# Performance analysis of IEEE 802.11e enhanced distributed channel access (EDCA) 

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#### Abstract

In this research article, we have proposed an analytical model for the performance analysis of the enhanced distributed channel access (EDCA) protocol of IEEE 802.11e wireless local area networks standard, using four-dimensional Markov chain. The contemporary EDCA models support only a small subset of EDCA features with limited accuracy. Our model accurately covers all salient features of standard EDCA, like multiple numbers of simultaneously active access categories (AC) per station, internal collision handling, post-back-off after successful transmission and frame-discarding after maximum retransmission limit. The proposed model has also implemented pre-back-off carrier sensing mechanism and back-off counter freezing with deferred states in both the cases. It has incorporated different carrier sensing and back-off parameters for each active AC for access category wise service differentiation. We have computed the saturation throughput and frame access delay of each access category for both RTS/CTS and basic modes. Analytical model is validated by simulation.


Keywords: Access Category (AC), Arbitration Inter-Frame Space (AIFS), Enhanced Distributed Channel Access (EDCA), Quality of Service (QoS), Short Interframe Space (SIFS).

## 1. Introduction

The enhanced distributed channel access (EDCA) protocol of the emerging IEEE 802.11e standard [1] supports access category wise quality of service ( QoS ) differentiation between the real-time and the non real-time applications. In the last few years, performance analysis of EDCA has attracted the attention of several researchers.

### 1.1 Related work

The contemporary research articles [2]-[10] on EDCA are all based on simulations. The analytical models [11]-[21] of EDCA have considered only one priority class active AC or flow per station. But the IEEE 802.11e EDCA standard has suggested four simultaneously active access categories (ACs) per station with internal collision handling feature. Also, the models [11], [13]-[14], [16]-[18], [20]-[21] have not implemented the back-off counter freezing i.e. not decrementing the back-off counter during the channel sensing of pretransmission back-off process, if the channel goes busy due to the transmissions of other access categories. The model [14] has not considered frame discarding after successful transmission, which reduces excessive frame access delay.

The model proposed by Tao and Panwar [22], Tantra et al. [ 23 ], Foh et al. [ 24 ] and Hwang et al. [25] have implemented only two priority class ACs per station. These models [23]-[25] have not considered back-off counter freezing for the higher priority class AC. Also, during the freezing process, the model [22] for the higher priority class AC and the models [22]-[25] for the lower priority class AC, have not incorporated the appropriate deferred states during the busy channel. Also, no deferred states are implemented during physical carrier sensing, which follows the back-off process.

None of the models [11]-[25] have implemented pre-back-off carrier sensing for any access category with the deferred states. The model proposed by Kong et al. [26] has also implemented only for two ACs per station. For the purpose of pre-back-off carrier sensing and channel sensing during the pre-transmission back-off process, it has considered the absolute busy probability of the channel, not the probability of sensing the channel busy by the target access category. Also, for the pre-back-off carrier sensing and back-off counter freezing, the model has considered arbitrary values for AIFS and total deferred time for all ACs.

Also, the models [11]-[26] have not incorporated the standard post back-off after successful transmission which reduces the starvation of lower ACs.

### 1.2 Scope of our proposed model

The aforesaid models are less accurate and inefficient due to their inability to capture the real situations. The differences between the above models and the model implemented by us are listed as follows:
(i) We have incorporated multiple number of simultaneously active ACs per station which is theoretically unlimited in our solution framework. (ii) We have implemented the internal collision handling feature with the extensive study of its effect on the performance of EDCA. (iii) We have incorporated pre-back-off carrier sensing for continuous AIFS[i] duration with deferred states for the $i_{t h}$ access category $A C_{i}$. (iv) We have implemented the channel sensing and back-off counter freezing with deferred states during pretransmission back-off process, followed by carrier sensing similar to case (iii). (v) We have considered the probability of sensing the channel busy ( $p_{i, s b}$ as per equation 14 ) by the access category $A C_{i}$, for both the carrier sensing and back-off counter freezing as mentioned in (iii) and (iv), instead of considering the absolute busy probability of the channel. Also, for both the above cases, we have considered the exact $A I F S_{i}$ value of each $A C_{i}$, as specified by the IEEE 802.11e standard, instead of choosing an arbitrary value. Again for both cases, we have computed the exact value of the total deferred time $T_{i}$ of the target $A C_{i}$ in the deferred states, as per computation in equation (20), instead of a choosing an arbitrary value. This computation involves $T_{i}$ as a function of the successful transmission probabilities of other ACs $\left(p_{j, s u}\right)$ and the collision probability $\left(P_{c l}\right)$ which are the equation variables. (vi) We have incorporated the standard post back-off after successful transmission to reduce the starvation of lower ACs. (vii) Frame discarding after retry limit which reduces excess frame access delay, is also considered by us.

The implementation of the above mentioned features in our model has made it very accurate, fair and efficient by taking care of the real situations.

The rest of this paper is organized as follows. The proposed analytical model, performance analysis and validation of model are discussed in section 2,3 and 4 respectively. Finally the conclusion is drawn in section 5.

## 2. Proposed analytical model

In this section, we have formulated the discrete-time, four dimensional Markov chain (Fig 1a and Fig 1b) for our proposed model for the $i_{t h}\left(0 \leq i \leq a c_{m}-1\right)$ access category $A C_{i}$ within a station. Here $a c_{m}$ is the maximum number of simultaneously active ACs per station which is theoretically unlimited in our solution framework. We have assumed ideal channel condition with saturation traffic for each access category. The access category $A C_{i}$ has its own arbitration inter-frame space number $A I F S N_{i}$ to compute its $A I F S_{i}$ (or AIFS [i]) value as: $\operatorname{AIFS}_{i}=\operatorname{AIFSN}_{i} * \delta+S I F S$, where $\delta$ is the slot time. It has also minimum contention window $W_{i, 0}$, maximum contention window $W_{i, m}$ and retry limit parameter $r_{i, m}$.

### 2.1 Markov chain formulation

In our model, time is considered to be slotted. For the access category $A C_{i}$ at slot time $t$, let $s(i, t), b(i, t)$ and $d(i, t)$ be the stochastic processes respectively to denote backoff stage value $r$, the back-off counter value $k$, and the AIFS counter or deferred states counter value $d$. For the purpose of random back-off, the value of $k$ is uniformly drawn from $\left[0, W_{i, r}-1\right]$ where $W_{i, r}=(2)^{r} W_{i, 0}$ and $W_{i, 0} \leq W_{i, r} \leq W_{i, m}=2^{r_{i, m}} W_{i, 0}$. Here $W_{i, 0}, W_{i, r}$ and $W_{i, m}$ are respectively the contention window at back-off stage $0, r$ and $r_{i, m}$.

We assume that the conditional collision probability $p_{i, c l}$ of access category $A C_{i}$ is constant and independent of the back-off stage $r$. Accordingly, the four-dimensional process $\{i, s(i, t), b(i, t), \mathrm{d}(i, t)\}$ becomes a discrete-time four-dimensional Markov chain for the access category $A C_{i}$. At slot time t , the state of $A C_{i}$ can be fully described by $(i, r, k, d)$. For the countdown states of AIFS counter and that of deferred states counter during the pre-back-off carrier sensing: $\left(r=c, k=0\right.$ and $\left.0 \leq d \leq \operatorname{AIFS}[i]+T_{i}\right)$; for pre-transmission back-off process states: $\left(0 \leq r \leq r_{i, m}, 0 \leq k \leq W_{i, r}-1\right.$ and $\left.d=0\right)$; for the countdown states of the deferred state counter and that of AIFS counter during the back-off counter freezing of the pre-transmission back-off process: $\left(0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1\right.$ and $1 \leq$ $\left.d \leq \operatorname{AIFS}[i]+T_{i}\right)$; for post-back-off stage: $(r=p, 0 \leq k \leq W-1$ and $d=0)$.

