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# Parameterization of Micro Satellite Launch Vehicle

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#### **Abstract**

The new trends in micro satellites mission for wide range of applications has motivated worldwide research in design and development of micro satellite launch vehicles (MSLVs) as a vital options in the deployment of such satellites into their respective mission orbits. Presently, most micro satellites are launched through rideshares with rockets or rocket-like systems, which were developed essentially in the seventieth and eightieth of the last century.

The MSLV as a proportional micro satellite launch vehicle, up till now has only the status of technology and system study work and is well known that the research and development of MSLV are diversified in different fields. However, the realization of MSLVs is rigorous since such vehicles compound the inherent difficulties of traditional launch experiment with intrinsic problems of uneven mass distribution, slenderness, high frequency and amplitude of vibration etc. MSLV are also more likely to be affected by wind gusts and other disturbances than their conventional counterpart, and the physical parameters such as mass distribution and moments of inertia can be easily altered by changing the payload location and unpredictable propellant burning. All these factors compromise the additional velocities to overcome the aerodynamic drag, to account for steering of the vehicle and other losses.

Consequently, We prototype a three stage micro-satellite launch equipment as a similitude of the European Space Agency's VEGA launcher using a scale down derivation model and parameterized using existing VEGA launch vehicle (LV) technical data. VEGA launch data, total orbital velocity requirement including the losses and stage payload ratio are inferred and applied to the model of parameterization of launch vehicles through coupled-parameters simulations. This approach can be helpful in viability and performance insights in terms of payload mass, stage mass distribution and material properties precision and effectiveness. It can also serve as a background for the development of time optimal waypoint trajectory of micro satellite launchers.

**Keywords:** Micro-electromechanical systems Microsatellites; Launch vehicles; VEGA

(MEMS);

#### Nomenclature

L<sub>1</sub>=Length of the first stage of the rocket

 $L_2$ =Length of the second of the rocket

L<sub>3</sub>=Length of the third stage of the rocket

L<sub>n</sub>=Length of the first stage of the rocket

m<sub>pl</sub>=Initial mass of the propellant of the first stage

 $m_{p2}$ =Initial mass of the propellant of the second stage

m<sub>n3</sub>=Mass of the payload (parabolic nose-cone)

T<sub>1</sub>=Thrust of the 1<sup>st</sup> stage

I<sub>sp. 1</sub>=Specific impulse of the 1<sup>st</sup> stage in sec

T<sub>2</sub>=Thrust of the 2<sup>nd</sup> stage

 $I_{sp,2}$ =Specific impulse of the  $2^{nd}$  stage in sec

T<sub>3</sub>=Thrust of the 3<sup>rd</sup> stage

I<sub>sp 3</sub>=Specific impulse of the 3<sup>rd</sup> stage in sec

#### Introduction

Evolving trends in technological development, e-commerce, governance and medicare urgently demand the decentralization and proliferation of space missions. This call is further intensified by the need for continuous high resolution information to address some of the emerging challenges of the new world. These include terrorism, natural disasters and resource scarcity. A timely and effective response to this

quest is high frequency deployment of dedicated satellites into space. To this end, advances in nanotechnology and micro-electromechanical systems (MEMS) have led to the emergence of microsatellites [1]. Ironically, launch equipment are not shedding weight and cost at a rate commensurate to their payloads. Therefore, satellites have to aggregate before making their trip to space. In view of this challenge, concerted efforts are ongoing in aerospace research and development communities to develop robust and cost effective microsatellite launch vehicles. On this basis, demand for launches has been growing steadily as people discover that continuous devolution in sizes of orbiting satellite can still handle missions previously performed by much larger satellites. The success and effective deployment of such Satellites into orbits however depends on the elements of space transportation such as ground based Launch vehicles.

Whatever the previous specifics method of deploying previous micro satellites to orbit, the natural continuation of research and development in the areas of micro satellites platforms requires vigorous complementary development in safe, affordable and sustainable launch vehicles, that is to say, the launch vehicle must be matched to the micro

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satellite mission if costs are to be minimized. Excess launch capacity beyond prudent margins represents wasted costs.

Recognizing that the move toward micro satellites has places added emphasis on the costs and availability of appropriate launchers, many aerospace industry as indicated in Table 1 now placed emphasis on the development of micro launch vehicles tailored specifically to meet this growing market segment.

The biggest challenge of MSLV project is development time and cost. To provide solution to these challenges, one requires unified and monumental efforts in all the major engineering fields. In addition to having an actual launch vehicles, one needs excellent instrument to provide sensor measurements, control actuators to steer the system and algorithms to process the errors and run the control loops. In order to develop the algorithms one also need testing frameworks and some kind of simulation of flights to debug the onboard algorithms. The dimension challenges, layers of dynamics complexity associated with MSLV and the potential of an improved vehicle dynamic model based on a combination of physical laws and empirical data serves as motivation of this study.

