

# Simulation and Optimization of a Continuous Biochemical Reactor

Ghanim M. Alwan\*

Chemical Engineering, University of Technology, Baghdad, Iraq

## Abstract

The present work focused on the dynamic and optimization of a continuous biochemical reactor using the glucose as a substrate. Simulated model provides the development of the process and reducing the risk of experimental runs. The selected process variables are; dilution rate (D), feed substrate concentration (Si), pH and temperature (T). The effect of D was observed at Si below 20 g/L. pH and T are affecting within Si of 60 g/L. Si is the effective process variable on the dynamic characteristics of the reactor. Reasonable agreement has found when compared the simulated results with that obtained by the previous work. Optimization technique guides the decision maker to select the best operating conditions. Stochastic genetic algorithm has found suitable for the nonlinear reactor. Optimal results indicate that the maximum biomass concentration (X) is 80.57 g/L at Si of 197.56 g/L and low D of 0.1 (1/hr). Si was the sensitive variable for changing of the objective X.

**Keywords:** Biochemical reactor; Dynamic model; Optimization; Simulation

**Nomenclatures:** D: Dilution rate, [1/hr]; F: Flow rate, [L/hr]; Km: Saturation constant, [g/L]; PH: Acidity [-]; r1: Rate of cell generation [g/L.hr]; r2: Rate of substrate consumption [g/L.hr]; S: Substrate concentration in the reactor [g/L]; Si: Feed substrate concentration [g/L]; T: Temperature [C°]; t: Time [hr]; V: Volume of the reactor [L]; X: Biomass concentration in the reactor [g/L]; Y: Yield [-]; Greek Symbols  $\mu_{max}$ : Maximum specific growth rate coefficient [1/hr];  $\mu(s)$ : Local specific growth rate coefficient, [1/hr]

## Introduction

Lee [1], and Kapadia et al. [2] described the concept and applications of the biochemical reactors. The stirred-tank bioreactor is one of the most commonly used types for large scale production in industrial applications such as food, pharmaceuticals, various commodity and specialty chemicals. It is used mainly in two modes: the continuous mode and the fed-batch mode. In the continuous mode, the limiting substrates are constantly added to the reactor, while the output stream is simultaneously removed at the same rate, to keep the reactor volume constant. The continuous stirred biochemical reactor is widely used in the treatment of liquid wastes. Its process kinetic can be characterized by the following reaction scheme:



Henson [3] explained that as compared to conventional chemical reactors, bioreactors present unique modeling and control challenges due to complexity of the underlying biochemical reactions.

Karadag and Puhakka [4] and Garhyan et al. [5] studied the bioreactor performance using mixed cultures influenced by several operational parameters which affect its static and dynamic behavior such as: dilution rate, feed substrate concentration pH, hydraulic retention time, organic loading rate and temperature. In particular, the role of pH seems the most important parameter in the regulation of enzymes pool production. Ruggeri et al. [6] indicated that the pH adjustments validated the dynamics of the system. Charoenchai et al. [7] concluded that the temperature is a variable that directly affects the growth rate of organisms.

Annamalai and Doble [8] had found the mathematical modeling of fermentation process helps to; elucidate the mechanism of production process, estimate kinetic parameters such as specific growth rate

of biomass and product formation rate develop the understanding between effects of operational conditions on production, and reduce laboratory experiments thereby saving time and resources.

Alhumaizi and Ajbar [9], and Shimizu [10] proved the biological processes are inherently very nonlinear and had frequently been changing optimum operating conditions. Many available mathematical models for biological reactions were not suitable for a control design since no accurate biological law had been proposed.

Kapadia et al. [2] proposed a novel robust controller for a continuous stirred biochemical reactor that controls the culture dilution rate into the reactor in order to maximize a cost function representing the biomass yield.

Genetic Algorithm (GA) is global stochastic search based on mechanics of natural selection and natural genetics. GA is based on Darwin's theory of 'survival of the fittest'. There are several genetic operators such as; selection, crossover and mutation, etc. Gupta and Srivastava [11] concluded that the deterministic algorithms for function optimization are generally limited to convex regular functions. However, many functions are either not differentiable or needed a lot of difficult mathematical treatment: decomposition, sensitivity computing, etc.

## Scope of the Work

The present work focuses on the simulation of the continuous biochemical reactor using glucose as the substrate. Study the effect of the process variables on the dynamic behavior of the reactor. The selected variables are; feed substrate concentration, dilution rate, pH and temperature. The reliable simulated model can be used to generate

\*Corresponding author: Ghanim M. Alwan, Chemical Engineering, University of Technology, Baghdad, Iraq, E-mail: [ghanim.alwan@yahoo.com](mailto:ghanim.alwan@yahoo.com)

Received September 28, 2012; Accepted November 26, 2012; Published November 28, 2012

Citation: Alwan GM (2013) Simulation and Optimization of a Continuous Biochemical Reactor. J Chem Eng Process Technol 4: 142. doi:10.4172/2157-7048.1000142

Copyright: © 2013 Alwan GM. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

the desirable data for formulating the optimization equation. The objective is to maximize the biomass concentration in the reactor. Stochastic globe genetic algorithm search will implement to select the best operating conditions of the reactor.

### Dynamic Model

Dynamic modeling for optimization and control requires models that describe the essential dynamic characteristics of the process under study. In the present work, the following assumptions have been adopted for the model:

1. Homogenous liquid-phase system.
2. Non-isothermal conditions.
3. Acidity of liquid is changed.
4. First order irreversible reaction.
5. Constant hold-up.
6. Follow the Monod law.