### 2.2 The state transition probabilities

Before transmitting a frame, the $i_{t h}$ access category $A C_{i}$ first performs the pre-backoff carrier sensing process to sense the channel continuously free for $A I F S_{i}$ or AIFS[i] period with the following state transitions from (1) to (3) with the non-null transition probabilities:

1) The $A C_{i}$ first goes from the $A I F S_{i}$ counter's countdown states (i,c,0,AIFS $S_{i}$ ) to (i,c, 0,0 ) by decrementing the $A I F S_{i}$ counter by 1 in each slot time by sensing the channel free with probability $p_{i, s f}$

$$
P\{(i, c, 0, d-1) \mid(i, c, 0, d)\}=p_{i, s f}, 1 \leq d \leq \operatorname{AIFS}[i] .
$$



Fig 1(a): Four-dimensional Markov chain for the $i_{\text {th }}$ AC.


Fig 1(b): Expanded view of the Markov chain for $r_{t h}$ back-off stage of figure (1a).
2) During each of the $A I F S_{i}$ countdown states of (1), if the channel goes busy due to the transmission of other ACs , the $A C_{i}$ goes to the maximum deferred state ( $i, c, 0, \operatorname{AIFS}[i]+T_{i}$ ), by sensing the channel busy with the probability $p_{i, s b}$

$$
P\left\{\left(i, c, 0, \operatorname{AIFS}[i]+T_{i}\right) \mid(i, c, 0, d)\right\}=p_{i, s b}, \quad 0 \leq d \leq \operatorname{AIFS}[i] .
$$

Where the meaning and the computation process of $T_{i}$ is explained in equation (20).
3) From the maximum deferred state (i, $c, 0, \operatorname{AIFS}[i]+T_{i}$ ), there is countdown of the deferred state counter by 1 at each slot time

$$
P\{(i, c, 0, d-1) \mid(i, c, 0, d)\}=1, \quad \operatorname{AIFS}[i]+1 \leq d \leq \operatorname{AIFS}[i]+T_{i} .
$$

Through this countdown process, access category $A C_{i}$ ultimately goes to the $A I F S_{i}$ countdown state ( $i, c, 0, A I F S_{i}$ ) like (1) and recursively follow the state transition procedures (1), (2), and (3), to eventually reach ( $i, c, 0,0$ ) state, to complete pre-back-off carrier sensing process.
4) From the AIFS $_{i}$ counter's countdown state ( $i, c, 0,0$ ), the pre-transmission back-off process is started for the back-off stage 0 , if the channel is free

$$
P\{(i, 0, k, 0) \mid(i, c, 0,0)\}=\frac{p_{i, s f}}{W_{i, 0}}, \quad 0 \leq k \leq W_{i, 0}-1 .
$$

5) During pre-transmission back-off process of any back-off stage $r$, the back-off counter is frozen i.e. not decremented and the access category $A C_{i}$ goes to the maximum deferred state ( $i, r, k, \operatorname{AIFS}[i]+T_{i}$ ), if channel goes busy

$$
P\left\{\left(i, r, k, \operatorname{AIFS}[i]+T_{i}\right) \mid(i, r, k, 0)\right\}=p_{i, s b}, \quad O \leq r \leq r_{i, m} \text { and } 1 \leq k \leq W_{i, r}-1 .
$$

6) During the frozen period, there is countdown of deferred state counter by 1 at each slot time

$$
\begin{gathered}
P\{(i, r, k, d-1) \mid(i, r, k, d)\}=1, \quad 0 \leq r \leq r_{i, m}, \quad 1 \leq k \leq W_{i, r}-1 \text { and } \\
\operatorname{AIFS}[i]+1 \leq d \leq \operatorname{AIFS}[i]+T_{i} .
\end{gathered}
$$

7) After the frozen period elapses by $T_{i}$, for the remaining frozen time, the AIFS[i] counter is decreased by one, if the channel is free

$$
\begin{gathered}
P\{(i, r, k, d-1) \mid(i, r, k, d)\}=p_{i, s f}, \quad 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1 \text { and } \\
1 \leq d \leq \operatorname{AIFS}[i] .
\end{gathered}
$$

Through this transition, $A C_{i}$ resumes the pre-transmission back-off state (i,r,k,0) after the frozen period.
8) But during the AIFS[i] counter countdown of step 7, if the channel goes busy again due to transmissions of other ACs, $A C_{i}$ again and goes to the maximum deferred state $\left(i, r, k, \operatorname{AIFS}[i]+T_{i}\right)$ like that of step 5.

$$
\begin{gathered}
P\left\{\left(i, r, k, \operatorname{AIFS}[i]+T_{i}\right) \mid(i, r, k, d)\right\}=p_{i, s b,} \quad 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1 \text { and } \\
1 \leq d \leq \operatorname{AIFS}[i] .
\end{gathered}
$$

Through these transition states (5) to (8), the access category $A C_{i}$ completes the backoff counter freezing process through transition step 7 and comes back to the pretransmission back-off process to resume countdown of back-off counter.
9) During pre-transmission back-off process, the back-off counter is decremented by 1 , at each slot time, if channel is free, otherwise follow step 5

$$
P\{(i, r, k-1,0) \mid(i, r, k, 0)\}=p_{i, s f}, \quad 0 \leq r \leq r_{i, m} \text { and } 1 \leq k \leq W_{i, r}-1
$$

When the back-off counter reaches zero, the access category $A C_{i}$ transmits the frame.
10) In case of successful transmission, state transition takes place to post-transmission back-off stage $p$, for a random wait interval. This interval is drawn uniformly from the range 0 to $W$ - 1 time slots, where, $W$ denotes the post-transmission back-off window, which is same for all ACs

$$
P\{(i, p, k, 0) \mid(i, r, 0,0)\}=\frac{\left(1-p_{i, c l}\right)}{W}, \quad 0 \leq r \leq r_{i, m} \text { and } 0 \leq k \leq W-1 \text {. }
$$

11) In case of collision, except during maximum back-off stage $r_{i, m}$, transition takes place to next stage, by doubling the contention window

$$
P\{(i, r+1, k, 0) \mid(i, r, 0,0)\}=\frac{p_{i, c l}}{W_{i, r+1}}, 0 \leq r \leq r_{i, m}-1,0 \leq k \leq W_{i, r+1}-1
$$

12) In case of collision at maximum back-off stage $r_{i, m}$, the frame is discarded and transition takes place to the state ( $i, c, 0, \operatorname{AIFS}[i])$ to start the pre-back-off carrier sensing for transmitting a new frame

$$
P\left\{(i, c, 0, \operatorname{AIFS}[i]) \mid\left(i, r_{i, m} 0,0\right)\right\}=p_{i, c l} .
$$

13) During post-back-off stage $p$, as there is no channel sensing, the back-off counter is always decremented by one

$$
P\{(i, p, k-1,0) \mid(i, p, k, 0)\}=1,1 \leq k \leq W-1 .
$$

14) After post-transmission back-off process, transition takes place to the state (i, c, $0, A I F S[i]$ ) to start pre-back-off carrier sensing for transmitting a new frame

$$
P\{(i, c, 0, \operatorname{AIFS}[i]) \mid(i, p, 0,0)\}=1
$$

For state transition for post-transmission back-off stage $p$, as mentioned in the state transition step 10 , we have chosen the same post-transmission back-off window $W$ for all ACs to satisfy the inequality: $W_{3,0}<W_{2,0}<W<W_{1,0}<W_{0,0}$ with the pretransmission back-off windows variables $W_{3,0}, W_{2,0}, W_{1,0}, W_{0,0}$. Due to this carefully chosen inequality, the post-transmission back-off process reduces the starvation of the lower ACs i.e. $A C_{0}$ and $A C_{1}$, by decreasing their post-transmission back-off delay compared to that of the pre-transmission back-off process. Also, unlike pre-transmission back-off process, the transitional probability of decrementing the back-off counter during the post-transmission back-off process is considered one, since the channel sensing is not implemented during this stage. Because, post-transmission back-off is not really meant for the frame transmission like the pre-transmission back-off process. It is performed only for adding some random wait to the recently successfully transmitting access categories to defer their next transmission.