Within the framework of this study, we considered a three-stage rocket, using the VEGA rocket as a basis to set the dimensional, wind tunnel, flight parameters and dynamic properties model. The parameterized MSLV is tailored for missions to low Earth orbits and qualified to launch satellites ranging from 10 kg to 20 kg. As a rule, these are low cost satellite missions conducted by research organizations and universities for Earth observations, as well as spy, scientific and amateur mission concepts.

## Geometry and Parameterization of Microsatellite Launch Vehicle

Realistic parameterization of MSLV is necessary condition for detailed design of new launch vehicle in loads analysis, trajectory design and guidance navigation and control mechanization. Two approaches i.e. clean-sheet method and derivatives from existing launch vehicles are commonly employ to design a new launch vehicle system [2]. In this study, constraints budget availability, low cost and the desire for a rapid development preclude clean-sheet method and derivatives of existing conventional launch systems were implemented. The proposed selected architecture of model development of MSLV is derived from existing launch systems that possesses the following attributes:

- · Multistage,
- Expendable or partially reusable,
- Solid Propellant powered Rockets in all stages,
- · Carries all of its required propellant from liftoff, and
- Takes off vertically with no assist from ground-based thrust augmentation.

With these features selected, we parameterize three-stage 2(10 kg) payload capacity micro satellite launch vehicle designed for Low Earth Orbit (LEO) from VEGA Launch Vehicle. VEGA Launch vehicle was developed by the European Space Agency and made its maiden voyage in 2012. Vega is lightweight three-stage all-solid launch vehicle with an optional liquid fueled upper stage for re-start and precise injection capability (fourth stage not considered here). It is designed to launch micro payloads 300 to 2,500 kg satellites for scientific and Earth observation missions to polar and low Earth orbits [3]. VEGA launch vehicle performance data for circular orbit mission with different inclination and altitudes between 300 km 1500 km are presented in figure. The three-stage MSLV employs same specific impulses similar to VEGA, but different structural ratio because of its slender nature which require more rigidity. In the aspect of stage payload ratio of VEGA used for MSLV, The second and third stages' payload ratios are 1.2 and 0.419 times, respectively, than that of the first stage.

In order to use total orbital velocity requirement and payload mass capacity to parameterize MSLV, we modified the Konstantin Tsiolkovsky equation and its corollaries. Real rocket equations accounting for losses can now be are expressed as [4]

$$V_{T} = V_{b} + \delta V \tag{1}$$

On this basis, we model preliminary mass estimator for three stages MSLV designs so that speeds required for placing micro payload into desired orbit  $V_b$  on MSLV can be achieved. The orbital velocity requirement to be delivered by the rocket for a given mission including all the losses due to gravity, atmospheric drag, propulsive losses due to the maneuvering and static pressure difference at the nozzle exit and velocity gain due to launch site  $V_i$  [5] can be stated as:

$$V_b - V_i = \int_0^{t_b} \left[ \frac{T \cos \alpha}{m(t)} - \frac{\mu_E \sin \gamma}{r^2} - \frac{D}{m(t)} + \Omega_E^2 r \cos \phi_L (\cos \phi_L \sin \gamma - \sin \phi_L \cos \gamma \sin \psi) - F_{const} \sin \gamma / m(t) \right] dt$$
 (2a)

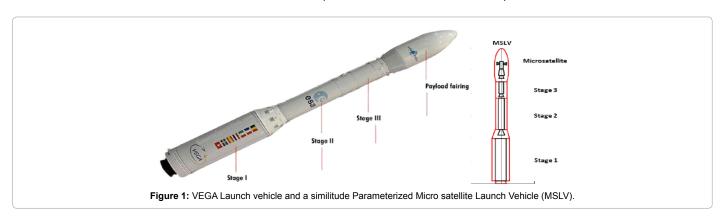
$$V_{b} - V_{i} = \int_{t_{ign}}^{t_{b}} \frac{T}{m(t)} dt - \int_{t_{ign}}^{t_{b}} \frac{T}{m(t)} (1 - \cos \alpha) dt - \int_{t_{ign}}^{t_{b}} \frac{D}{m(t)} dt - \int_{t_{ign}}^{t_{b}} \frac{\mu_{E}}{r^{2}} \sin \gamma dt - \int_{t_{ign}}^{t_{b}} \frac{F_{const}}{m(t)} \sin \gamma dt + \int_{t_{ign}}^{t_{b}} \Omega_{E}^{2} r \cos^{2} \phi_{L} \sin \gamma dt - \int_{t_{ign}}^{t_{b}} \Omega_{E}^{2} r \cos \phi_{L} \sin \phi_{L} \sin \psi dt$$

$$(2b)$$

Where:

Vehicle Name	Organization (Country)	Max Payload Capacity (LEO)	Development Status	Target User/Buyer Markets
Alderbaran	CNES, DLR, CDTI (France, Germany, Spain)	Up to 300 kg	Concept Study	Non-commercial, government science and tech. demo missions
Microsatellite Launch Vehicle	Canadian Space Agency (Canada)	Up to 150 kg	Market Study	
Multipurpose Nanomissible	U.S Army Space and Missile Defence Command (United States)	Apx 23 kg	In design phases	U.S. Government military payloads, operationally responsive space
Neptune 30	Inter orbital Systems (United States)	30 kg	In development	CubeSats, universities and non- profits
Scorpius/Mini-Sprite	Microcosm Inc. (United States)	22 kg	Design	U.S. Military and operationally responsive space     U.S Civil Government     Educational Organizations
Nano-Launcher	IHI Aerospace, USEF, CSP Japan (Japan)	100 kg	Concept Study	Academia and government missions
Virgin Galactic Micro Satellite Launch Vehicles	Virgin Galactic (United States)	100 kg	Indevelopment	Science Missions
NASA NanoSat Launch Challenge (United States)		> 1 kg, twice in one week	Innovation Prize	Cubesats

Table 1: Characteristics of Prospective Microsatellite Launch Vehicle and Operators.



$$\int_{t_{-}}^{t_{b}} \frac{T\cos}{m(t)} dt = \int_{t_{-}}^{t_{b}} \frac{T}{m(t)} dt - \int_{t_{-}}^{t_{b}} \frac{T}{m(t)} (1 - \cos t) dt$$
 (3a)

$$V_b = V_T - \Delta V_{steering} - \Delta V_{drag} - \Delta V_{gravity} - \Delta V_{const} - \Delta V_{earth\ rotation} + \Delta V_i \quad (3b)$$

$$\delta V = \Delta V_{steering} + \Delta V_{drag} + \Delta V_{gravity} + \Delta V_{const} + \Delta V_{earth\ rotation}$$
 (3c)

$$V_{T} = g_{0}I_{sp} \ln \frac{m_{0}}{m_{f}} = \int_{t_{-}}^{t_{b}} \frac{T}{m(t)} dt$$
 (3d)

$$m_0 = m_{pr} + m_f \tag{3e}$$

$$\Delta V_{steering} = \int_{t_{low}}^{t_{b}} \frac{T}{m(t)} (1 - \cos \alpha) dt$$
 (3f)

$$\Delta V_{drag} = \int_{t_{ign}}^{t} \frac{D}{m(t)} dt = \int_{t_{ign}}^{t_b} \frac{D_{power}}{m(t)} dt_b + \int_{t_b}^{t} \frac{D_{coast}}{m(t_b)} dt$$
 (3g)

$$\Delta V_{gravity} = \int_{t_{gin}}^{t} \frac{\mu_E}{r^2} \sin \gamma dt \tag{3h}$$

$$\Delta V_{const} = \int_{t_{lgm}}^{t_b} \frac{F_{const}}{m(t)} \sin \gamma dt$$
 (3i)

$$\Delta V_{earth\_rotation} = \int_{t_{ign}}^{t_h} \Omega^2_E r \cos^2 \phi_L \sin \gamma dt - \int_{t_{ign}}^{t_h} \Omega^2_E r \cos^2 \phi_L \sin \phi_L \sin \psi dt \quad (3j)$$

$$V_i = 0.465 \cos \phi_L \tag{3k}$$

$$V_b = I_{sp}.g \ln(\frac{m_0}{m_f}) = V_0 \left\{ \frac{2}{1 + (\frac{R_E + h}{R_E + h_0})} \right\}^{\frac{1}{2}}$$
(31)

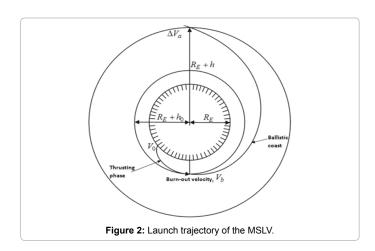
$$V_0 = \left\{ \frac{\mu}{R_E + h_0} \right\}^{\frac{1}{2}} \tag{3m}$$

For elliptical orbit as shown in Figure 2 and considering circularization burn  $\Delta V_a$  out at apogee,

$$\Delta V_{a} = V_{0} \left\{ \frac{R_{E} + h_{0}}{R_{E} + h} \right\}^{\frac{1}{2}} \left\{ 1 - \left[ 1 + \frac{2}{\frac{R_{E} + h}{R_{E} + h_{0}}} \right]^{\frac{1}{2}} \right\}, \tag{4}$$

Each of the terms in the  $\delta V$  represent losses from various forces on the vehicle integrated over the flight path.

 $\Delta V_{steering}$  is the losses due to inefficiency of the thrust vector control system for trajectory control,  $\Delta V_{gravity}$  is the losses due to gravitational forces,  $\Delta V_{drag}$  is the losses due to fluidic retarding effect of the endoatmospheric flight acting the opposite direction of the vehicle velocity



vector,  $\Delta V_{earth\_rotation}$  is losses due to earth rotation while  $\Delta V_{const}$  are the losses during lift off, rain effect and other unknown of unknown. In addition  $V_T$  is the total propulsive force from the propulsion system on the vehicle. It is the sum of the  $V_b$  required to place micro satellite into desired orbit plus all the  $\delta V$  losses,  $\phi_L$  is the launch site latitude,  $h_0$  is desired satellite mission altitude (circular orbit) or perigee for elliptical orbit,  $\mu$  is Earth gravitational parameter, h is circularization orbit and  $R_E$  is Radius of the Earth.