The component material balances for biomass(X) and substrate(S) are:

$$dX/dt = r1 - (F/V)X \tag{1}$$

$$dS/dt = (F/V) Si - (F/V) S - r2 \tag{2}$$

In addition, the reaction rate equations are:

$$r1 = \mu(s) X \tag{3}$$

$$\text{And, } Y = r1/r2 \tag{4}$$

For Monod law;

$$\mu(s) = (\mu_{max} * S) / (Km + S) \tag{5}$$

X(gm/l)	Si(gm/l)	D(hr <sup>-1</sup> )	Y(-)	μ(1/hr)
0.001	6.0	0.3	0.4	0.4

Table 1: Optimum initial operating conditions.

$$\mu_{max} = -40.5 + 11.78 pH - 0.0691 pH^2 + 1.65T + 0.003T^2 - 0.468 pH.T \tag{6}$$

Equations (1&2) can be simplified to:

$$dX/dt = (\mu(s) - D)X \tag{7}$$

$$dS/dt = D (Si - S) - (X/Y)\mu(s) \tag{8}$$

where  $D=F/V$

Equation 6 was correlated depended on the experimental data of Lopez et al. [12].

The simulated model will implement for the wastewater contains glucose with different concentrations from 6.0 to 200.0 gm/L. Temperature of water are varied from 20 to 30 °C and the acidity are from pH 2 to pH 4. The kinetic parameters of the biological reaction are; maximum specific growth rate coefficient ( $\mu_{max}=0.3 \text{ hr}^{-1}$ ), saturation constant ( $Km=1.0 \text{ g/L}$ ) and yield ( $Y=0.4$ ) regarding to Lopez et al. [12], Cutlip and Shacham [13].

### Results and Discussion

#### Optimal operating conditions

The initial optimal operating conditions of the system (Table 1) were estimated by the nonlinear Levenberg-Marquardt method with the aid of the MATLAB computer program.

#### Unsteady state conditions

The present bioreactor can be viewed as nonlinear dynamic system and the simulation is very useful tool for model validation .The unsteady- state model equation 7 and equation 8 were solved numerically using 5th order Runge-kutta method with the aid of the MATLAB program, starting from steady- state operating conditions (Table 1). Figures 1-7 explain the behaviors of the biochemical process under different values of variables; dilution rate (D), feed substrate concentration (Si) at operating conditions of pH 2-4 and temperature of 20-30°C.