### 2.3 System equations

Let $b_{i, r, k, d}=\lim _{t \rightarrow \infty} P\{i, s(i, t)=r, b(i, t)=k, \mathrm{~d}(i, t)=d\}$ be the stationary distribution of the four-dimensional Markov chain for the $i_{\text {th }} \mathrm{AC}$, for $0 \leq i \leq a c_{m}-1$, $0 \leq r \leq r_{i, m}, 0 \leq k \leq W_{i, r}-1$ and $0 \leq d \leq \operatorname{AIFS}[i]+T_{i}$. In steady state, we can derive the following equations through chain regularities

$$
\begin{equation*}
b_{i, r, 0,0}=b_{i, r-1,0,0} p_{i . c l} \rightarrow b_{i, r, 0,0}=\left(p_{i . c l}\right)^{r} b_{i, 0,0,0}, \quad 0 \leq r \leq r_{i, m} . \tag{1}
\end{equation*}
$$

Now using the standard steady state formulation of Markov chain, w. r. t. Fig 1(b), for pre-transmission back-off process, we get

$$
\begin{align*}
& b_{i, r, k, 0}=b_{i, r-1,0,0} \frac{p_{i, c l}}{W_{i, r}}+b_{i, r, k, 1} p_{i, s f}+b_{i, r, k+1,0} p_{i, s f}, \quad 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1 . \\
& =\frac{b_{i, r, 00}}{W_{i, r}}+b_{i, r, k, 1} p_{i, s f}+b_{i, r, k+1,0} p_{i, s f} . \quad \text { (Using the first part of Eq. (1) ) } \tag{2a}
\end{align*}
$$

Using chain regularities w.r.t. Fig 1(b), we can derive

$$
\begin{equation*}
b_{i, r, k, 1} p_{i, s f}=p_{i, s b} b_{i, r, k, 0} \rightarrow b_{i, r, k, 1} p_{i, s f}=\left(1-p_{i, s f}\right) b_{i, r, k, 0} . \tag{2b}
\end{equation*}
$$

Putting (2b) in (2a) and interchanging sides we get

$$
\begin{equation*}
b_{i, r, k, 0}=\frac{b_{i, r, 0}}{W_{i, r} r_{i, s f}}+b_{i, r, k+1,0} \tag{2c}
\end{equation*}
$$

From (2c), using the regularities of chain we get

$$
\begin{equation*}
b_{i, r, k+1,0}=\frac{b_{i,, 0,0}}{W_{i, r} p_{i, s f}}+b_{i, r, k+2,0} \tag{2d}
\end{equation*}
$$

Similarly,

$$
\begin{equation*}
b_{i, r, W_{i, r}-2,0}=\frac{b_{i, r, 0,0}}{W_{i, r} p_{i, s f}}+b_{i, r, W_{i, r}-1,0} \tag{2e}
\end{equation*}
$$

Since, for $r_{t h}$ stage, $b_{i, r, W_{i, r}-1,0}$ is the last element of the chain and there is no state on its right side, we get

$$
\begin{equation*}
b_{i, r, W_{i, r}-1,0}=\frac{b_{i, 0,0}}{W_{i, r} p_{i, s f}} \tag{2f}
\end{equation*}
$$

Putting (2d) to (2f) in (2c), we get

$$
\begin{align*}
b_{i, r, k, 0} & \left.=\frac{b_{i, r, 0,0}}{W_{i, r} p_{i, s f}}+\frac{b_{i, r, 0,0}}{W_{i, r} p_{i, s f}}+\cdots \frac{b_{i, r, 00}}{W_{i, r} p_{i, s f}}+\frac{b_{i, r, 0,0}}{W_{i, r} p_{i, s f}},\left(W_{i, r}-1\right)-(k-1)=W_{i, r}-k \text { terms }\right) \\
& =\frac{W_{i, r}-k}{W_{i, r}} \frac{b_{i, r, 0,0}}{p_{i, s f}} \\
& =\frac{W_{i, r}-k}{W_{i, r}} \frac{b_{i, r, 0,0}}{\left(1-p_{i, s b}\right)^{\prime}}, \quad 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1, d=0 . \tag{2~g}
\end{align*}
$$

For carrier sensing during back-off counter freezing of pre-transmission back-off process, from Eq. (2b), we get

$$
\begin{align*}
& b_{i, r, k, 1} p_{i, s f}=\left(1-p_{i, s f}\right) b_{i, r, k, 0} \\
& \rightarrow b_{i, r, k, 1}=\frac{\left(1-p_{i, s f}\right) b_{i, r, k, 0}}{p_{i, s f}}, \quad 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1 \tag{3a}
\end{align*}
$$

Now using chain relation, w.r.t. Fig 1 (b) we get

$$
\begin{align*}
& b_{i, r, k, 1}=b_{i, r, k, 2} p_{i, s f}  \tag{3b}\\
& \rightarrow b_{i, r, k, 2}=\frac{b_{i, r, k, 1}}{p_{i, s f}}=\frac{\left(1-p_{i, s f)} b_{i, r, k, 0}\right.}{p_{i, s f^{2}}}, \text { (Using Eq. (3a)and (3b)). } \tag{3c}
\end{align*}
$$

Similarly,

$$
\begin{equation*}
b_{i, r, k, 3}=\frac{b_{i, r, k, 2}}{p_{i, s f}}=\frac{\left(1-p_{i, s f}\right) b_{i, r, k, 0}}{p_{i, s f^{3}}{ }^{3}} . \tag{3d}
\end{equation*}
$$

Through the same reasoning, we get

$$
\begin{equation*}
b_{i, r, k, A I F S[i]}=\frac{\left(1-p_{i, s f}\right) b_{i, r, k, 0}}{p_{i, s f} A I F S[i]} . \tag{3e}
\end{equation*}
$$

Therefore,

$$
\begin{equation*}
b_{i, r, k, d}=\frac{\left(1-p_{i, s f}\right) b_{i, r, k, 0}}{p_{i, s f^{d}}}, 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1 \text { and } \leq d \leq A I F S[i] . \tag{3f}
\end{equation*}
$$

For other deferred states during back-off counter freezing, using the chain relationship of Fig 1(b), we get

$$
\begin{align*}
& b_{i, r, k, d}=\frac{\left(1-p_{i, s f}\right)}{\left(p_{i, s f}\right)^{A I F S[i]}} b_{i, r, k, 0} \\
& 0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1, \operatorname{AIFS}[i]+1 \leq d \leq \operatorname{AIFS}[i]+T_{i} \tag{4}
\end{align*}
$$

Using the chain regularity in the similar way for pre-back-off carrier sensing with the deferred states, we get

$$
\begin{align*}
& b_{i, c, 0, d}=\frac{1}{\left(p_{i, s f}\right)^{d+1}} b_{0,0,0,0}, 0 \leq d \leq \operatorname{AIFS}[i] .  \tag{5}\\
& b_{i, c, 0 d}=\frac{1-p_{i, s f} A I F S[i]+1}{\left(p_{i, s f}\right)^{A I F S[i]+1}} b_{0,0,0,0}, \quad \operatorname{AIFS}[i]+1 \leq d \leq \operatorname{AIFS}[i]+T_{i} . \tag{6}
\end{align*}
$$

For post-back-off stage p , w.r.t Fig 1(a),

$$
\begin{equation*}
b_{i, p, k, 0}=\frac{W-k}{W} b_{i, p, 0,0}, 0 \leq k \leq W-1 \tag{7}
\end{equation*}
$$

(Putting $r=p, W_{i, r}=W$ and $p_{i, s b}=0$ in Eq. (2g), since for post-back-off stage p, back-off counter is decremented with probability of 1)
Also for post-back-off stage $p$, we can derive

$$
\begin{equation*}
b_{i, p, 0,0}=\sum_{r=0}^{r_{i, m}}\left(1-p_{i, c l}\right) b_{i, r, 0,0} . \tag{8}
\end{equation*}
$$