The drag losses are primarily depend on Rocket thrust to total rocket weight ratio  $\left(T/m(t)g\right)$  and on the magnitude of  $\Delta V_{drag}$  which becomes significant due to the slender nature and length of the class of MSLV.

In approach to preliminary mass estimator in this study, we consider an n-stage rocket of payload mass,  $m_{pl}$ , stage structural mass/inert mass,  $m_{\mathrm{int},k}$ , and stage propellant mass,  $m_{pr,k}$ . Thus, the initial mass is

$$m_{ok} = m_{pl} + m_{prk} + m_{ink} + \sum_{n=k+1}^{n} (m_{prn} + m_{inn})$$
 (5)

and the final mass after all the propellant has been consumed is

$$m_{fk} = m_{pl} + m_{ink} + \sum_{n=k+1}^{n} (m_{prn} + m_{inn})$$
 (6)

Where the subscript k denotes quantities pertaining to the stage of the vehicle and it is assumed here that only one stage is burning at a given time, and each stage is discarded immediately after its propellant is consumed.

Relating rocket equation of single stage to multiple stages considered here, [4] showed that the ideal rocket equation burn out velocity for a multi-stage rocket with a total of n stages can be written as follows [5]:

$$V_b = \sum_{i=1}^{n} v_{ek} (\sigma_k + (1 - \sigma_k) \lambda_k$$
 (7)

With consideration that VEGA launch vehicle has accounted for all the anticipated losses and total velocity requirement is Equation. (7), we derive real rocket equations as a function of rocket mass, payload and unperturbed mission orbit as below [4];

$$V_T = \sum_{k=1}^{n} v_{ek} (\sigma_k + (1 - \sigma_k) \lambda_k + \delta V - 0.465 \cos \phi_L$$
 (8)

We use the parameter [6] of VEGA launch vehicle and ideal

trajectory equation 2 to derive the total losses as follows;

$$V_T^{VEGA} = \sum_{k=1}^{n} v_{ek}^{VEGA} (\sigma_k^{VEGA} + (1 - \sigma_k^{VEGA}) \lambda_k^{VEGA}$$
(9)

$$\delta V = V_T^{VEGA} - V_0 \left\{ \frac{2}{1 + \left(\frac{R_E + h}{R_E + h_0}\right)} \right\}^{\frac{1}{2}} - 0.465 \cos \phi_L$$
 (10)

Using the parameters of VEGA Launch vehicle from published manual and Equations. (3l,3m,4,9,10), a Simulink simulation solution was developed to infer the anticipated total velocity losses as shown in Simulink block in Figure 3 for realistic dynamics of the rocket motion.

Substituting Equation. (10) Into Equation. (8),

A real rocket equation formulation suitable for MSLV is proposed as

$$V_{T} = \sum_{i=1}^{n} v_{ek} (\sigma_{k} + (1 - \sigma_{k}) \lambda_{k} + V_{T}^{VEGA} - V_{0} \left\{ \frac{2}{1 + \left(\frac{R_{E} + h}{R_{E} + h_{0}}\right)} \right\}^{\frac{1}{2}} - 0.465 \cos \phi_{L}$$
 (11)

In order to determine the rocket mass distribution, it is required to estimate the payload ratio  $\lambda_k$ , inert mass fraction,  $\delta_k$  and propellant mass fraction  $p_k$ , of the each stage.

The  $\lambda_k$  ,  $\delta_k$  and  $p_k$  , of the each stage is therefore defined as follows

$$\lambda_{k} = \frac{m_{0(k+1)}}{m_{0k}} \tag{12}$$

For multistage rockets considered in this study, rocket payload

$$\lambda_T = \frac{m_{pl}}{m_{01}} = \prod_{k=1}^n \lambda_k \tag{13a}$$

$$\mathcal{S}_k = \frac{m_{in,k}}{m_{pr,k} + m_{in,k}} \tag{13b}$$

$$p_{k} = \frac{m_{pr,k}}{m_{pr,k} + m_{in,k}} \tag{13c}$$

$$\delta_k + p_k = 1 \tag{13d}$$

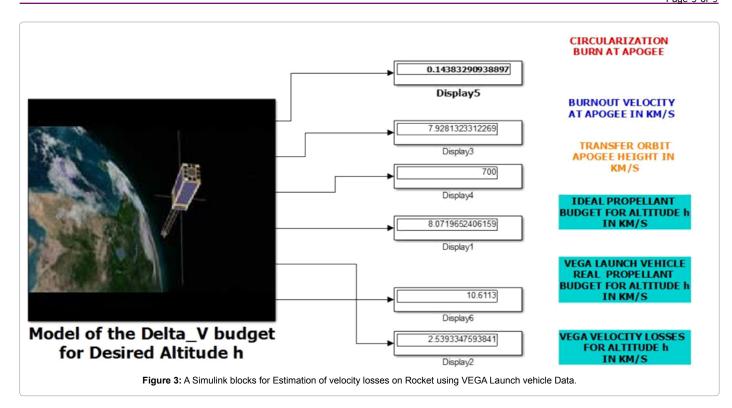
Devolution of VEGA launch vehicle mass for 20 Kg microsatellites [7] payload considered in this study is modeled as;