Dynamically, the system behaves as the first- order lag system. The

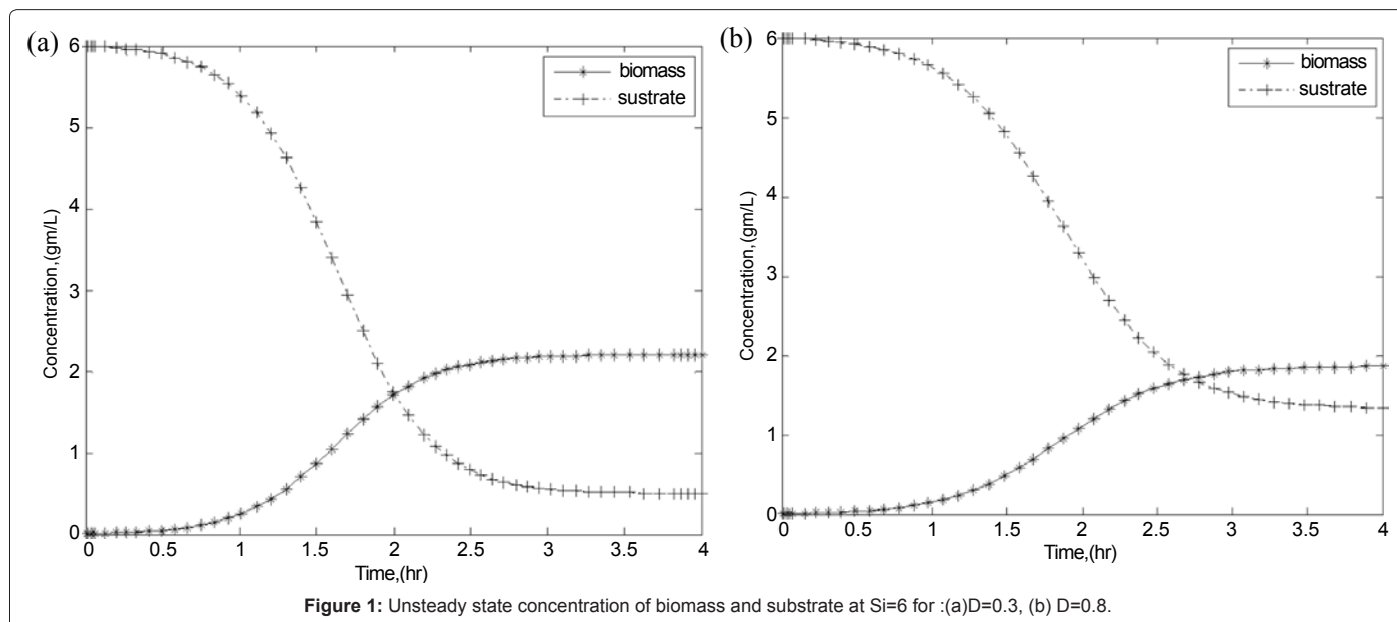
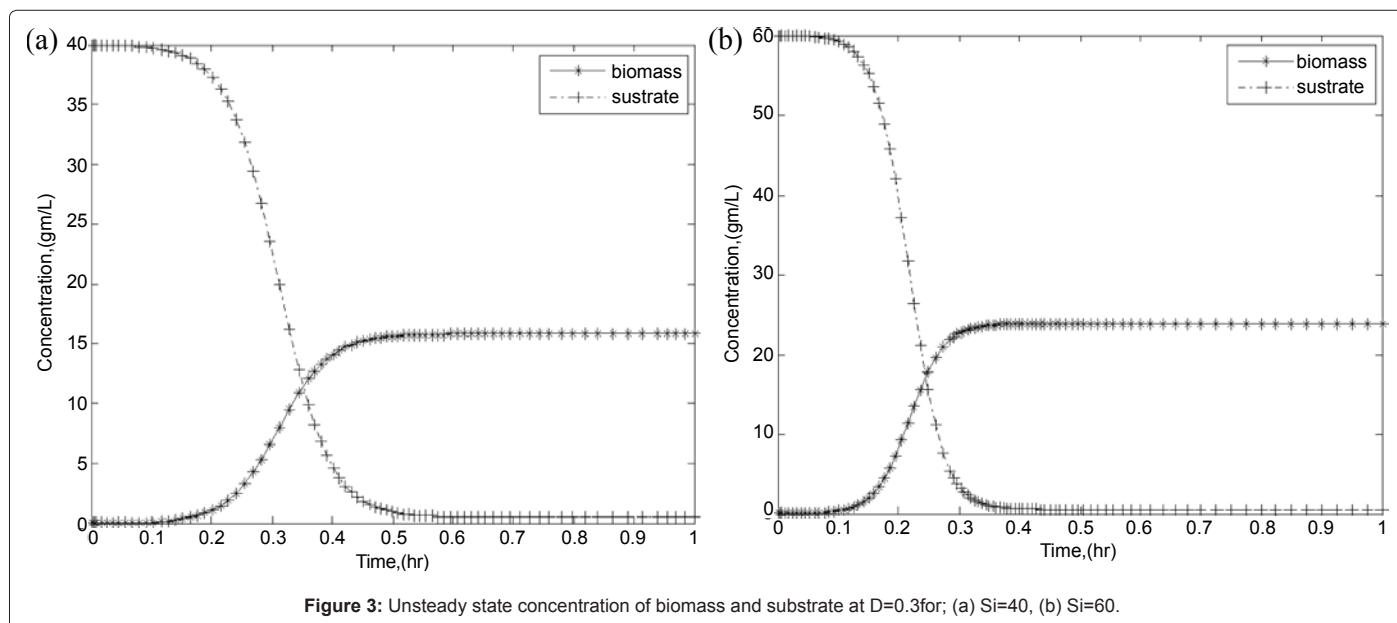
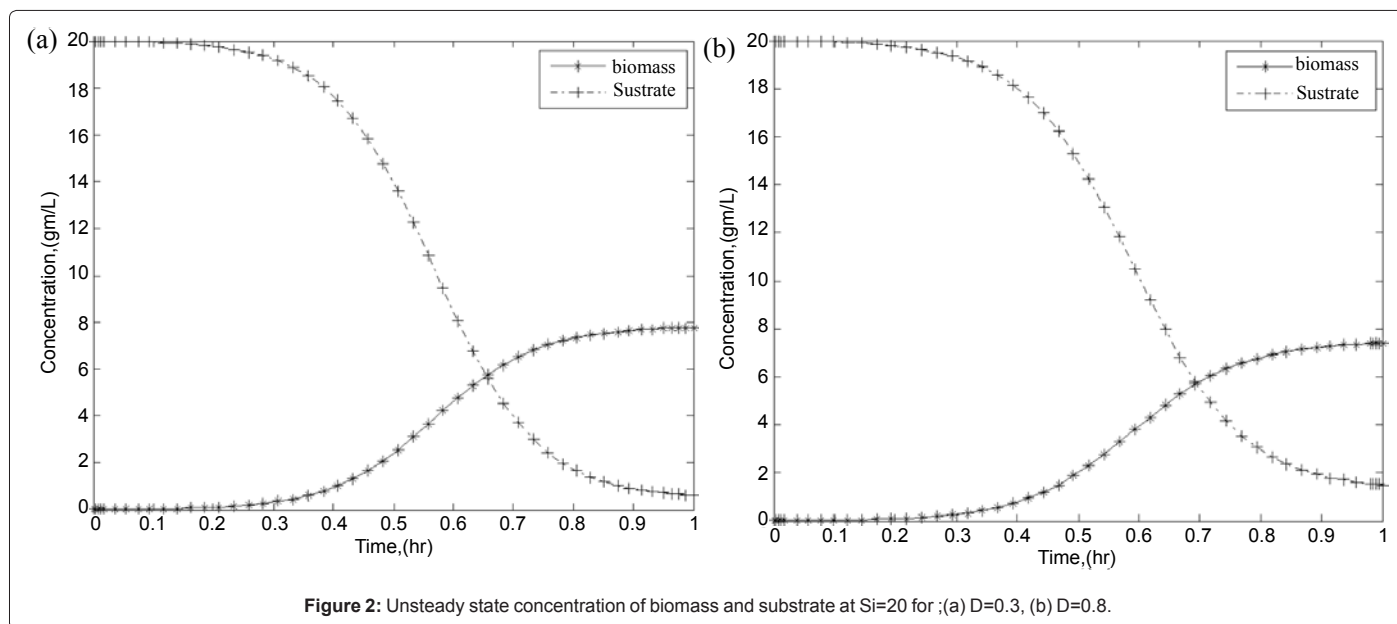


Figure 1: Unsteady state concentration of biomass and substrate at Si=6 for (a) D=0.3, (b) D=0.8.



dynamic model appears that the biomass concentration curves have S-shape and more sluggish when compared with the substrate curves, which have an exponential shape because of the rate of consumed substrate is more than the rate of biomass cell generation in the reactor. The response speed of the biomass and substrate curves increase with  $Si$  and decreases with  $D$  as shown in figures 1-3. The intersection point between two curves indicates to the local optimal point of the system, where the concentration of the biomass equal to that of the substrate. These points are various depended on the operating conditions.