Now, since the sum total of the steady state probabilities of all the states of the Markov chain is 1, therefore
$\sum_{d=0}^{A I F S[i]+T_{i}} b_{i, c, 0, d}+\sum_{r=0}^{r_{i, m}} \sum_{k=0}^{W_{i, r-1}} b_{i, r, k, 0}+\sum_{r=0}^{r_{i, m}} \sum_{k=1}^{W_{i, r-1}} \sum_{d=1}^{A I F S[i]+T_{i}} b_{i, r, k, d}+\sum_{k=0}^{W-1} b_{i, p, k, 0}=1$.
Using Eq. (1) to Eq. (9) and by simplifying we get

$$
\begin{align*}
& b_{i, 0,0,0}= \\
& {\left[\left[\left[\frac{\left(1-p_{i, s f} A I F S[i]+1\right)}{\left(p_{i, s f}\right)^{A I F S[i]+1}}\right]\left[\frac{1+\left(1-p_{i, s f}\right) T_{i}}{\left(1-p_{i, s f}\right)}\right]\right]+\left[\sum_{r=0}^{r_{i, m}}\left[1+\frac{1}{p_{i, s f}} \frac{\left(W_{i, r}-1\right)}{2}\right]\left(p_{i, c l}\right)^{r}\right]+\right.} \\
& \left.\left[\sum_{r=0}^{r_{i, m}}\left[\frac{\left(1-\left(p_{i, s f}\right)^{A I F S[i]}+\left(1-p_{i, s f}\right) T_{i}\right)}{\left(p_{i, s f}\right)^{A I F S[i]+1}} \frac{\left(W_{i, r}-1\right)}{2}\right]\left(p_{i, c l}\right)^{r}\right]+\left[\left(1-p_{i, c l}\right) \frac{W+1}{2} \sum_{r=0}^{r_{i, m a x}}\left(p_{i, c l}\right)^{r}\right]\right]^{-1} . \tag{10}
\end{align*}
$$

Let $\tau_{i}$ be the probability that an $A C_{i}$ within a station transmits in the channel in a randomly chosen slot time. Since, a transmission occurs in state ( $i, r, 0,0$ ) for all transmission stages $r \in\left[0, r_{i, m}\right], \tau_{i}$ may be expressed as the sum of steady state probabilities of all the corresponding (i,r,0,0) states. Therefore

$$
\begin{equation*}
\tau_{i}=\sum_{r=0}^{r_{i, m}} b_{i, r, 0,0}=\sum_{r=0}^{r_{i, m}} b_{i, 0,0,0}\left(p_{i, c l}\right)^{r}=\frac{\left(1-\left(p_{i, c l}\right)^{\left(r_{i, m}+1\right)}\right)}{\left(1-p_{i, c l}\right)} b_{i, 0,0,0}, 0 \leq i \leq a c_{m}-1 . \tag{11}
\end{equation*}
$$

Also, let $\tau$ be the probability that a station transmits in the channel in a randomly chosen slot time. A station transmits, when at least one of the ACs within that station transmits. Therefore

$$
\begin{equation*}
\tau=1-\prod_{i=0}^{a c_{m}-1}\left(1-\tau_{i}\right) . \tag{12}
\end{equation*}
$$

Let $p_{i, s f}$ be the probability that an access category $A C_{i}$ within a station senses the channel free during pre-back-off carrier sensing and pre-transmission back-off process. The $A C_{i}$ may sense the channel free, if none of the ACs from the set of remaining ACs within the same station and none from the remaining ( $N-1$ ) stations transmits. Here $N$ is the total number of stations in the WLAN. Therefore

$$
\begin{equation*}
p_{i, s f}=(1-\tau)^{N-1} \prod_{i^{\prime} \neq i}\left(1-\tau_{i^{\prime}}\right), 0 \leq \mathrm{i} \leq \mathrm{ac}_{\mathrm{m}}-1 . \tag{13}
\end{equation*}
$$

Therefore, the probability $p_{i, s b}$, that an access category $A C_{i}$ within a station senses the channel free, be given as

$$
\begin{equation*}
p_{i, s b}=1-p_{i, s f},\left(\text { Since } p_{i, s b}+p_{i, s f}=1\right) . \tag{14}
\end{equation*}
$$

Let $p_{i, c l}$ be the conditional collision probability i.e. the probability that an access category $A C_{i}$ within a station, while transmitting, sees collision in the channel. Considering both internal and external collisions, such collision would occur when at least one access category from the set of higher ACs within the same station or from the remaining $N-1$ station transmits. Therefore,

$$
\begin{equation*}
p_{i, c l}=1-(1-\tau)^{N-1} \prod_{i^{\prime}>i}\left(1-\tau_{i^{\prime}}\right) . \tag{15}
\end{equation*}
$$

Now, considering all the $N$ stations in the WLAN, let $p_{i, s u}$ be the successful transmission probability of an $A C_{i}$ in the wireless channel. $p_{i, s u}$ can be calculated as $N$ times the joint probabilities the following three statistically independent events:
(i) The $A C_{i}$ within the station is transmitting with probability $\tau_{i}$,
(ii) None of the higher ACs than the access category $A C_{i}$ in the same station is transmitting with probability $\prod_{i^{\prime}>i}\left(1-\tau_{i^{\prime}}\right)$,
(iii) None of the remaining ( $N-1$ ) stations are transmitting with probability of

$$
(1-\tau)^{N-1} .
$$

Therefore,

$$
\begin{equation*}
p_{i, s u}=N \tau_{i}(1-\tau)^{N-1} \prod_{i^{\prime}>i}\left(1-\tau_{i^{\prime}}\right) . \tag{16}
\end{equation*}
$$

Now, including all ACs, the total successful transmission probability $P_{s u}$ in the channel, is the sum total of the successful transmission probabilities of the individual ACs. Therefore,

$$
\begin{equation*}
P_{s u}=\sum_{i=0}^{a c_{m}-1} p_{i, s u} . \tag{17}
\end{equation*}
$$

The probability $P_{f r}$, that the channel is free or idle, is the probability that none of the $N$ stations In the WLAN is transmitting. Therefore

$$
\begin{equation*}
P_{f r}=(1-\tau)^{N} . \tag{18}
\end{equation*}
$$

Finally, the probability $P_{c l}$, that collision is taking in the channel is given by

$$
\begin{equation*}
P_{c l}=1-P_{s u}-P_{f r} . \tag{19}
\end{equation*}
$$

Since, the sum total of the probabilities of all the above three events are 1.
Let $T_{i}$ (in slot time) be the total deferred time of the target access category $A C_{i} . T_{i}$ is actually the transmission time of other ACs in slot time that makes the channel busy for the target access category $A C_{i}$ during the pre-back-off carrier sensing and back-off counter freezing. $T_{i}$ is computed as the statistical average of the expected value of the successful transmission time and collision time of other ACs, divided by the slot time $\delta$ and rounded off to the nearest integer. Therefore

$$
\begin{equation*}
T_{i}=\frac{1}{\delta} \frac{\sum_{j=0, j \neq i}^{a c m-1}\left(p_{j s u} T_{j, s u}\right)+P_{c c} T_{c l}}{\sum_{j=0, j \neq i}^{a c \mid}\left(p_{j, s u}\right)+P_{c l}} \tag{20}
\end{equation*}
$$

Now equations (10) to (20), for $0 \leq i \leq\left(a c_{m}-1\right)$, give rise to a total of ( $7 * a c_{m}+4$ ) non-linear equations with equal number of unknown variables, depending on the value of $a c_{m}$. These variables are given by the set: $\left\{b_{i, 0,0,0}, \tau_{i}, p_{i, s f}, p_{i, s b}, p_{i, c l}, p_{i, s u}, T_{i} \mid\left(0 \leq i \leq a c_{m}-1\right)\right\}$ and $\tau, P_{s u}, P_{f r}$, and $P_{c l}$. Here, $T_{i, s u}, T_{c l}, W, W_{i, 0}, W_{i, r}, r_{i, m}$ are known constants for $0 \leq r \leq r_{i, m}, 0 \leq i \leq a c_{m}-1$ and $a c_{m}$ is numbers of simultaneously active ACs per stations which is theoretically unlimited in our model. By numerical methods, we have solved the above equations for variables: $\left\{\tau_{i} \mid\left(0 \leq i \leq a c_{m}-1\right)\right\}$ and $\tau$ for any value of $a c_{m}$ in the same solution framework. Knowing the values of the above variables, subsequent computations are carried out.

## 3. Performance analysis.

### 3.1 Saturation throughput computation

The normalized saturation throughput of $A C_{i}$ i.e. Throughput ${ }_{i}$ is defined as the ratio of the expected value of the successful transmission time of the payload i.e. $\left(p_{i, s u} \frac{E(P)}{\text { speed }_{m}}\right)$ to the expected value of the total time of transmission. The latter includes:
(i) the average idle time $\left(P_{f r} \delta\right.$ ), (ii) average total successful frame transmission time $\sum_{i=0}^{a c_{m}-1}\left(p_{i, s u} T_{i, s u}\right)$ of all ACs inclusive of payload with headers and (iii) the average time lost in collision $\left(P_{c l} T_{c l}\right)$ in the channel. Therefore,

$$
\begin{equation*}
\text { Throughput }_{i}=\frac{p_{i, s u} \frac{E(P)}{s_{\text {speed }}^{m}}}{P_{f r} \delta+\sum_{i=0}^{a c c^{-1}\left(p_{i, s u} T_{i, s u}\right)+P_{c l} T_{c l}}} . \tag{21}
\end{equation*}
$$

Here $E(P)$ is the expected value of the payload in bits that is transmitted at the MAC speed (speed ${ }_{m}$ ). Also, $\delta$ is the slot-time, $T_{i, s u}$ is the average successful transmission time of a frame of an access category $A C_{i}$ and $T_{c l}$ is the average collision time of a frame as formulated in the subsequent equations.


