

Energy Deposition by Swift Hadrons in Mixed Gas Targets: The Mean Excitation Energy of Planetary Atmospheres

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In many widely varying types of systems, energy is deposited by the collision of swift hadrons (typically H⁺ or He²⁺), with target molecules, resulting in the conversion of projectile kinetic energy to various types of energy in the target, through various processes. The ability to absorb energy from a hadronic projectile is referred to as the *stopping power* or linear energy transfer (LET), $-dE/dx$, of the target species.

For a single component system, the stopping power for fast projectiles can be described in SI units by Bethe's formulation [1].

$$-\frac{dE}{dx} = n \frac{4\pi e^4 Z_1^2 Z_2^2}{mv^2} \ln \frac{2mv^2}{I_0} \quad (1)$$

Here, n is the scatterer density, Z_1 is the projectile charge, Z_2 is the target electron number, v is the projectile velocity and m and e are the electron mass and charge, respectively. The quantity I_0 is the *mean excitation energy* of the target, and is the single materials quantity that describes the ability of the target to absorb energy from a projectile [1]. It is obtained as the first energy weighted moment of the dipole oscillator strength distribution of the target [1,2].

$$\ln I_0 = \frac{\int \frac{df}{dE} \ln E dE}{\int \frac{df}{dE} dE} \quad (2)$$

It should be noted that the complete dipole oscillator strength distribution of the target, including all discrete and continuous transitions, is required.

In many situations, however, such as planetary atmospheres, [1] plasmas and warm, dense matter, the target can be composed of various components with various scatterer densities. In order to treat the stopping power of such a mixture, providing the components are non-interacting, each component would be treated separately and the results summed, as

$$\frac{dE}{dx} = \sum_{i=\text{components}} \left(\frac{dE}{dx} \right)_i \quad (3)$$

However, it would be more convenient to treat the mixture as a single substance as in eq.1, with its own mean excitation energy, I_0^{mix} . The stopping power for the mixture as a whole for a projectile of charge Z_1 would then be

$$\left(-\frac{dE}{dx} \right)_{\text{mix}} = n_{\text{mix}} \frac{4\pi e^4 Z_1^2 Z_{\text{mix}}^2}{mv^2} \ln \frac{2mv^2}{I_0^{\text{mix}}} \quad (4)$$

Here, n_{mix} is a density of scattering centers, where $n_{\text{mix}} = \sum_i n_i$. Z_{mix} is the weighted average of the number of electrons per scatterer, $Z_{\text{mix}} = \frac{\sum_i n_i Z_i}{n_{\text{mix}}}$, and I_0^{mix} is the mean excitation energy appropriate to the mixture. Such treatment would derive from a sum of stopping

powers of the components, weighted by their relative density of scattering centers, as in eq. 3.

$$\begin{aligned} \left(-\frac{dE}{dx} \right)_{\text{mix}} &= \sum_i n_i \frac{4\pi e^4 Z_1^2 Z_i^2}{mv^2} \ln \frac{2mv^2}{I_0^i} \\ &= \frac{4\pi e^4 Z_1^2}{mv^2} \sum_i n_i Z_i^2 \ln \frac{2mv^2}{I_0^i} \end{aligned} \quad (5)$$

Equating equations 4 and 5, one obtains

$$\ln I_0^{\text{mix}} = \frac{\sum_i n_i Z_i \ln I_0^i}{\sum_i n_i Z_i} \quad (6)$$

Thus, the mean excitation energy of the mixture of non-interacting components is simply the appropriate weighted average of the mean excitation energies of those components.

Applying the foregoing to the constituents of the atmospheres of solar planets [5] and using the standard molecular mean excitation energies of Janni [6], a single mean excitation energy for each of the solar planetary atmospheres can be calculated. The molecular mean excitation energies used were: $I_0^{\text{He}} = 39.10\text{eV}$, $I_0^{\text{H}_2} = 20.40\text{eV}$, $I_0^{\text{O}_2} = 115.7\text{eV}$, $I_0^{\text{CO}_2} = 102.35\text{eV}$.

The results for the mean excitation energies of the atmospheres for the solar planets are given in the Table 1.

It should be noted that trace atmospheric components (<1%) were not included, as inclusions make very small differences in the mean excitation energies of the atmosphere, and even smaller differences in the values of $\ln I_0$, which is the quantity that governs energy deposition by swift, massive particles in the atmospheres. For example, the mean excitation energy for Earth's atmosphere, without including the 1% Ar is 101.89 eV, leading to a difference of 0.59 in I_0 and 0.006 in $\ln I_0$.

Thus, energy deposition by auroral hadrons in planetary atmospheres, such as, for the many newly discovered Goldilocks planets, may be accurately estimated from the projectile flux and planetary composition.

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Planet	Atmospheric composition	I_0 (eV)
Mercury	98% He 2% H ²	38.59
Venus	96.5% CO ₂ 3.5% N ₂	102.24
Earth	78.1% N ₂ 20.9% O ₂ 1% Ar	102.48
Mars	95.3% CO ₂ 2.7% N ₂ 2% Ar	103.25
Jupiter, Saturn Uranus, Neptune	89% H ₂ 11% He	24.43

Table 1: Mean excitation energies of the atmospheres of the solar planets

References

1. Bethe H (1930) Ann. Phys (Leipzig) 5, 325.
2. Inokuti M (1971) Inelastic collisions of fast charged particles with atoms and molecules-Bethe theory revisited. Rev Mod Phys 43: 297-437.
3. Sabin JR, Oddershede J, Cabrera-Trujillo R, Sauer SPA, Deumens E, et al. (2010) Stopping power of molecules for fast ions. Mol Phys 108: 2891-2897.
4. Sabin JR (2013) Suggestion for study of an aspect of energy deposition by auroral particles in planetary atmospheres. J Phys Chem Biophys 3: e114.
5. National Space Science Data Center's Fact Sheet.
6. Janni JF (1982) Proton Range-Energy Tables, 1 keV-10 GeV, Energy Loss, Range, Path Length, Time-of-Flight, Straggling, Multiple Scattering, and Nuclear Interaction Probability. Part I. For 63 Compounds. At Data Nuc Data Tables 27: 147.