The concentration of the biomass in the reactor decreases with increasing  $D$  (Figure 4a) for low and high  $Si$ . In the contrast, the increasing of  $Si$  increases the concentration of biomass in the reactor as shown in the figure 4b. This is due to the fact; that  $Si$  has a positive effect on the specific growth rate constant ( $\mu$ ) regarding to the Monod law (equation 5). While the increasing of  $D$  tends to increase the dilution of

the substrate which could moderate the growth rate then reduces the concentration of the biomass in the biochemical reactor. The sensitivity of the process (steady-state gain) against  $Si$  (Figure 4b) is more than that with  $D$  (Figure 4a). The effect of  $Si$  is more pronounced at low  $D$  as shown in Figure 4. These behaviors were also concluded by Jarzebski [14].

The effect of temperature on the biomass growth rate appears in figure 5 and 6 at the temperature range from 15 to 30°C. The simulated results explain that the increasing of temperature will increase the growth rate of the biomass at low and high  $Si$ . This tends to increase the response speed of the biomass concentration. The steady-state value of the biomass concentration was unaffected with the increasing of temperature as shown in figure 5 and 6.

Figure 7 and 8 explain the effect of the water acidity (pH) on biomass growth. The effect studied for the available data ranged

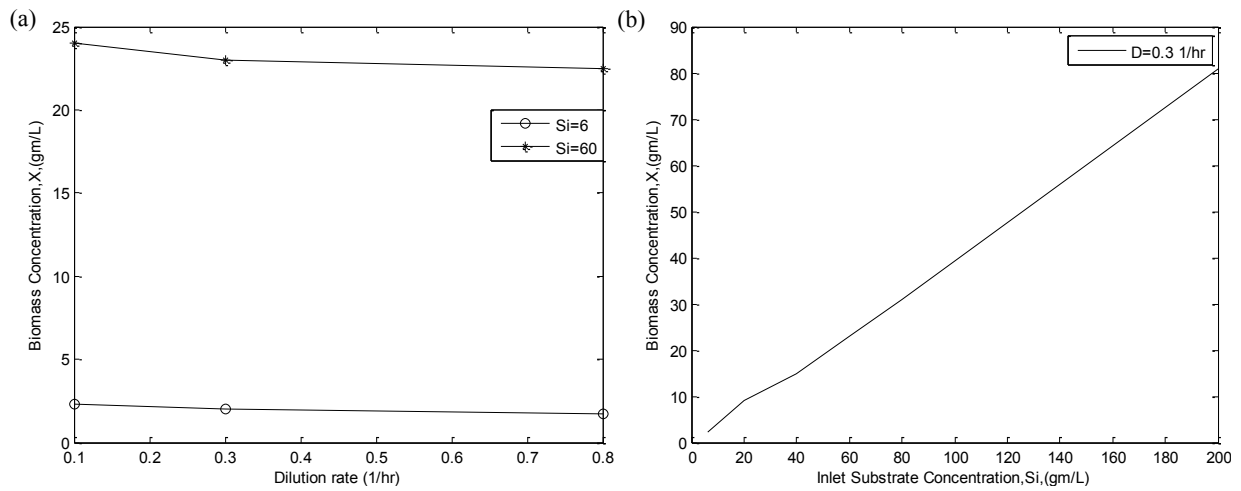


Figure 4: Biomass concentration as a function of (a) Dilution rate, (b) Inlet substrate concentration.

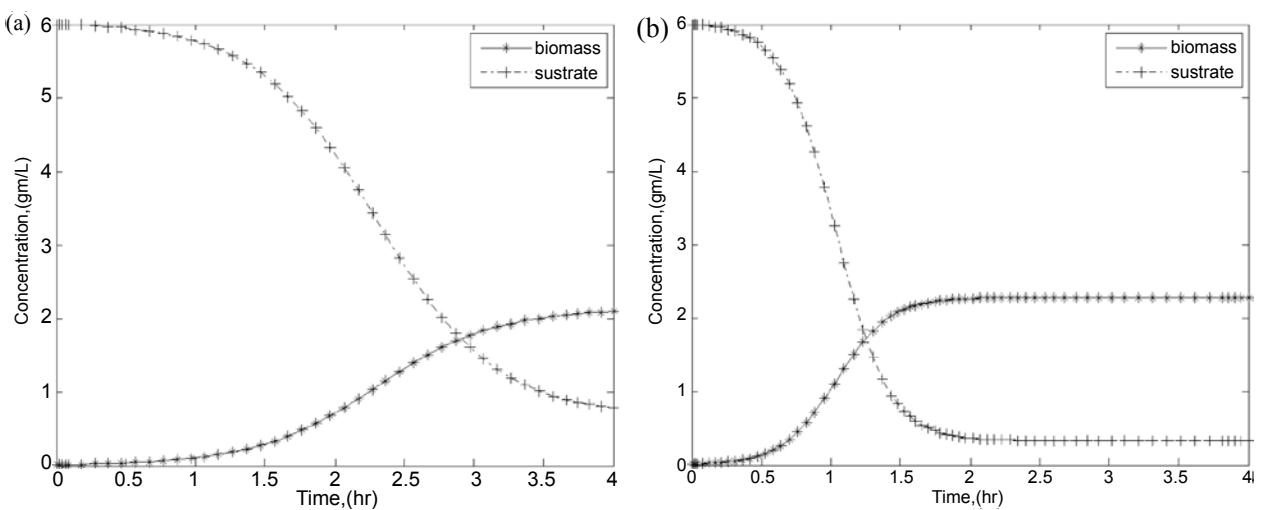


Figure 5: Effect of temperature on the process at  $D=0.3$  and  $Si=6$  for (a)  $T=20$ , (b)  $T=30$ .