Fig 2 (a): Timing Sequence for Transmission of RTS/CTS Mode of Standard EDCA for $i_{t h}$ AC.


Fig 2 (b): Timing Sequence for Transmission of Basic Mode of Standard EDCA for $i_{t h}$ AC.
Now, $T^{r t s}{ }_{i, s u}$ and $T^{r t s}{ }_{c l}$ (used in Eq. 21 as $T_{i, s u}, T_{c l}$ ) are formulated for RTS/CTS mode , according to Fig 2 (a)

$$
\begin{align*}
& T^{r t s}{ }_{i, s u}=A I F S[i]+\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{R T S}{\text { speed }_{m}}\right)+\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{C T S}{\text { speed }_{m}}\right)+\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{H_{m}+E(P)+F C S}{\text { speed }_{m}}\right) \\
& +\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{\text { ACK }}{\text { speed }_{m}}\right)+3 \text { SIFS. } \tag{22}
\end{align*}
$$

Also,

$$
\begin{equation*}
T_{c l}^{r t s}=\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{R T S}{\text { speed }_{m}}\right)+\text { SIFS }+ \text { CTSTIMEOUT. } \tag{23}
\end{equation*}
$$

Similarly for the basic access mode, according to Fig 2(b)

$$
\begin{equation*}
T^{\text {bas }}{ }_{i, s u}=A I F S[i]+\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{H_{m}+E(P)+F C S}{\text { speed }_{m}}\right)+S I F S+\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{A C K}{\text { speed }_{m}}\right) . \tag{24}
\end{equation*}
$$

Also,

$$
\begin{equation*}
T^{\text {bas }}{ }_{c l}=\left(\frac{H_{p}}{\text { speed }_{p}}+\frac{H_{m}+E(p)+F C S}{\text { speed }_{m}}\right)+\text { SIFS }+ \text { ACKTIMEOUT. } \tag{25}
\end{equation*}
$$

The notational meaning and the values above of parameters are presented in table1.

Table 1 802.11e PHY/MAC parameters for analysis and simulation

| Payload size <br> $[E(P)]$ | 1024 <br> bytes | MAC speed <br> $\left[\right.$ speed $\left._{m}\right]$ | 11 Mbps |
| :---: | :---: | :---: | :---: |
| Physical Header <br> $\left[H_{p}\right]$ | 192 bits | Slot-time $[\delta]$ | $20 \mu \mathrm{~s}$ |
| Data Frame MAC <br> header $\left[H_{m}\right]+$ FCS | 288 bits | SIFS | $10 \mu \mathrm{~s}$ |
| RTS frame $[R T S]$ | 160 bits | DIFS | $2 * \delta+$ SIFS |
| CTS frame $[C T S]$ | 112 bits | ACKTIMEOUT | DIFS+ACK |
| ACK frame $[A C K]$ | 112 bits | CTSTIMEOUT | DIFS+CTS |
| Physical/channel <br> speed $\left[\right.$ speed $\left._{p}\right]$ | 1 Mbps | AIFS[AC] | SIFS + AIFSN <br> $[A C] * \delta$ |

### 3.2 Saturation delay computation

For the computation of saturation delay, we have followed the model [12] with substantial modifications.

Let $P_{i, s t}$ be the probability that a frame of access category $A C_{i}$, is successfully transmitted. $P_{i, s t}$ is calculated by summing up the probabilities of the successful transmission cases from the first attempt of transmission (with $r=0$ ) to the retry limit $r_{i, m}$. Now the probability of $r_{t h}$ successful transmission case is: $\left(p_{i, c l}\right)^{r}\left(1-p_{i, c l}\right)$. Therefore

$$
\begin{equation*}
P_{i, s t}=\sum_{r=0}^{r_{i, m}}\left(p_{i, c l}\right)^{r}\left(1-p_{i, c l}\right)=1-\left(p_{i, c l}\right)^{r_{i, m}+1} . \tag{26}
\end{equation*}
$$

Let $R_{i, b s}$ be a random variables respectively to denote the total number of back-off slots that a frame of $A C_{i}$ passes through during the pre-transmission back-off process, till it is successfully transmitted through any of the back-off stages $r \in\left[0, r_{i, m}\right]$. When a frame has successful transmission through a back-off stage $r$, it performs back-off in all stages from stage 0 to $r$. The average number of back-off slots that a frame passes through, during its back-off process at any arbitrary back-off stage u is: $\sum_{n=1}^{W_{i, u}-1} \frac{n}{W_{i, u}}$. Therefore, total number of back-off slots a frame undergoes when it has successful transmission through a back-off stage $r$ is: $\sum_{u=0}^{r} \sum_{n=1}^{W_{i, u}-1} \frac{n}{W_{i, u}}$. Now the conditional probability of successful transmission of a frame through back-off stage $r$ is: $\frac{p_{i, c l}^{r}\left(1-p_{i, c l}\right)}{P_{i, s t}}$. Therefore the expected value of the total number of back-off slots i.e. $E\left(R_{i, b s}\right)$, is given by

$$
\begin{equation*}
E\left(R_{i, b s}\right)=\sum_{r=0}^{r_{i, m}} \frac{p_{i, c l}^{r}\left(1-p_{i, c l}\right)}{P_{i, s t}} \sum_{u=0}^{r} \sum_{n=1}^{W_{i, u}-1} \frac{n}{W_{i, u}} \tag{27}
\end{equation*}
$$

Let $R_{i, b f}$ be random variables to denote the total instances back-off counter freezing that a frame of access category $A C_{i}$ passes through during the back-off process, till it is successfully transmitted through any of the back-off stages $r \in\left[0, r_{i, m}\right]$. Since the expected
value of total instances back-off counter freezing i.e. $E\left(R_{i, b f}\right)$ is proportional to $E\left(R_{i, b s}\right)$ and $p_{i, s b}$ as per Eq. (14), hence

$$
\begin{equation*}
E\left(R_{i, b f}\right)=E\left(R_{i, b s}\right) \frac{p_{i, s b}}{p_{i, s b}+p_{i, s b}} . \tag{28}
\end{equation*}
$$

Let $R_{i, r t}$ be a random variable denoting the total number of retransmissions, for a frame of $A C_{i}$, before its successful transmission. Hence, through the similar reasoning

$$
\begin{equation*}
E\left(R_{i, r t}\right)=\sum_{r=0}^{r_{i, m}} \frac{r\left(p_{i, c l}\right)^{r}\left(1-p_{i, c l}\right)}{P_{i, s t}} \tag{29}
\end{equation*}
$$

Let $F_{R A M E} E_{i, \text { delay }}$ be a random variable denoting the total saturation frame access delay for a frame of access category $A C_{i}$, before its successful transmission. Therefore, for the RTS/CTS and basic mode

$$
\begin{equation*}
E\left(F R A M E_{i, \text { delay }}\right)=E\left(R_{i, b s}\right) \delta+E\left(R_{i, b f}\right) T_{i, b f}+E\left(R_{i, r t}\right)\left(T_{i, c s}+T_{c l}\right)+\left(T_{i, c s}+T_{i, s u}\right) . \tag{30}
\end{equation*}
$$

Where $T_{i, b f}$ and $T_{i, c s}$ are respectively the time spent in each instance of back-off counter freezing and carrier sensing for an $A C_{i}$. We calculate $T_{i, b f}$ and $T_{i, c s}$ in the following way:

To calculate $T_{i, b f}$, let Delay ( $i, r, k, \mathrm{~d}$ ) be the delay of the state ( $i, r, k, \mathrm{~d}$ ) due to freezing w. r. $t$ the state $(i, r, k, 0)$. Following the chain relationship of the Markov chain for the back-off counter freezing, for $0 \leq r \leq r_{i, m}, 1 \leq k \leq W_{i, r}-1$, we get

$$
\begin{equation*}
\operatorname{Delay}(i, r, k, d)=\operatorname{Delay}(i, r, k, d-1)+\delta, \operatorname{AIFS}[i]+1 \leq d \leq \operatorname{AIFS}[i]+T_{i} . \tag{31}
\end{equation*}
$$

For the remaining frozen states

$$
\begin{align*}
& \text { Delay }(i, r, k, d)=p_{i, s b} \operatorname{Delay}\left(i, r, k, \operatorname{AIFS}[i]+T_{i}\right)+p_{i, s f} \operatorname{Delay}(i, r, k, d-1)+\delta \\
& 1 \leq d \leq \operatorname{AIFS}[i] . \tag{32}
\end{align*}
$$

Therefore,

$$
\begin{equation*}
T_{i, b f}=\operatorname{Delay}\left(i, r, k, \operatorname{AIFS}[i]+T_{i}\right)-\operatorname{Delay}(i, r, k, 0) \tag{33}
\end{equation*}
$$

Since all the delays are calculated w.r.t. state $(i, r, k, 0)$ we can assume

$$
\begin{equation*}
\operatorname{Delay}(i, r, k, 0)=0 . \tag{34}
\end{equation*}
$$

The equation number (31) to (34) gives rise to $\operatorname{AIFS}[i]+T_{i}+2$ number of equations (for $0 \leq i \leq a c_{m}-1$ ) with equal number of variables, which are solved for Delay ( $i, r, k, d$ ) for $O \leq d \leq \operatorname{AIFS}[i]+T_{i}$ and $T_{i, b f}$.

To calculate $T_{i, c s}$, let Delay ( $i, c, 0, d$ ) be the delay of the state $(i, c, 0, d$ ) due to carrier sensing w.r. $t$ the state $(i, c, 0,0)$. Following the chain relationship of the Markov chain for the pre-back-off carrier sensing, we get

$$
\begin{equation*}
\operatorname{Delay}(i, c, 0, d)=\operatorname{Delay}(i, c, 0, d-1)+\delta, \operatorname{AIFS}[i]+1 \leq d \leq \operatorname{AIFS}[i]+T_{i} . \tag{35}
\end{equation*}
$$

Now, for the remaining frozen states

$$
\begin{align*}
& \operatorname{Delay}(i, c, 0, d) \\
& =\quad p_{i, s b} \operatorname{Delay}\left(i, c, 0, \operatorname{AIFS}[i]+T_{i}\right)+p_{i, s f} \operatorname{Delay}(i, c, 0, d-1)+\delta, \quad 1 \leq d \leq \operatorname{AIFS}[i] . \tag{36}
\end{align*}
$$

Therefore,

$$
\begin{equation*}
T_{i, c s}=\operatorname{Delay}(i, c, 0, \operatorname{AIFS}[i])-\operatorname{Delay}(i, c, 0,0) . \tag{37}
\end{equation*}
$$

Since all the delays are calculated w.r.t. state (i,c,0,0) we can assume

$$
\begin{equation*}
\text { Delay }(i, c, 0,0)=0 . \tag{38}
\end{equation*}
$$

The equation number (35) to (38) give rise to $\operatorname{AIFS}[i]+T_{i}+2$ number of equations with equal number of variables, which are solved for Delay ( $i, c, 0, d$ ) for $0 \leq d \leq \operatorname{AIFS}[i]+T_{i}$ and $T_{i, c s}$.

## 4. Validation of model

The number of simultaneous active ACs within a station in our model is theoretically unlimited. But for simplicity and without the loss of generality, we have considered 4 ACs i.e. $A C_{0}, A C_{1}, A C_{2}$ and $A C_{3}$ to satisfy the requirements of IEEE 802.11e EDCA standard. Here, $A C_{0}$ is the lowest and $A C_{3}$ is the highest priority access category. For service differentiation, each access category $A C_{i}(0 \leq i \leq 3)$ has its own parameter values like Arbitration Inter-Frame Space Number $\operatorname{AIFSN}_{i}$, Minimum Contention Window $W_{i, 0}$, Maximum Contention Window $W_{i, m}$ and retry Limit $r_{i, m}$. This is presented in the following sets: AIFSN set $=\left\{\operatorname{AIFSN}_{0}\right.$, AIFSN $_{1}$, AIFSN $_{2}$, AIFSN $\left._{3}\right\} ; \quad W_{0}$ set $=\left\{W_{0,0}, W_{1,0}, W_{2,0}, W_{3,0}\right\}, W_{m}$ set $=\left\{W_{0, m}, W_{1, m}, W_{2, m}, W_{3, m}\right\} \quad$ and $R_{m}$ set $=\left\{r_{0, m}, r_{1, m}, r_{2, m}, r_{3, m}\right\}$. We have incorporated the following inequalities for service differentiation between ACs: $W_{0,0}>W_{1,0}>W_{2,0}>W_{3,0} ; \operatorname{AIFSN}_{0}>\operatorname{AIFSN}_{1}>$ $\operatorname{AIFSN}_{2}>\operatorname{AIFSN}_{3}$.We have investigated the performance features of EDCA with the variations of $A I F S N_{i}$ and $W_{i, 0}$ parameters for each $A C_{i}(0 \leq i \leq 3)$. we have also studied the effect of internal collision handling on the performance of EDCA.

### 4.1 Comparison of simulation and analytical results

The simulation of the proposed model has been carried out in NS2 [27] network simulator. NS2 is the most popular network simulator among the researchers because of its open source code and continuous development process. We have extended NS2 by adding additional code in $\mathrm{C}++$ and linking it to the existing code. For simulation purpose, we have considered 4 ACs per station. We have used constant bit rate traffic with its rate higher than the link capacity to implement the saturation traffic condition. Also, each AC within a station transmits fixed size UDP packets. For performance measurement, we have repeated simulations 25 times for each case. The final results of simulations are obtained by taking their average. All the parameters used for numerical computations and simulation purpose are listed in table 1 . The physical header is transmitted at 1 mbps , physical /channel bit rate. The AC transmits the MAC header, payload and FCS at 11 mbps (MAC) bit rate.

Comparisons of analytical values TPT-AC0, TPT-AC1, TPT-AC2, TPT-AC3 to simulation values TPT-AC0-simu, TPT-AC1-simu, TPT-AC2-simu and TPT-AC3-simu of table 2 for throughput and analytical values DLY-AC0, DLY-AC1, DLY-AC2 DLY-AC3 to simulation values DLY-AC0-simu, DLY-AC1-simu, DLY-AC2-simu, DLY-AC3-simu of table 3 for delay, show that the simulation results of throughput and delay matches well to the corresponding analytical values.

Table 2 Comparisons of analytical saturation throughput values with simulation results for RTS-CTS mode. $W_{0}$ set $=\{32,16,8,4\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

| Number of stations $\downarrow$ | RTS/CTS THROUGHPUT <br> (ANALYTICAL) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | TPT-AC0 | TPT-AC1 | TPT--AC2 | TPT--AC3 |
| 10 | 0.0240232 | 0.0493119 | 0.104185 | 0.571863 |
| 30 | 0.0283589 | 0.0573533 | 0.117334 | 0.524607 |
| 50 | 0.0291765 | 0.058777 | 0.119286 | 0.511991 |
| 70 | 0.0294487 | 0.0592186 | 0.119745 | 0.505019 |
| Number of | RTS/CTS THROUGHPUT (SIMULATION) |  |  |  |
| stations $\downarrow$ | TPT- AC0-simu | TPT-AC1-simu | TPT- AC2-simu | TPT-AC3-simu |
| 10 | 0.0234226 | 0.04849 | 0.103143 | 0.568499 |
| 30 | 0.026232 | 0.0544856 | 0.113814 | 0.515349 |
| 50 | 0.0255294 | 0.0538789 | 0.113322 | 0.496932 |
| 70 | 0.0242952 | 0.0523098 | 0.111363 | 0.484224 |