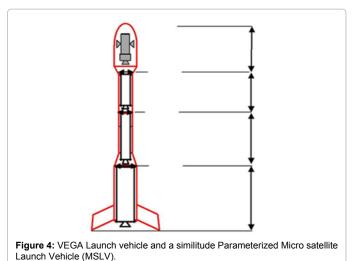
$$m_{01} = \frac{m_{sat}}{\prod_{k=1}^{N} \lambda_k}$$
 for k=1 (14a)

and

$$m_{0(k+1)} = l_k m_{0k} \tag{14b}$$

Propellant mass of each stage is expressed as





 $m_{pk} = (m_{ok} - m_{0(k+1)}) \times (1 - \delta_k)$  (14c)

Last stage propellant mass is

$$m_{nk} = (m_{ok} - m_{sat}) \times (1 - \delta_{kn}) \tag{14d}$$

Mass of the empty structure after power phase for stage k

$$m_{bk} = m_{ok} - m_{pk} \tag{14e}$$

Stage k initial Thrust to Weight Ratio  $\beta_{0k}$ 

$$\beta_{0k} = \frac{T_k}{gm_{ok}} \text{ where } \beta_{0k} > 1$$
 (14f)

Stage k Thrust Level

$$T_k = \beta_{0k} (m_{sk} + m_{pk} + m_{0(k+1)})g$$
(14g)

$$T_k = \beta_{0k} (m_{0(k+1)} + m_{sk}) g \tag{14h}$$

Time duration  $t_{b,k}$  of the power phase of stage k is

$$t_{b,k} = m_{0k} \left( 1 - \frac{m_{bk}}{m_{0k}} \right) \frac{g_0 I_{sp_k}}{T_k} \tag{14i}$$

Total Thrust burn time  $t_k$  of the LV

$$t_k = \sum_{k=1}^{n} t_{b,k} \tag{14j}$$

Instantaneous mass  $m_{0k}(t)$  of Stage k

$$m_{0k}(t) = m_{0k} - m_{pk} \frac{t}{t_{b,k}}$$
 (14k)

where  $0 \le t \le t_{b,k}$ 

We calculate mass distribution of MSLV based on the gross mass of each stage of VEGA LV [8] distributed as

$$m_{0i} = m_{pi} + m_{si} + m_{0(i+0)} (141)$$

The Equations (1-14) above give proportional mass model form n-stage MSLV that can deploy a micro satellite payload to a specified burnout velocity  $V_b$ . In addition to this, mass and propulsive thrust is partition in the numerical solutions as follows:

$$\begin{split} m = & \begin{cases} m_{0,1} - \dot{m}_{p,1}t & t < t_{b,1} \\ m_{0,3} - \dot{m}_{p,3}(t - t_{b,1}) & t \leq t_{b,1} + t_{b,2} \\ m_{0,3} - \dot{m}_{p,3}(t_f - t_{b,2} - t_{b,1}) & t_f \leq t_{b,1} + t_{b,2} + t_{b,3} \end{cases} \\ T = & \begin{cases} T_1 & t \leq t_{b,1} \\ T_2 \leq t_{b,2} + t_{b,2} \\ T_3 & t_f \leq t_{b,1} + t_{b,2} + t_{b,3} \end{cases} \end{split}$$

#### **MSLV Centre of Mass Shift Formulation**

This mathematical model is more representative of a solid-fuel launch vehicle [9] considered in this study (Figure 2). The new model formulation distributed the masses of the rocket m as the sum of dry unloaded rocket  $m_f$  and the instantaneous mass of the propellants  $m_{pr}(t)$  where m is now dependent on both time and the instantaneous distance from the nose tip to the Centre of mass of the rocket  $X_n$ .

$$m(t, X_p) = m_f + m_{pr}(t) \tag{15}$$

The distribution of mass  $\sum_{i=1}^{3} m_i$  on three stage rocket considered in

this study is shown in Figure 1 and used to

i=1 model the distribution of the  $m(t, X_p) = m_f + m_{pr}(t)$ .