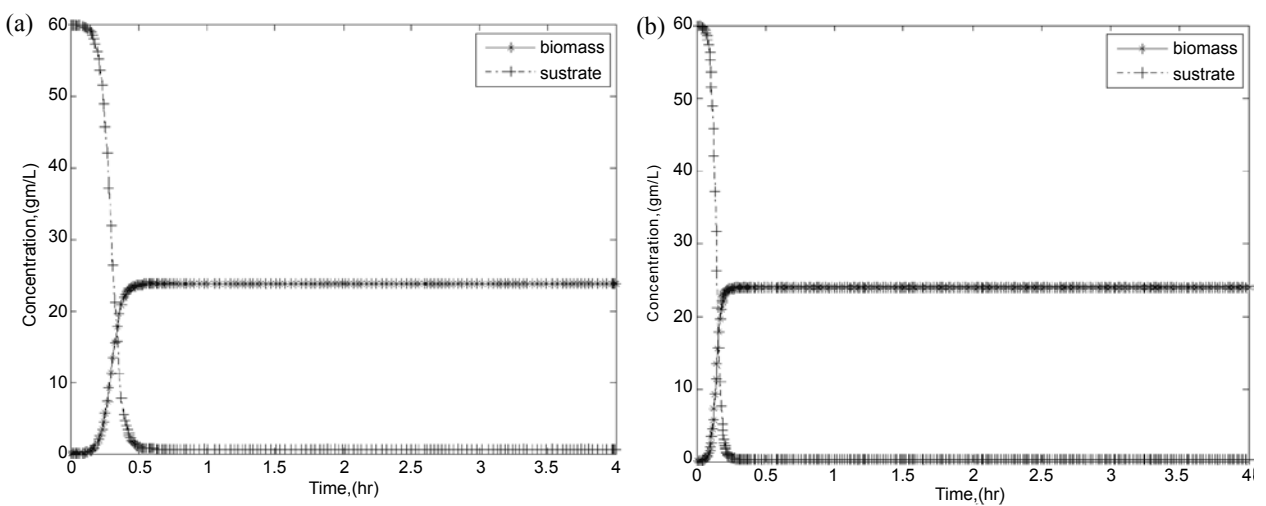
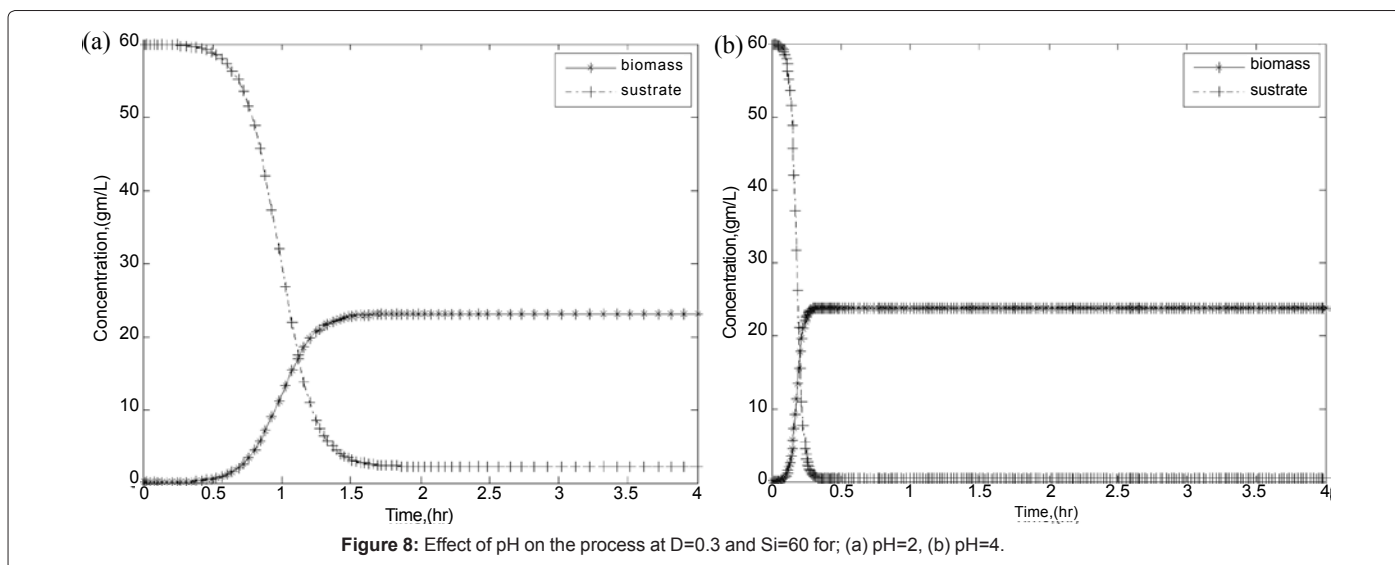
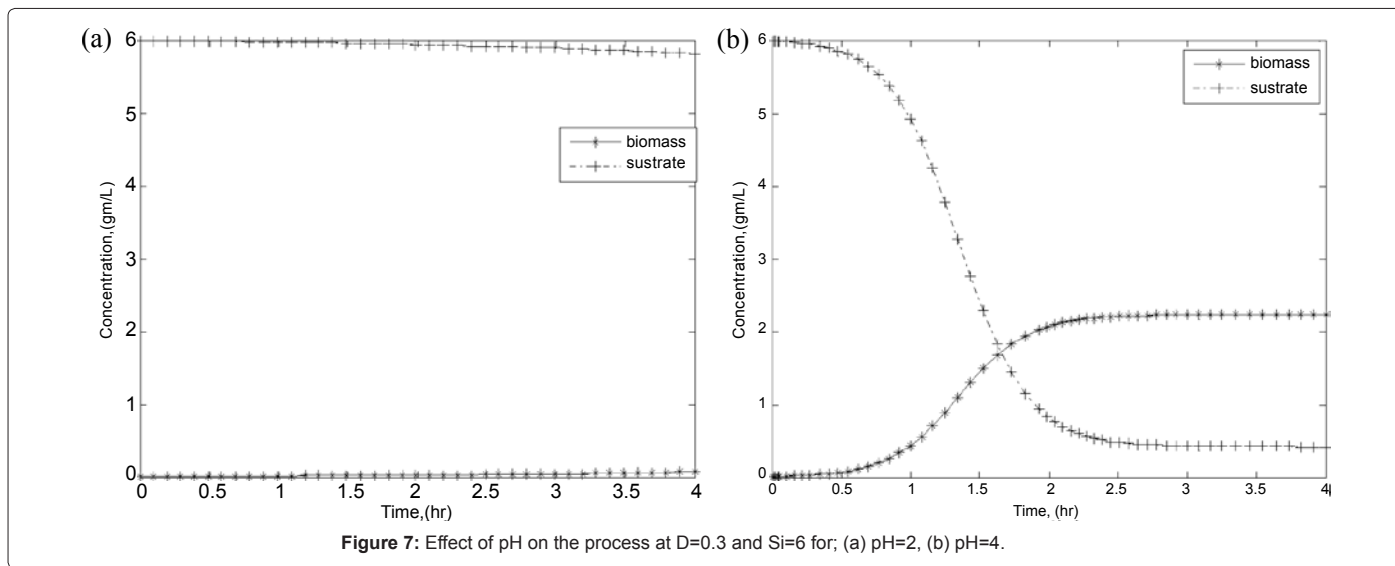


