A_i(0) e^{-iHt/\hbar} = e^{-i\varepsilon_A t/\hbar} A_i(0), A_i^+(t) = e^{i\varepsilon_A t/\hbar} A_i^+(0)$$

$$a_{i\delta}(t) = e^{-i\hbar\omega_{i\delta} t} a_{i\delta}(0), a_{i\delta}^+(t) = e^{i\hbar\omega_{i\delta} t} a_{i\delta}^+(0)$$

Utilizing these relationships, then Equation (28) can be expressed by the Green function of signal particle for the Boson operator B_n of the exciton, which is as follows:

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{1}{(i\hbar)^2} \sum_{\delta m \delta' n'} \frac{V_{in}^{(\delta)*} V_{in'}^{(\delta')}}{\beta E_{\delta}} \delta_{ii'} \delta_{\delta\delta'} \int_{-\infty}^t dt \exp[\varepsilon t - i(\frac{\varepsilon_A}{\hbar} + \omega_{i\delta})t] \times \langle B_n(o) | B_n^+(t) \bar{N}_i(A) \bar{n}_{i\delta}(a) + C.C \quad (29)$$

$$\text{Where } \bar{n}_{i\delta}(a) = \{\exp[(\beta \hbar \omega_{i\delta}) - 1]\}^{-1}, \bar{n}_{i\delta}(a) = \{\exp[(\beta \hbar \omega_{i\delta}) - 1]\}^{-1}.$$

We now study the roles of the above supersound soliton in the process of electron transfer. In this case, let the above Green function denotes as:

$$\langle B_n(o) | B_n^+(t) \rangle^{ret} = \frac{\mathcal{G}(-t)}{i\hbar} \langle [B_n(o), B_n^+(t)] \rangle_{coh}$$

For the coherent wave function in Eq.(7) the Boson operator $B_n(t)$ has the feature.

$$B_n(t) | \varphi_n \rangle = \varphi_n | \varphi_n \rangle$$

Applying these features and Wojtezak's method [35] and further considering the influence of temperature of the system, then the Green function of signal particle can be found out, which is:

$$\langle B_n(o) | B_n^+(t) \rangle = \frac{\mathcal{G}(-t)}{i\hbar} \varphi_n(0) \varphi_n^*(t) \exp[-\bar{\beta}(\varepsilon_0 - \mu_B)]$$

Thus, Eq. (29) can represent as:

$$Q(\dot{N}(A), \dot{N}(A)) = \sum_{\delta_{in}} \frac{V_{in}^{(\delta)} V_{in}^{(\delta)*}}{\beta E_{\delta}} \int_{-\infty}^t dt \exp[\epsilon t - i(\frac{\epsilon_A}{\hbar} + \omega_{i\delta})t] \frac{g(-t)}{\hbar^2} \varphi_n(0) \varphi_n^*(t) \bar{N}_i \bar{n}_{i\delta} e^{-\beta(\epsilon_0 - \mu_B)} \quad (30)$$

Where $\varphi_n(0)$ and $\varphi_n^*(t)$ are the amplitudes of the supersound soliton in Eqs. (12 and 14). Inserting Eq. (12) into Eq. (30) we can obtain.

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{2A^2(T)}{\hbar^2 \beta} \sum_{\delta_i} \frac{(V_0^{(\delta)})^2 \bar{N}_i \bar{n}_{i\delta}}{E_{\delta} \cosh^2[v'(X - X_0)]} \int_{-\infty}^0 dt \frac{\cos \Omega t e^{-\beta(\epsilon_0 - \mu_B) + \epsilon t}}{\cosh^2[v'(X - X_0 - vt / r_0)]} \quad (31)$$

Where $X=x/r_0$, $X_0=x_0/r_0$, $\Omega = \omega_{sol} - \omega_{i\delta} - \epsilon_A / \hbar$.

We now find out the integration of t in Eq. (31), which is:

$$g(t) = \int_{-\infty}^0 dt \frac{\cos \Omega t e^{-\beta(\epsilon_0 - \mu_B) + \epsilon t}}{\cosh^2[v'(X - X_0 - vt / r_0)]} = \frac{\pi \Omega r_0^2}{2v'v^2} \frac{1}{\cosh^2[v'(X - X_0)] \sinh(\frac{\pi \Omega r_0}{2v'v})} \times [1 - 2th[v'(X - X_0)] \frac{v'v}{\pi \Omega r_0} - \frac{\pi \Omega r_0^2}{v'v} th[\frac{\pi \Omega r_0}{2v'v} - \frac{\pi \Omega^2 r_0^2}{v'^2 v^2} B_2] + th^2[v'(X - X_0)] (1 - \frac{\pi \Omega^2 r_0^2}{v'^2 v^2})]$$