Instantaneous mass of the rocket  $m_{mslv} = m_{01} + m_{02} + m_{03} + m_{pl}$ 

The instantaneous propellant load position in the combustion chamber and instantaneous change in Centre of origin of the rocket during the burning of propellant is model as

$$X_p(t) = \frac{m_{01}(t)x_1 + m_{02}(t)x_2 + m_{03}x_3(t) + m_4x_4}{m_{mslv}(t)} - X_{icg} \text{ and}$$

$$X_{icg}(t=0) = \frac{m_{01}x_1 + m_{02}x_2 + m_{03}x_3 + m_{pl}x_4}{m_{mslv}(t=0)}$$
 respectively.

Derived Parameters	1st Stage K=1	2 <sup>nd</sup> Stage k=2	3 <sup>rd</sup> Stage k=3
Structural Mass min, k(KG)	7.431	1.845	793
Gross Mass $m_{ok}$ ( <b>KG</b> )	134,485 Fairing Inclusive	38.199	12.448
Stage Payload Mass $m_{pl}^{}$ ( <b>KG</b> )	38689 Fairing Inclusive	12.448	1500
$\delta_{\scriptscriptstyle k}$	0.0776	0.0716	0.0725
$m_{fk} = m_{0k} - m_{prk}  \mathbf{Kg}$	46.120	14.294	2.293
$R_k = m_{0k} / m_{fk}$	2.9160	2.6725	1.6196
$ln R_k$	1.0702	0.9830	1.6916
$v_{ek} < I_{spk}g$ Km/s	2.7440	2.8322	2.8910
$\Delta V_T pprox \sum_{k}^{n} I_{spk} g \ln R_k$ Km/s	10.61130		

Table 2: Derived  $V_{\it{T}}$  Performance of VEGA Launch Vehicle using Rocket Equation.

Where  $X_p$  is the instantaneous centre of mass of the rocket with respect to initial centre of mass  $X_{\rm icg}$  ,

 $X_{icg}(t=0)$  is the initial centre of mass of the full propellant load from aft end before ignition,  $\mathcal{X}_i$  is the instantaneous centre of mass of each  $i^{th}$  stage,  $m_{mslv}$  is the initial total lift off mass of MSLV,  $m_{mslv}(t)$  is the instantaneous mass of MSLV during each of the stage propellant burning,  $m_f$  is the mass of the dry unloaded rocket,  $m_{pr}$  is the mass of the propellants. The launch vehicle's full mass is calculated as the sum of all current stages with fuel in operating engines, determined in accordance with the current propulsion system's profile of thrust.

The centre of mass of each stage is also defined as follows:

Centre of mass of first stage =  $x_1 = -(L_1/2 + L_2 + L_3 + L_n)$ 

Centre of mass of second stage =  $x_2 = -(L_2/2 + L_3 + L_n)$ 

Centre of mass of third stage =  $x_2 = -(L_3/2 + L_n)$ .

The translational equation of motion can now be re-derived by replacing m(t) with  $m(t, X_p) = m_f + m_{pr}(t)$  Therefore;

$$\vec{F} = m(t, X_p) \frac{d\vec{V}}{dt} + 2m(t, X_p) \overrightarrow{\omega_e} \times \vec{V} + m(t, X_p) \overrightarrow{\omega_e} \times (\overrightarrow{\omega_e} \times \vec{r})$$
 (16)

On this basis, the governing equations of motion on system dynamics suitable for flight of a three stage MSLV model as slender, distributed mass (Figure 4) and variable point mass with internal flow over rotating and spherical Earth is defined and can form the basis for improved mathematical models of translational motion of MSLV. The model can also reveal the effect of lumped masses on the stability of slender body with internal flow where the system has several point masses at various locations numbers.

## **Derivatives of MSLV from VEGA Launch Vehicle**

The no dimensional rocket equation for a 3-stages rocket can thus be written as follows [4] (Table 2):

$$\frac{V_T}{v_{ek}} = -\sum_{k=1}^{3} \beta_{ek} (\sigma_k + (1 - \sigma_k) \alpha_k$$
 (17)

Where

$$\sigma_k^{MSLV} = \left[ \frac{\delta_1^{MSLV}}{\delta_1^{MSLV}} \frac{\delta_2^{MSLV}}{\delta_1^{MSLV}} \frac{\delta_3^{MSLV}}{\delta_1^{MSLV}} \right]$$
(18a)

$$\alpha_k^{MSLV} = \left[ \frac{\lambda_1^{MSLV}}{\lambda_1^{MSLV}} \frac{\lambda_2^{MSLV}}{\lambda_1^{MSLV}} \frac{\lambda_3^{MSLV}}{\lambda_1^{MSLV}} \right]$$
(18b)