Figure 6: Effect of temperature on the process at  $D=0.3$  and  $Si=60$  for (a)  $T=20$ , (b)  $T=30$ .



between  $pH 2$  to  $pH 4$ . The biomass growth is very slow at low acidity ( $pH 2$ ) and increased with increasing to  $pH 4$  as shown in figure 7a and 7b. The concentration of the biomass in the reactor is very low with the lower feed substrate concentration ( $S_i=6$ ) and  $pH 2$  of water as shown in the figure 7a. At high substrate feed concentration ( $S_i=60$ ), the growth of biomass cell would be enhanced at low acidity ( $pH=2$ ) when compared figure 8a with figure 7a. The growth rate coefficient ( $\mu$ ) is directly affected by  $S_i$  regarding to the Monod law. The final steady-state concentration of biomass is unaffected by the increasing of  $pH$  at high  $S_i$  as shown in figure 8.

Reasonable result can be observed when compared the simulated results with those obtained by Cutlip and Shacham [13] as shown in figure 9. The deviation is about 8%. This indicates that the proposed simulated model is agreed for the present biochemical reactor. Therefore, the reliable model will be used to generate the desirable data for formulating the optimization equation.

### Optimization problem

The available simulated data have been used to correlate the

objective (concentration of biomass  $X$ ) with the decision variables to facilitate the optimization scheme. The selected effective decision variables are; dilution rate ( $D$ ) and inlet concentration of substrate ( $S_i$ ). Nonlinear regression using the Levenberg-Marquardt method is implemented with the aid of the computer program (Statistica version 10).

The empirical correlation is:

$$X = 0.409 S_i - 0.575 D - 0.028 D S_i + 0.02 \quad (9)$$

Subject to inequality constraints:

$$6.0 \leq S_i \leq 200 \quad (10)$$

$$0.1 \leq D \leq 0.8$$

Equation 9 indicates that the dilution rate ( $D$ ) has a negative effect on the biomass concentration while the inlet concentration of substrate ( $S_i$ ) has a positive effect. The interaction between  $S_i$  and  $D$  shows that  $S_i$  is more effective than  $D$ .

### Optimization technique

The objective is to maximize the biomass concentration in the reactor. The optimization equation (equation 9) is interacted and

Population type	Double vector
Population size	80
Creation function	Feasible population
Scaling function	Rank
Selection function	Roulette
Crossover function	Scattered
Crossover fraction	0.8
Mutation function	Adaptive feasible
Migration direction	Forward
Migration fraction	0.1
Hybrid function	Pattern search
Number of generation	51
Function tolerance	1.0E-6

Table 2: Adapted parameters of GA.