Where B_2 is Bernoolli number. Then the above dynamic coefficient can finally denote as:

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{A^2(T) \pi \Omega r_0^2}{\hbar^2 \beta v'^2 v^2} \sum_{\delta_i} \frac{(V_0^{(\delta)})^2 e^{-\beta(\epsilon_0 - \mu_B)} \bar{N}_i \bar{n}_{i\delta}}{E_{\delta} [e^{-\beta(\epsilon_0 - \mu_B)} + 1] [e^{-\beta \hbar \omega_{i\delta}} - 1] \cosh^4[v'(X - X_0)]} \times [1 - 2th[v'(X - X_0)] \frac{v'v}{\pi \Omega r_0} - \frac{\pi \Omega r_0^2}{v'v} th[\frac{\pi \Omega r_0}{2v'v} - \frac{\pi \Omega^2 r_0^2}{v'^2 v^2} B_2] + th^2[v'(X - X_0)] (1 - \frac{\pi \Omega^2 r_0^2}{v'^2 v^2})] \quad (32)$$

Equation (32) is just the dynamical coefficient of electron transfer along the protein molecules by the supersound soliton in Eq. (10). Obviously, the speed of the electron transfer is related to the amplitude and velocity of the soliton, the electron's distribution in the donor and acceptor as well as the interaction among the soliton, donor and acceptor. In general, the stronger the coupling between them, then the larger the speed of electron transfer because the latter is directly proportional to the square of the interaction potential $V_0^{(\delta)}$. This is corresponded with practical case and reasonable. Therefore, the above result is correct. In order to exhibit clearly the features of the electron transfer we now study some special situations.

Discussion

1. The features of the electron transfer in the case of higher concentration of donor and acceptor. In this case $v'_D + v'_A = N$. This means that \bar{N}_i , $\bar{n}_{i\delta}$ and δ are not related to i , $\delta = 1$ and the sum, $\int_{-\infty}^{\infty} dz$, can be replaced by the integration $\int_{-\infty}^{\infty} dz$. Thus we can obtain from Eq. (32)

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{(V_0^{(\delta)})^2 \bar{N}_i \bar{n}_{i\delta} \pi \Omega r_0^2 e^{-\beta(\epsilon_0 - \mu_B)}}{2\hbar^2 A^2(T) \beta v'^3 v^2 E_{\delta} \sinh(\frac{\pi \Omega r_0}{2v'v})} \quad (33)$$

This shows clearly that the dynamic coefficient is also directly proportional to the square of the interaction potential $V_0^{(\delta)}$ and decreased with increasing the velocity and amplitude of the soliton. This means that the speed of electron transfer by larger and fast soliton is small than that by small and slow soliton in this case.

If we further take account of this case of $\pi \Omega r_0 \ll 2v'v$, then Eq.

(32) becomes as:

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{(V_0^{(\delta)})^2 \bar{N}_i \bar{n}_{i\delta} \pi \Omega r_0^2}{2\hbar^2 A^2(T) \beta v'^3 v^2 E_{\delta}} e^{-\beta(\epsilon_0 - \mu_B)} \quad (34)$$

Thus we know that the dynamical coefficient will increase intensely in the case $E_{\delta} \rightarrow 0$ and

$$\epsilon_0 \rightarrow \mu_B.$$

2. In the case of $v = 0$. This means that the supersound soliton is in static state. From Eq. (31) we can obtain:

$$Q(\dot{N}(A), \dot{N}(A)) = \frac{A^2(T)}{\beta} \sum_{\delta_i} \frac{U_{\delta}^{sol} \bar{N}_i(A) \bar{n}_{i\delta}(a) e^{-\beta(\epsilon_0 - \mu_B)}}{E_{\delta} (\epsilon_0 - \hbar \omega_{sol}^{(0)} - \mu_B - \epsilon_A) \cosh^4[v'(X - X_0)]} \quad (35)$$

Where

$$U_{\delta}^{sol} = \frac{2\pi}{\hbar} |V_0^{(\delta)}|^2 \delta[\hbar(\omega_{sol}^{(0)} - \omega_{i\delta}) - \epsilon_A], \hbar \omega_{sol}^{(0)} = -\hbar \omega_{i\delta} - \epsilon_A$$

If the features of dynamic coefficients among Eqs. (31, 32 and 35) are compared we can find that the dynamic coefficient in the case of $v=0$ is larger than those in other cases. This resemble the electron transfer by the bell-type magnetic-soliton and the result of transfer speed of energy of ferromagnetic resonant in the ferromagnet obtained by Wojtezak and Sukiennicki [35].