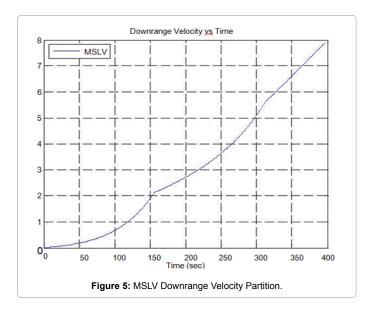
$$\boldsymbol{\beta}_{ek}^{VEGA} = \begin{bmatrix} v \boldsymbol{e}_1^{VEGA} & v \boldsymbol{e}_2^{VEGA} & v \boldsymbol{e}_3^{VEGA} \\ v \boldsymbol{e}_1^{VEGA} & v \boldsymbol{e}_3^{VEGA} & v \boldsymbol{e}_3^{VEGA} \end{bmatrix}$$
(18c)

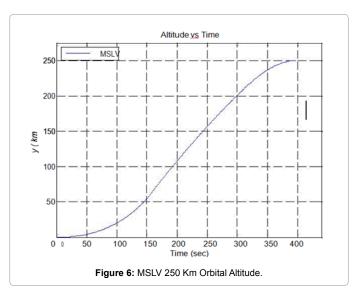
We then determine the relative payload ratios,  $\alpha_k$  (k=2,3) such that proportional total payload ratio,  $\lambda_T = \lambda_1 \prod_{k=1}^N \alpha_k$  can be determine for MSLV.

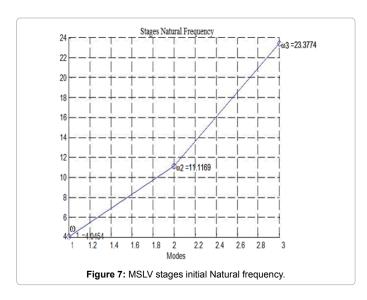
On the basis of VEGA Launch vehicle parameters, we use this model formulation to develop a new approach to parameter inversion of  $\lambda_k$  and total orbital velocity requirement  $V_T$  from existing launch vehicle for proportional mass model of 3-stage MSLV suitable for deployment of micro satellite payload to orbit using the Equations (11-18)

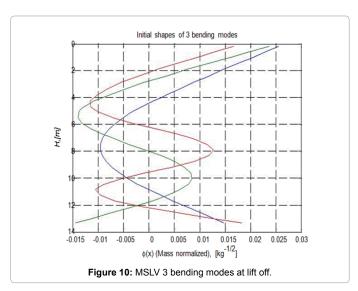
Derived Parameters	1 <sup>st</sup> Stage i=1	2 <sup>nd</sup> Stage i=2	3 <sup>rd</sup> Stage i=3
Gross Mass $m_{0k}$ (Kg)	134,485	38,199	12,448
Stage Mass $m_{plk}(m_{0(k+1)})$ (Kg)	38,689	12,448	1500 (m <sub>sat</sub> )
$\lambda_k = rac{m_{0(k+1)}}{m_{0k}}$ Stage Ratios	0.287682	0.325872	0.120501
Sigma	1	1.133	0.419
$rac{V_T^{vega}}{V_{ek}^{vega}}$	10611.30/2744		
$eta_k^{vega}$	1	1.03214	1.054
$oldsymbol{lpha}_k^{vega}$	1	1.13275	0.41887
$\sigma_k^{ extit{veg}a}$	0.0776	0.0716	0.0725
$\mathcal{V}_k^{vega}$	2.93663	2.78404	4.89070
$m_{01} = \frac{m_{sat}}{\prod_{k=1}^{n} \lambda_k} = \frac{m_{sat}}{0.011322} = 88.32 m_{sat}$	For $\sigma_1$ =0.0776 $\sigma_2$ =0.0716 $\sigma_3$ =0.0726		
$m_{01} = \frac{m_{sat}}{\prod_{k=1}^{n} \lambda_k} = \frac{m_{sat}}{0.00709} = 141.044 m_{sat}$	For $\sigma_1$ =0.1 $\sigma_2$ =0.1 $\sigma_3$ =0.1		
$m_{01} = \frac{m_{sat}}{\prod_{k=1}^{n} \lambda_k} = \frac{m_{sat}}{0.002529} = 395.41 m_{sat}$	For $\sigma_1$ =0.15 $\sigma_2$ =0.15 $\sigma_3$ =0.15		

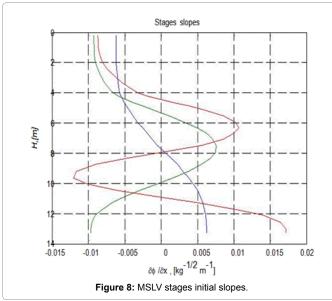
Table 3: Derived Mass distribution on MSLV at structural mass fraction 0.0776(VEGA), 0.1 and 0.15.