Table 3 Comparisons of analytical saturation delay values with simulation results for RTS-CTS mode. $W_{0}$ set $=\{32,16,8,4\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

| Number of stations | RTS/CTS DELAY (seconds) <br> (ANALYTICAL) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | DLY-ACO | DLY-AC1 | DLY-AC2 | DLY-AC3 |
| 10 | 0.0988839 | 0.0487648 | 0.0235815 | 0.00503722 |
| 30 | 0.165004 | 0.0821613 | 0.0406335 | 0.00980654 |
| 50 | 0.206411 | 0.103008 | 0.0512031 | 0.012618 |
| 70 | 0.235792 | 0.11778 | 0.0586725 | 0.0145771 |
| Number of stations $\downarrow$ | RTS/CTS DELAY (seconds) (SIMULATION) |  |  |  |
|  | DLY-ACO-.simu | DLY-AC1-simu | DLY--AC2-simu | DLY-AC3-simu |
| 10 | 0.0984344 | 0.048521 | 0.0234131 | 0.00497425 |
| 30 | 0.162754 | 0.0809289 | 0.0397628 | 0.00943879 |
| 50 | 0.20172 | 0.100433 | 0.0493744 | 0.0118294 |
| 70 | 0.22829 | 0.113658 | 0.0557389 | 0.0133016 |

### 4.2 Service differentiation

For both RTS/CTS and basic mode with any $W_{0}, R_{m}$ and AIFSN set, for any number of stations, the throughput and delay maintains the following inequalities: Throughput $_{\mathrm{AC} 3}>$ Throughput $_{\mathrm{AC} 2}>$ Throughput $_{\mathrm{AC} 1}>$ Throughput $_{\mathrm{AC} 0}$ (table 4) and Delay $_{\mathrm{AC} 3}<$ Delay $_{\mathrm{AC} 2}<$ Delay $_{\mathrm{AC} 1}<$ Delay $_{\mathrm{AC} 0}$ (table 5). This service differentiation is because of the following in-built inequalities of the model: $W_{0,0}>W_{1,0}>W_{2,0}>$ $W_{3,0} ; \operatorname{AIFSN}_{0}>\operatorname{AIFSN}_{1}>\operatorname{AIFSN}_{2}>\operatorname{AIFSN}_{3}$ and also due to the implementation of the internal collision handler.

Table 4 Saturation throughput comparisons between RTS/CTS and basic mode. $W_{0}$ set $=\{32,16,8,4\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

| Number of stations $\downarrow$ | RTS/CTS THROUGHPUT |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | ACO | AC1 | AC2 | AC3 |
| 10 | 0.0240232 | 0.0493119 | 0.104185 | 0.571863 |
| 30 | 0.0283589 | 0.0573533 | 0.117334 | 0.524607 |
| 50 | 0.0291765 | 0.058777 | 0.119286 | 0.511991 |
| 70 | 0.0294487 | 0.0592186 | 0.119745 | 0.505019 |
| Number of stations $\downarrow$ | $\begin{gathered} \text { Basic } \\ \text { THROUGHPUT } \end{gathered}$ |  |  |  |
|  | ACO | AC1 | AC2 | AC3 |
| 10 | 0.017025 | 0.0349469 | 0.0738349 | 0.405274 |
| 30 | 0.0177637 | 0.0359255 | 0.0734971 | 0.328609 |
| 50 | 0.0170543 | 0.0343563 | 0.0697254 | 0.299269 |
| 70 | 0.0163553 | 0.032889 | 0.0665043 | 0.280479 |

Table 5 Saturation delay comparisons between RTS/CTS and Basic mode. $W_{0}$ set $=\{32,16,8,4\}, R_{m}$ set $=$ $\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

| Number of stations $\downarrow$ | $\begin{gathered} \text { RTS/CTS } \\ \text { DELAY (seconds) } \end{gathered}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | ACO | AC1 | AC2 | AC3 |
| 10 | 0.0988839 | 0.0487648 | 0.0235815 | 0.00503722 |
| 30 | 0.165004 | 0.0821613 | 0.0406335 | 0.00980654 |
| 50 | 0.206411 | 0.103008 | 0.0512031 | 0.012618 |
| 70 | 0.235792 | 0.11778 | 0.0586725 | 0.0145771 |
| Number of stations $\downarrow$ | BASICDELAY (seconds) |  |  |  |
|  | ACO | AC1 | AC2 | AC3 |
| 10 | 0.138553 | 0.068657 | 0.0335616 | 0.00759115 |
| 30 | 0.260258 | 0.129999 | 0.0647526 | 0.016226 |
| 50 | 0.347891 | 0.174057 | 0.0870305 | 0.0221187 |
| 70 | 0.417338 | 0.20893 | 0.104619 | 0.0267048 |

### 4.3 RTS/CTS and basic mode comparison

With the same $W_{0}$ set $=\{32,16,8,2\}, R_{m}$ set $=\{8,8,8,8\}$ and AIFSN set $=$ $\{7,5,3,2\}$, it is observed that, for any number of stations, for any $A C_{i}$, the normalized saturation throughput for RTS/CTS mode is always higher than that of the basic mode as shown in table 4 and the saturation delay for RTS/CTS mode measured in seconds is always lower than that of the basic mode as shown in table 5, because of lesser collision loss of RTS/CTS mode.


Fig 3: RTS/CTS Throughput with the Variation of Contention Window. For Case W1: $W_{o}$ Set $=\{16,8,4,2\}$, for Case W2: $W_{o}$ Set $=\{48,24,12,2\}$. For Both the Cases, AIFSN set $=\{7,5,3,2\}, R_{m}$ set $\{8,8,8,8\}$.


Fig 4: RTS/CTS Delay with the Variation of Contention Window. For Case W1: $W_{o}$ Set $=\{16,8,4,2\}$, for Case W2: $W_{o}$ Set $=\{48,24,12,2\}$. For Both the Cases, $\operatorname{AIFSN}$ Set $=\{7,5,3,2\}, R_{m} \operatorname{Set}\{8,8,8,8\}$.

### 4.4 Effect of Contention Window variation

To show the effect of contention window variation on saturation throughput (Fig 3) and saturation delay (Fig 4) of RTS/CTS mode, we have considered two different cases of contention windows i.e. W1 and W2. For case W1: $W_{0}$ set $=\{16,8,4,2\}$ and for case W2: $W_{0}$ set $=\{48,24,12,2\}$. In both the cases the contention window of access category $A C_{3}$ is kept at the same low value of 2 , whereas in case W 2 , the contention window values of $A C_{2}, A C_{1}$ and $A C_{0}$ are kept at higher values. Because of this, access category $A C_{3}$ gets more chances of winning the channel in case W 2 , due to its comparatively lesser waiting time in pre-transmission back-off process. Therefore, the throughput of $A C_{3}$ in case W 2 (Fig 3) increases and the delay of access category $A C_{3}$ in case of W 2 (Fig 4) decreases. The throughput and delay of access categories $A C_{2}, A C_{1}, A C_{0}$ in case of W 2 follows the reverse trend.

### 4.5 Effect of Contention Window variation on total throughput

From table 6, it is observed that as the contention window set $W_{0}$ is moved from $=\{16,8,4,2\}$ to $\{64,32,16,2\}$, the total saturation throughput keeps on increasing. This is because, in the latter contention window sets, the spread of the contention window values from lower to higher ACs increases. Therefore, the total collision probability in the channel decreases and the total throughput increases.

Table 6 Total throughput with contention window $W_{0}$ set variation for RTS/CTS mode.

$$
R_{m} \text { set }=\{8,8,8,8\}, \text { AIFSN set }\{7,5,3,2\}
$$

| RTS/CTS TOTAL THROUGHPUT |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $W_{\text {o set }} \rightarrow$ | $\{16,8,4,2\}$ | $\{32,16,8,2\}$ | $\{48,24,12,2\}$ | $\{64,32,16,2\}$ |  |  |
| Number of <br> Stations $\downarrow$ | THROUGHPUT <br> TOTAL | THROUGHPUT <br> TOTAL | THROUGHPUT <br> TOTAL | THROUGHPUT <br> TOTAL |  |  |
| 10 | 0.707458 | 0.749383 | 0.76946 | 0.781151 |  |  |
| 30 | 0.684174 | 0.727653 | 0.749653 | 0.762909 |  |  |
| 50 | 0.675478 | 0.71923 | 0.741562 | 0.755112 |  |  |
| 70 | 0.669513 | 0.713431 | 0.735897 | 0.749562 |  |  |

### 4.6 Effect of AIFSN variation

To show the effect of AIFSN variation on saturation throughput (Fig 5) and saturation delay (Fig 6) of RTS/CTS mode, we have considered two different cases of AIFSN i.e. A1 and A2. For case A1: AIFSN set $=\{7,5,3,2\}$ and for case A2: AIFSN set $=\{10,7,5,2\}$. In both the cases, the AIFSN values of access category $A C_{3}$ is kept at the same low value of 2 , whereas, in case A2, the AIFSN values of access categories $A C_{2}, A C_{1}$ and $A C_{0}$ are kept at higher values. Because of this, access category $A C_{3}$ get more chances of winning the channel in case W 2 , due to its comparatively much lesser waiting time in pre-back-off carrier sensing process. Therefore, the throughput of $A C_{3}$ in case of A2 (Fig 5) increases and the delay of the $A C_{3}$ of case of A2 (Fig 6) decreases. The throughput and delay of access categories $A C_{2}, A C_{1}$ and $A C_{0}$ of case A 2 follows the reverse pattern.