Otherwise, we can also obtain the dynamic coefficient of donor, $Q(\dot{N}(A), \dot{N}(D))$, if only the parameters of the acceptor in Eqs. (31-35) are replaced by corresponding parameters of the donor. However, to find representation of $Q(\dot{N}(A), \dot{N}(D))$ is difficulty. We must again add the interaction between the acceptor and donor, which is $H_{int}^{A-D} = \sum_{i\delta lm} V_{i\delta lm} A_{i\delta}^+ D_{lm} a_{i\delta}^+ d_{lm} + C.C$, into the above Hamiltonian. Then its calculation is complicated, which is studied in other paper.

The relaxation time of the electron transfer, which denotes the size of speed of electron transfer from the donor to the acceptor, is an inverse measure of the dynamical coefficient. Thus it can be represented by $\bar{\tau} = constant.1 / Q(\dot{N}(A), \dot{N}(A))$. Using Eq. (35) we can obtain.

$$\bar{\tau} = constant. \frac{2\hbar^2 A^2(T) \beta v'^3 v^2 E_{\delta} \sinh(\frac{\pi \Omega r_0}{2v'v})}{(V_0^{(\delta)})^2 \bar{N}_i \bar{n}_{i\delta} \pi \Omega r_0^2 e^{-\beta(\epsilon_0 - \mu_B)}} \quad (36)$$

Then the electric current formed in the electron transfer process in the protein molecule can be represented by:

$$\langle \dot{N}_A \rangle = \langle \dot{N}_A^0 \rangle \exp[-t / \tau] \quad (37)$$

This representation is very useful in molecular and chemical biology.

Conclusion

In this paper we studied the mechanism and properties of electron transfer along protein molecules with finite temperature $T \neq 0$ in the life systems using nonlinear theory of bio-energy transport and Green function method. The mechanism of the electron transfer can be described as follows. When the supersound soliton is formed under action of energy released in ATP hydrolysis, in which deformation of protein molecules occurs, the electrons are adhered on the soliton through an attracted interaction between them and moves towards the acceptor to follow the motion of the soliton along the protein molecular chains. When they approach the acceptors, the electrons are transported to the acceptors due to the interaction between the electrons and acceptors. Thus the electrons are transferred from donors to acceptors in virtue of the supersound soliton. Therefore the mechanism of the

electron transfer is, in essence, just a process of oxidation-reduction reaction. Based on this mechanism we first give the Hamiltonian and wave function of the system and find out the soliton solution of the dynamical equation in the protein molecules with finite temperature, and obtain finally the dynamical coefficient of the electron transfer and its features of transfer. The results obtained show that the speed of the electron transfer is related to the amplitude and velocity of the soliton, the electron's distribution in the donor and acceptor as well as the interaction among the soliton, donor and acceptor. In general, the stronger the coupling between them, then the larger the speed of electron transfer because the latter is directly proportional to the square of the interaction potential $V_0^{(\delta)}$. Meanwhile, we finally get the changed rule of electric current arising from the electron transfer with varying time. These results are useful in molecular and chemical biology.

Acknowledgement

The authors would like to acknowledge the National "973" project of China for financial support (Grant No: 212011CB503701).