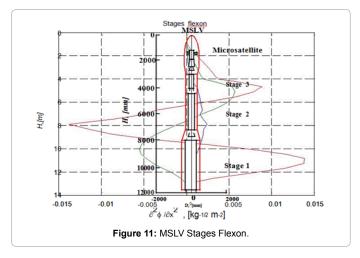












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140	500	4000	4500	2000	250
140	500	1000	1500 [kg m <sup>-1</sup> ]	2000	250

Parameters	Stage 1	Stage 2	Stage 3
Gross Mass (KG)	11864.10	1775.58	236.89 plus payload
Stage Mass (KG)	10088.52	1568.69	206.89
Propellent Mass (KG)	8575.24	1333.38	175.86
Inert Mass (KG)	1513.28	235.30	31.03
Thrust (KN)	291.40	35.40	4.64

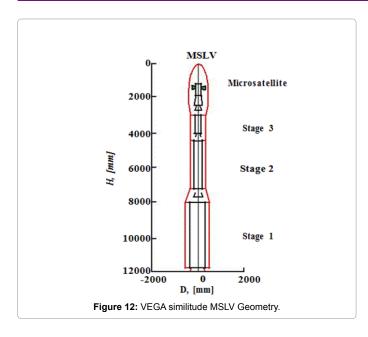
Table 4: MSLV Vehicle parameters.

and parameters of VEGA launch vehicle from published manual [2].

Considering the mass distribution of VEGA [6], VEGA Rockets lass fraction at 92.6 percent propellant and 7.4 percent structure and payload are on the extreme edge of ability to fabricate, and its adaptability to MSLV due to its slender nature becomes unrealistic (Table 3). Lightweight structures made of aluminum, magnesium, titanium, and composites of epoxy-graphite are the norm for MSLV and therefore MSLV mass fraction at 85 percent propellant and 15 percent structure and payload was envisaged and considered in this study and was used to derive mass distribution as follows:

Payload=2(10 kg)

Poly-Pico Satellite Orbital Deployer (P-POD) deployment mechanism=10 Kg



$$m_{01} = \frac{m_{sat}}{\prod\limits_{k=1}^{n} \lambda_k} = \frac{m_{sat}}{0.002529} = 395.41 m_{sat}$$

Total lift off Mass=11864.10 Kg

# Plots of Stages Parameters Distribution and Bending Modes

Plots of stages parameters distribution and bending modes are shown in Figures 5-12.

# **Discussion of Results**

Respective plots for mass distribution (Figure 5), Natural frequency of the structural compartment at 0.15 structural mass fraction (Figure 7), bending modes (Figure 10), slopes (Figure 8) and MSLV similitude geometry of VEGA (Figure 12) is shown above using a scale down derivation models based on hybrid models of theoretical and empirical analysis and parameterized using existing VEGA launch vehicle (LV) technical data. The mass distribution plot indicate the uneven mass distribution for first, second and third stage and therefore a significant body elastic displacement during the rapid propellant burning and at the payload compartment (Figure 11 and Table 4).

On the basis of centre of mass formulation of equation (16), the governing equations of motion on system dynamics suitable for flight of a three stage MSLV model as slender, distributed mass (Figure 4) and variable point mass with internal flow over rotating and spherical Earth is defined and can form the basis for improved mathematical models of translational motion of MSLV. The model can also reveal the effect of lumped masses on the stability of slender body with internal flow where the system has several point masses at various locations.

#### Conclusion

Within the framework of this study, Prototype three stage micro-satellite launch equipment as a similitude of the European Space Agency's VEGA launcher using a scale down derivation models and parameterized using existing VEGA launch vehicle (LV) technical data has being developed. VEGA launch data, total orbital velocity for 250 Km orbital requirement including the losses and stage payload ratio are inferred and applied to the model of parameterization of launch vehicles through coupled-parameters simulations. This approach can be helpful in viability and performance insights in terms of payload mass, stage mass distribution and material properties precision and effectiveness. It can also serve as a system engineering platform for evaluating parameters variability on real launch vehicles, optimizing cost functions, and jump-starting achievable technologies for real implementation.

#### References

- Schoneman S, Chadwick M, Amorosi L (2003) A New Space Launch Vehicle: Low Cost Access to Space Using Surplus Peacekeeper ICBM Motors. A program managed by the Air Force Rocket Systems Launch Program (RSLP).
- Zipfel PH (2000) Modeling and Simulation of Aerospace Vehicle Dynamics. AIAA Education Series, American Institute of Aeronautics and Astronautics, Reston, VA.
- Seywald H, Cliff EM (1989) Optimal Rocket-Powered Ascent Study. American Control Conference, Institute of Electrical and Electronics Engineers, Pittsburgh, USA.
- Curtis H (2013) Orbital Mechanics for Engineering Students. Butterworth-Heinemann (3rdedn.), USA.
- Sutton GP, Biblarz O (2001) Rocket Propulsion Elements. John Wiley & Sons Inc., New York, NY, USA.
- 6. VEGA user's manual (2006) Arianespace©, France.
- 7. Matthew RC (2009) NPS Cubesat Launcher Design, Process and Requirements.
- Isakowitz SJ (2004) International Reference Guide to Space Launch Systems. AIAA, (4th edn.), Washinton DC, USA.
- Braun RD, Moore AA, Kroo IM (1997) Collaborative approach to launch vehicle design. Journal of Spacecraft and Rockets 34: 478-485.