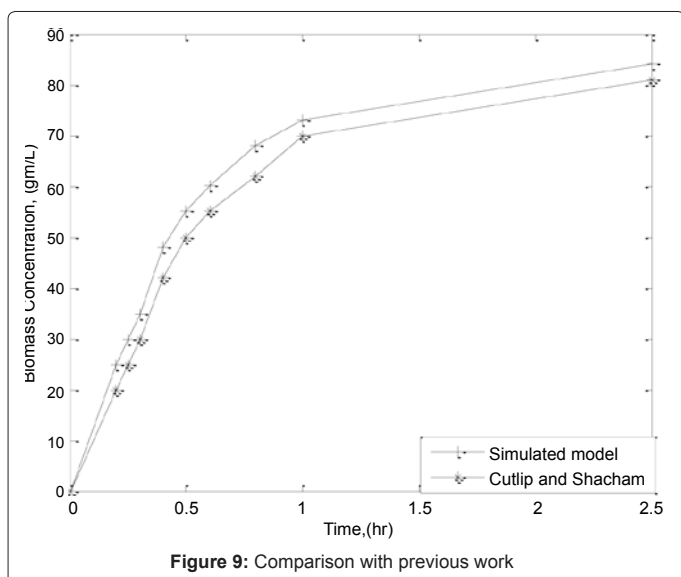


Figure 9: Comparison with previous work

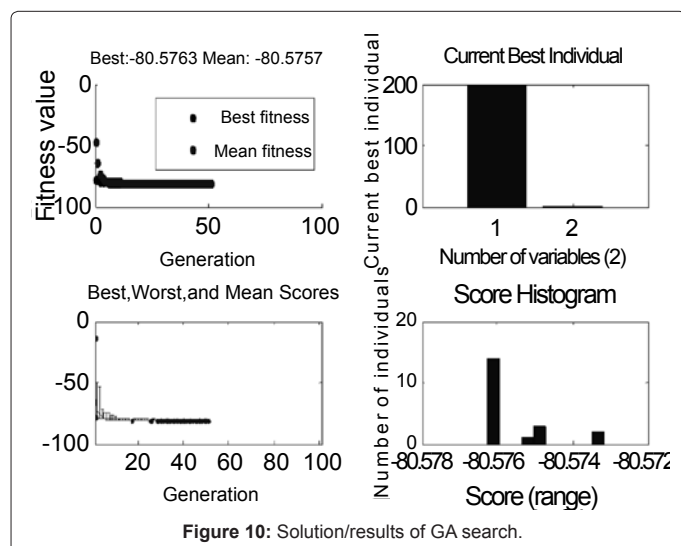


Figure 10: Solution/results of GA search.

nonlinear, so that the deterministic search is unsuccessful. GA has been found suitable for the present biochemical process. GA is stochastic global search based on mechanics of natural selection. Figure 9 illustrates the results/solution of the algorithm scheme. The parameters of the GA were adapted, and the selected operators are suitable for solving the problem to obtain the best optimal values. Hybrid function implemented as the combined search between genetic algorithm and pattern search to refine the values of decision variables. 51 generations occurred regarding to the nonlinearity of the process. The adapted operators of GA are explained in the table 2.

Table 2 explains the best operators of the genetic algorithms. Figure 10 illustrates the outputs of the algorithms solutions/operators of genetic algorithm. GA is implemented with the pattern search by using the hybrid function as shown in table 2 to refine the decision variables. The best fitness, best function and score histogram as shown in figure 10 illustrate that the maximum biomass concentration is 80.57 g/L. The histogram of decision variables indicates that the optimal values are;  $S_i=197.56$  g/L (variable 1) and  $D=0.1hr^{-1}$  (variable 2), which are within the limit of inequality constraints (equation 10). The histogram of the variables in the figure 10 indicates that  $S_i$  (variable 1) is the effective variable on X. Due to the nonlinearity of the bioreactor process; the optimization equation (equation 9) was solved by 51 generations as shown in figure 10.

The optimal sets of the decision variables are illustrated in figures 11a and 11b corresponding to the objective X. The scattering and stochastic of the results are appeared in these figures as a results of natural selection by GA. It is found that the optimal values of the dilution rate (D) are approximately constant within its lower bound as explained in the figure 11a. Inlet substrate concentration ( $S_i$ ) is more sensitive to the optimal objective change(X) as shown in figure 11b. This is due to that  $S_i$  is the effective variable on X as shown in the figure 10.  $S_i$  is changed within its upper bound (Figure11b). These behaviors are because of  $S_i$  has positive effect while D has negative effect on X as shown in the equation 9. Optimal values of the two decision variables are stayed within optimal value of X, which equal to 80.57 g/L as shown in figure 11.

Optimization technique is a powerful tool to obtain the desired operating conditions that improves the performance of the reactor. This reduces the risk of experimental runs and cost consumed for design and operation. However, the reliability of the search depends on; the best selection of decision variables, formulation of the objective function and the selection of the proper optimization technique. Palonen et al. [15] also indicated this conclusion.

### Conclusions

1. Simulated model helps the study of dynamic characteristics of the biochemical reactor. Reliable model could use to generate extra data in the case of unavailable experimental results.
2. Effect of dilution rate was observed at low feed substrate concentration that is below 20 g/L. The effect of pH and temperatures were appeared within the concentration of 60 g/L.
3. Feed substrate concentration was found the effective process variable on the growth rate of the biomass cell in the reactor.
4. Maximum concentration of the biomass cell could be obtained at high concentration of substrate and low dilution rate.