References

- Xiao-Feng P (2007) Biophysics. The Press of University of Electronic Science & Technology of China, Chengdu, China.
- Huili C, Moushi L, Yunsong Z (1999) The structures and functions of bio macromolecules. Shanghai Press of Medical Science, Shanghai, China pp: 34-154.
- Davydov AS (1982) Biology and quantum mechanics. Pergamon, NY, USA.
- Davydov AS (1991) The solitons in molecular systems. Reidel, Dordrecht.
- Davydov AS (1982) Solitons in quasi-one-dimensional molecular structures. *Sov Phys Usp* 25: 898-917.
- Davydov AS, Zolotariuk AV (1983) Electron and excitons in nonlinear molecular chains. *Physica Scripta* 28: 249-256.
- Sataric M, Zakula R (1983) On the role of the soliton mechanism in the electron transfer along the quasi-one dimensional molecular structures. *Phys Stat Sol* 116: 617-233.
- Sataric M, Ivic Z, Zakula R (1986) The kinetic coefficient of the electron transfer along a one dimensional molecular chain achieved by the mechanism of supersonic Davydov soliton. *Physica Scripta* 34: 283-288.
- Goldman C (1991) Long-range electron transfer in protein by a renormalized-perturbation-expansion approach. *Phys Rev A* 43: 4500-4509.
- Pang XF (2000) Improvement of the Davydov theory of bioenergy transport in protein molecular systems. *Phys Rev E* 62: 6989.
- Pang XF (2001) The lifetime of the soliton in the improved Davydov model at the biological temperature 300 K for protein molecules. *European Phys J B* 19: 297-316.
- Pang XF (2001) Calculation of vibrational energy-spectra of α -helical protein molecules and its properties. *Commun Theor Phys* 35: 323.
- Pang XF (2001) The Features of Infrared Absorption of the Protein Molecules in the Living System. *Commun Theor Phys* 36: 178.
- Pang XF (2001) Vibrational energy-spectra of protein molecules and non-thermally biological effect of infrared ligh. *J Int Inf Mill Waves* 22: 291-307.
- Pang XF (2001) Quantum vibrational energy spectra of molecular chains in crystalline acetanilide. *J Phys Chem Solids* 62: 793.
- Pang XF (1999) Investigation on molecular mechanism cured sickness for infrared medical-instrument. *Chin J BioMed Eng* 8: 39.
- Pang XF (2001) The biological effect and medical functions of the infrared rays. *Chin J BioMed Eng* 10: 613.
- Pang XF, Feng YP (2005) Quantum mechanics in nonlinear systems. World Science Publishing Co, NJ, USA, pp: 471-551.
- Pang XF, Zhang HW, Yu JF, Feng YP (2005) States and properties of the soliton transported bio-energy in nonuniform protein molecules at physiological temperature. *Phys Lett A* 335: 408.
- Pang XF, Luo YH (2004) Stabilization of the soliton transported bio-energy in protein molecules in the improved model. *Commun Theor Phys* 41: 470.
- Pang XF, Yu JF, Luo YH (2005) Influences of quantum and disorder effects on solitons excited in protein molecules in improved model. *Commun Theor Phys* 43: 367.
- Pang XF, Zhang HW (2005) Changes of the Mössbauer effect caused by the excitation of the solitons in the organic molecular crystals at finite temperature. *J Phys Chem Solids* 66: 963-972.
- Pang XF, Zhang HW, Yu JF, Luo YH (2005) Thermal stability of the new soliton transported bio-energy under influence of fluctuations of characteristic parameters at biological temperature in the protein molecules. *Int J Modern Physics B* 19: 4677-4699.
- Pang XF, Zhang HW, Yu JF (2006) The influence of the heat bath and structural disorder in protein molecules on soliton transported bio-energy in an improved model. *J Phys Condensed Matter* 18: 613-627.
- Pang XF, Zhang HW, Yu JF, Luo YH (2006) Influences of variations of characteristic parameters of protein molecules on states of soliton transported bio-energy. *Int J Modern Physics B* 20: 3027-3049.
- Pang XF, Yu JF, Lao YH (2007) Combination effects of structure nonuniformity of proteins on the soliton transported bio-energy. *Inter J Mod Phys B* 21: 13-42.
- Pang XF, Liu MJ (2007) Properties of soliton-transported bio-energy in α -helix protein molecules with three channels. *Commun Theor Phys* 48: 369-376.
- Pang XF (2008) Influence of structure disorders and temperatures of systems on the bio-energy transport in protein molecules (II). *Frontiers of Physics in China* 3: 457-488.
- Pang XF, Liu MJ (2009) Features of motion of soliton transported bio-energy in aperiodic α -helix protein molecules with three channels. *Commun Theor Phys* 51: 170-180.
- Pang XF, Yu JF, Liu MJ (2010) Changes of properties of the soliton with temperature under influences of structure disorder in the α -helix protein molecules with three channels. *Mol Phys* 108: 1297-1315.
- Pang XF (2011) The theory of bio-energy transport in the protein molecules and its properties. *Physics of Life Review* 8: 264-286.
- Pang XF (2011) Correctness and completeness of the theory of bio-energy transport. *Phys Life Rev* 8: 301-305.
- Pang XF (2012) The properties of bio energy transport and influence of structure non-uniformity and temperature of systems on energy transport along polypeptide chain. *Progress of Biophysics Mol Biol* 108: 1-49.
- Zubarev NT (1971) Non-equilibrium statistical thermodynamics (1st edn.). Nauka, Moscow, Russia pp: 261-334.
- Wojtozak L, Sukiennicki A (1982) Ferromagnetic resonance for one-dimensional magnets with solitons. *Z Phys B Condensed Matt* 47: 223-226.