Fig. 5 RTS/CTS Throughput with the Variation of AIFSN Value. For Case A1, AIFSN Set $=\{7,5,3,2\}$, for Case A2, AIFSN Set $=\{10,7,5,2\}$. For Both the Cases, $W_{0}$ set $=\{16,8,4,2\}, R_{m}$ set $\{8,8,8,8\}$.


Fig. 6 RTS/CTS delay with the Variation of AIFSN Value. For Case A1, AIFSN set $=\{7,5,3,2\}$, for Case A2, AIFSN Set $=\{10,7,5,2\}$. For Both the Cases, $W_{0}$ Set $=\{16,8,4,2\}, R_{m}$ set $\{8,8,8,8\}$.

### 4.7 Effect of Internal collision handler

To compare the performance results without and with internal collision handler of RTS/CTS mode for normalized saturation throughput and saturation delay we have considered same $W_{0}$ set $=\{5,4,3,2\}, R_{m}$ set $=\{8,8,8,8\}$ and AIFSN set $=\{7,5,3,2\}$ in both cases. From the table 7 and table 8 for saturation throughput and table 9 and table 10 for saturation delay, the following observations are made:
(a) For throughput, there is highest increase for $A C_{3}$ and highest decrease for $A C_{0}$ with internal collision handler compared to that without the internal collision handler. This is expected due to highest favor of internal collision handler to highest Access

Category. The throughput of intermediate ACs i.e. $A C_{2}$ and $A C_{1}$ are also decreased with $A C_{1}$ having higher decrease due to the same reason. Also, due to the same reason, the saturation delay pattern follows the reverse trend.
(b) The effect of internal collision is most dominant at the lower number of stations as expected and it fades away at the higher number of stations due to more external collisions.

Table 7 Saturation throughput of RTS/CTS mode without and with internal collision handler. $W_{0}$ set = $\{5,4,3,2\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.


Table 8 Saturation throughput increase (\%) of RTS/CTS mode with internal collision handler, compared to that without internal collision handler. $W_{0}$ set $=\{5,4,3,2\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

| Number of stations $\downarrow$ | RTS/CTS \% THROUGHPUT INCREASE WITH INTERNAL COLLISION HANDLER |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | ACO | AC1 | AC2 | AC3 |
| 2 | -44.6922 | -42.2042 | -37.7153 | 27.5543 |
| 6 | -15.6097 | -11.5297 | -4.81518 | 11.7378 |
| 10 | -9.00015 | -6.10224 | -1.76493 | 6.51708 |
| 18 | -4.62776 | -2.94102 | -0.592574 | 3.23044 |
| 34 | -2.17722 | -1.33075 | -0.202107 | 1.47265 |
| 50 | -1.23008 | -0.73752 | -0.102576 | 0.812884 |

Table 9 Saturation delay of RTS/CTS mode without and with internal collision handler. $W_{0}$ set $=\{5,4,3,2\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

|  | RTS/CTS DELAY (seconds) <br> WITHOUT INTERNAL COLLISION HANDLER |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Number of stations $\downarrow$ | ACO | AC1 | AC2 | AC3 |
| 2 | 0.0107001 | 0.00840443 | 0.00603405 | 0.00229723 |
| 6 | 0.0167376 | 0.0135739 | 0.0103751 | 0.00563709 |
| 10 | 0.0217559 | 0.0178126 | 0.0138268 | 0.00771689 |
| 18 | 0.0292141 | 0.0240947 | 0.0189036 | 0.0106049 |
| 34 | 0.0392364 | 0.0325491 | 0.0257279 | 0.0142011 |
| 50 | 0.0475868 | 0.0396345 | 0.0314736 | 0.0169068 |
| Number of stations $\downarrow$ | RTS/CTS DELAY (seconds)WITH INTERNAL COLLISION HANDLER |  |  |  |
|  | ACO | AC1 | AC2 | AC3 |
| 2 | 0.0163569 | 0.0123673 | 0.00860359 | 0.00160043 |
| 6 | 0.0190883 | 0.0148763 | 0.0108773 | 0.00440085 |
| 10 | 0.0237173 | 0.0189065 | 0.014294 | 0.0064547 |
| 18 | 0.0309604 | 0.0251402 | 0.0194933 | 0.00941265 |
| 34 | 0.0406779 | 0.0334252 | 0.0263165 | 0.0132702 |
| 50 | 0.04838 | 0.0399533 | 0.0316516 | 0.0163956 |

Table 10 Saturation delay increase (\%) of RTS/CTS mode with internal collision handler, compared to that without internal collision handler. $W_{0}$ set $=\{5,4,3,2\}, R_{m}$ set $=\{8,8,8,8\}$, AIFSN set $\{7,5,3,2\}$.

|  | RTS/CTS \% DELAY INCREASE WITH INTERNAL COLLISION HANDLER |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Number of stations | ACO | AC1 | AC2 | AC3 |
| 2 | 52.8668 | 47.1522 | 42.584 | -30.3322 |
| 6 | 14.0444 | 9.59488 | 4.84044 | -21.9305 |
| 10 | 9.01549 | 6.14116 | 3.37895 | -16.3562 |
| 18 | 5.97759 | 4.33913 | 3.11951 | -11.2424 |
| 34 | 3.67388 | 2.69163 | 2.28779 | -6.55513 |
| 50 | 1.66685 | 0.80435 | 0.565553 | -3.02364 |

## 5. Conclusion

In the analytical model of this research article, we have studied the performance features of EDCA mode of operation of WLAN based on IEEE 802.11e standard. From the analytical and simulation results discussed in section 4 , we draw the following conclusions:

1. Analytical and simulation results match well for both normalized saturation throughput and saturation delay and validate our model.
2. The throughput and delay pattern of standard EDCA shows the access category wise QoS differentiation feature, with higher ACs having higher throughput and lower delay. This shows that EDCA is suitable for soft real-time application, when the latter is being run through higher ACs.
3. RTS/CTS mode is better than the basic mode for both throughput and delay because of less collision loss.
4. Contention window and AIFSN variation is very effective means of service differentiation between the ACs.
5. Internal collision handler has dominating effect on system performance enhancement for higher ACs at lower load.

## In this research article, our key research contributions are:

(i) Implementation of pre-back-off carrier sensing with actual deferred states.
(ii) Implementation of back-off counter freezing during the channel sensing of pretransmission back-off process with actual deferred states followed by carrier sensing with deferred states.
(iii) The contemporary EDCA models have implemented only one or at best two priority class active ACs per station whereas we have incorporated multiple number of simultaneously active ACs within each station (theoretically unlimited) denoted by $a c_{m}$, in the same solution framework.
(iv) To implement $a c_{m}$ (theoretically unlimited) number of ACs per station, we have solved a total of $\left(7 * a c_{m}+4\right)$ numbers of non-linear equations, depending on the value of $a c_{m}$, in the same solution framework.
(v) We have elaborately demonstrated the effect of internal collision handler on the performance of EDCA and established the fact that at low load, the internal collision handler plays a very crucial role in the performance enhancement of EDCA, making it more suitable for real-time applications.
(vi) We have implemented frame discarding after retry limit which reduces excessive frame access delay.
(vii) We have also implemented post-back-off after successful transmission to add fairness to the EDCA mode of operation.

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