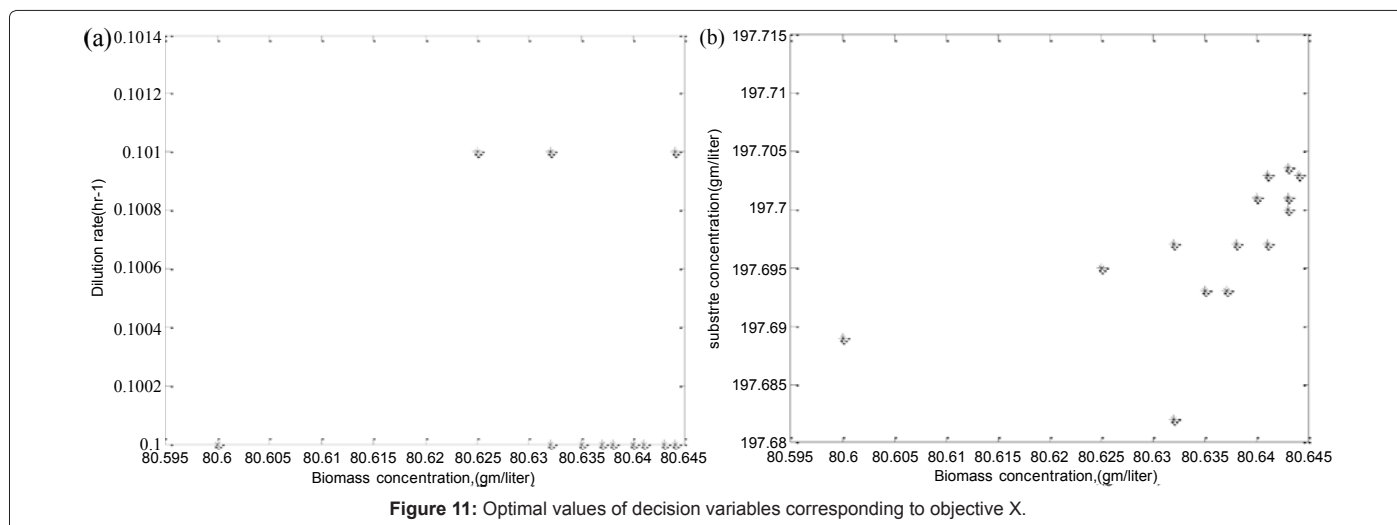


Figure 11: Optimal values of decision variables corresponding to objective X.

Optimal feed substrate was more sensitive to the variations of the objective biomass concentration.

5. Reasonable agreement was obtained when compared the simulated results with that obtained by the previous work.
6. Simulation and optimization provide the development of the process and reducing the risk of experimental runs and cost for design and operation.
7. Stochastic genetic algorithm was suitable search for the nonlinear biochemical reactor process.

#### References

1. Lee JM (1992) Biochemical Engineering. Prentice-Hall, UK.
2. Kapadia A, Nath N, Burg TC, Dawson DM (2010) Lyapunov-Based Continuous-Stirred Tank Bioreactor Control to Maximize Biomass Production Using the Haldane and Monod Specific Growth Model. American Control Conference, USA.
3. Henson MA (2003) Dynamic Modeling and Control of Yeast Cell Populations in Continuous Biochemical Reactors. Comput Chem Eng 27: 1185-1199.
4. Karadag D, Puhakka JA (2010) Effect of Changing Temperature on Anaerobic Hydrogen Production and Microbial Community Composition in an Open-mixed Culture Bioreactor. Int J Hydrogen Energ 35: 10954-10959.
5. Garhyan P, Elnashaie SSEH, Al-Haddad SM, Ibrahim G, Elshisini SS (2003) Exploration and Exploitation of Bifurcation/Chaotic Behavior of a Continuous Fermentor for the Production of Ethanol. Chem Eng Sci 58: 1497-1496.
6. Ruggeri B, Tommasi T, Sassi G (2009) Experimental kinetics and dynamics of hydrogen production on glucose by hydrogen forming bacteria (HFB) culture. Int J Hydrogen Energ 34: 753-763.
7. Charoenchai C, Fleet GH, Henschke PA (1998) Effects of temperature, pH and sugar concentration on the growth rates and cell biomass of wine yeasts. Am J Enol Vitic 49: 283-288.
8. Annamalai M, Doble M (2007) Modeling of D-Hydantoinase production by *Agrobacterium radiobacter* in a batch system. J Appl Sci 7: 2051-2056.
9. Alhumaizi K, Ajbar AH (2004) Optimization of an Unstructured First Order Kinetic Model of Cyclically Operated Bioreactors. J Environ Eng 132: 453-462.
10. Shimizu K (1993) An Overview on the Control System Design of Bioreactors. Measurement and Control 50: 65-84.
11. Gupta AK, Srivastava RK (2006) Integral Water Treatment Plant Design Optimization: Genetic Algorithm Based Approach. IE Journal 8.
12. Lopez FNA, Orlic S, Querol A, Barrio E (2009) Effects of Temperature, pH and Sugar Concentration on the Growth Parameters of *Saccharomyces Cerevisiae*, *S. kudriavzevii* and their Interspecific Hybrid. Int J Food Microbiol 131: 120-127.
13. Cutlip MB, Shacham M (2007) Modular and Multilayer Modeling Application to Biological Processes. Comput Aided Chem Eng 24: 1019-1024.
14. Jarzebski AB (1992) Modelling of Oscillatory Behaviour in Continuous Ethanol Fermentation. Biotechnol Lett 14: 137-142.
15. Palonen M, Hasan A, Siren K (2009) A Genetic Algorithm for Optimization of Building Envelope and HVAC System Parameters. 11th International IBPSA Conference, Glasgow, Scotland, UK.